tkz-euclide

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\texttt{tkz-euclide} 4.00 is now independent of \texttt{tkz-base}. It is a set of convenient macros for drawing in a plane (fundamental two-dimensional object) with a Cartesian coordinate system. It handles the most classic situations in Euclidean Geometry. \texttt{tkz-euclide} is built on top of PGF and its associated front-end TikZ and is a (La)TeX-friendly drawing package. The aim is to provide a high-level user interface to build graphics relatively simply. The idea is to allow you to follow step by step a construction that would be done by hand as naturally as possible.

English is not my native language so there might be some errors.

\textit{Firstly, I would like to thank Till Tantau for the beautiful \LaTeX package, namely \texttt{TikZ}.}

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\textit{You can find some examples on my site: altermundus.fr. under construction!}

Please report typos or any other comments to this documentation to: Alain Matthes.
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Part I.

General survey: a brief but comprehensive review
1. Installation

`tkz-euclide` is on the server of the CTAN\(^1\). If you want to test a beta version, just put the following files in a `texmf` folder that your system can find. You will have to check several points:

- The `tkz-euclide` folder must be located on a path recognized by `latex`.
- The `tkz-euclide` uses `xfp`.
- This documentation and all examples were obtained with `lualatex` but `pdflatex` or `xelatex` should be suitable.

---

\(^1\) `tkz-euclide` is part of TeXLive and `tlmgr` allows you to install them. This package is also part of MiKTeX under Windows.
2. Presentation and Overview

2.1. Why \texttt{tkz-euclide}?

My initial goal was to provide other mathematics teachers and myself with a tool to quickly create Euclidean geometry figures without investing too much effort in learning a new programming language. Of course, \texttt{tkz-euclide} is for math teachers who use \LaTeX{} and makes it possible to easily create correct drawings by means of \LaTeX{}.

It appeared that the simplest method was to reproduce the one used to obtain construction by hand. To describe a construction, you must, of course, define the objects but also the actions that you perform. It seemed to me that syntax close to the language of mathematicians and their students would be more easily understandable; moreover, it also seemed to me that this syntax should be close to that of \LaTeX{}. The objects, of course, are points, segments, lines, triangles, polygons and circles. As for actions, I considered five to be sufficient, namely: define, create, draw, mark and label.

The syntax is perhaps too verbose but it is, I believe, easily accessible. As a result, the students like teachers were able to easily access this tool.

2.2. \texttt{TikZ} vs \texttt{tkz-euclide}

I love programming with \texttt{TikZ}, and without \texttt{TikZ} I would never have had the idea to create \texttt{tkz-euclide} but never forget that behind it there is \texttt{TikZ} and that it is always possible to insert code from \texttt{TikZ}. \texttt{tkz-euclide} doesn't prevent you from using \texttt{TikZ}. That said, I don't think mixing syntax is a good thing.

There is no need to compare \texttt{TikZ} and \texttt{tkz-euclide}. The latter is not addressed to the same audience as \texttt{TikZ}. The first one allows you to do a lot of things, the second one only does geometry drawings. The first one can do everything the second one does, but the second one will more easily do what you want.

The main purpose is to define points to create geometrical figures. \texttt{tkz-euclide} allows you to draw the essential objects of Euclidean geometry from these points but it may be insufficient for some actions like coloring surfaces. In this case you will have to use \texttt{TikZ} which is always possible.

Here are some comparisons between \texttt{TikZ} and \texttt{tkz-euclide}. For this I will use the geometry examples from the \texttt{PGFManual}. The two most important Euclidean tools used by early Greeks to construct different geometrical shapes and angles were a compass and a straightedge. My idea is to allow you to follow step by step a construction that would be done by hand (with compass and straightedge) as naturally as possible.

2.2.1. Book I, proposition I _Euclid's Elements_

To construct an equilateral triangle on a given finite straight line.

Explanation:
The fourth tutorial of the \texttt{PgfManual} is about geometric constructions. \textit{T. Tantau} proposes to get the drawing with its beautiful tool \texttt{TikZ}. Here I propose the same construction with \texttt{tkz-elements}. The color of the \texttt{TikZ} code is green and that of \texttt{tkz-elements} is red.
\usepackage{tikz}
\usetikzlibrary{calc,intersections,through,backgrounds}
\usepackage{tkz-euclide}

How to get the line AB? To get this line, we use two fixed points.

\coordinate [label=left:$A$] (A) at (0,0);
\coordinate [label=right:$B$] (B) at (1.25,0.25);
\draw (A) -- (B);
\tkzDefPoint(0,0){A}
\tkzDefPoint(1.25,0.25){B}
\tkzDrawSegment(A,B)
\tkzLabelPoint[left](A){$A$}
\tkzLabelPoint[right](B){$B$}

We want to draw a circle around the points A and B whose radius is given by the length of the line AB.

\draw let \p1 = ($ (B) - (A)$), \n2 = {veclen(\x1,\y1)} in
(A) circle (\n2)
(B) circle (\n2);
\tkzDrawCircles(A,B B,A)

The intersection of the circles $\mathcal{D}$ and $\mathcal{E}$

\draw [name path=A--B] (A) -- (B);
node (D) [name path=D,draw,circle through=(B),label=left:$D$] at (A) {GC};
node (E) [name path=E,draw,circle through=(A),label=right:$E$] at (B) {GC};
path [name intersections={of=D and E, by={left:$C$}C, right:$C'$}C'];
\draw [name path=C--C',red] (C) -- (C');
path [name intersections={of=A--B and C--C', by=F}];
node [fill=red,inner sep=1pt,label=-45:$F$] at (F) {GC};
\tkzInterCC(A,B)(B,A) \tkzGetPoints{C}{X}

How to draw points:
\foreach \point in {A, B, C}
\fill [black,opacity=.5] (\point) circle (2pt);
\tkzDrawPoints[fill=gray,opacity=.5](A,B,C)

2.2.2. Complete code with tkz-euclide

We need to define colors
\colorlet{input}{red!80!black}
\colorlet{output}{red!70!black}
\colorlet{triangle}{orange!40}
\begin{tikzpicture}
[\scale=1.25, thick, help lines/.style={\thin, draw=\black!50}]
\tkzDefPoint(0,0){A}
\tkzDefPoint(1.25+\rand(),0.25+\rand()){B}
\tkzInterCC(A,B)(B,A) \tkzGetPoints{C}{X}
\tkzFillPolygon[\triangle, opacity=.5](A,B,C)
\tkzDrawSegment[\input](A,B)
\tkzDrawSegments[\red](A,C B,C)
\tkzDrawCircles[\help lines](A,B B,A) \tkzGetPoints{C}{X}
\tkzDefMidPoint(A,B)
\tkzGetPoint{C}
\tkzLabelPoints(A,B)
\tkzLabelCircle[below=12pt](A,B)(180){$D$}
\tkzLabelCircle[above=12pt](B,A)(180){$E$}
\tkzLabelPoint[above, \red](C){$C$}
\tkzDrawPoints[fill=\gray, opacity=.5](A,B,C)
\end{tikzpicture}

\textbf{Book I, Proposition II \Euclid's Elements}  \\
\textit{To place a straight line equal to a given straight line with one end at a given point.}

\textbf{Explanation}

In the first part, we need to find the midpoint of the straight line AB. With Ti\kz we can use the calc library

\begin{verbatim}
\coordinate [label=left:$A$] (A) at (0,0);
\coordinate [label=right:$B$] (B) at (1.25,0.25);
\draw (A) -- (B);
\node [fill=red, inner sep=1pt, label=below:$X$] (X) at (\nodepart{left} (A)!.5!(B)) {};
\end{verbatim}

With tkz-euclide we have a macro \texttt{tkzDefMidPoint}, we get the point X with \texttt{tkzGetPoint} but we don't need this point to get the next step.
2. Presentation and Overview

Then we need to construct a triangle equilateral. It's easy with \texttt{tkz-euclide}. With TikZ you need some effort because you need to use the midpoint \(X\) to get the point \(D\) with trigonometry calculation.

\begin{verbatim}
\tkzDefPoints{0/0/A,0.75/0.25/B,1/1.5/C}
\tkzDefMidPoint(A,B) \tkzGetPoint{X}

\node [fill=red,inner sep=1pt,label=below:$X$] (X) at ($ (A)!.5!(B) $) {}; \tkzDrawPolygon{A,B,C}
\node [fill=red,inner sep=1pt,label=above:$D$] (D) at ($ (X) ! {\sin(60)*2} ! 90:(B) $) {}; \tkzDefTriangle[eqilateral](A,B) \tkzGetPoint{D}
\end{verbatim}

We can draw the triangle at the end of the picture with

\begin{verbatim}
\tkzDrawPolygon{A,B,C}
\end{verbatim}

We know how to draw the circle \(\mathcal{H}\) around \(B\) through \(C\) and how to place the points \(E\) and \(F\)

\begin{verbatim}
\node (H) [label=135:$H$,draw,circle through=(C)] at (B) {}; \tkzDrawCircle(B,C)
\draw (D) -- ($ (D) ! 3.5 ! (B) $) coordinate [label=below:$F$] (F);
\draw (D) -- ($ (D) ! 2.5 ! (A) $) coordinate [label=below:$E$] (E);
\tkzDrawLines[add=0 and 2](D,A D,B) \tkzDrawCircle(B,C)
\tkzDrawLines[add=0 and 2](D,A D,B)
\tkzDrawCircle(D,G)
\tkzInterLC(D,A)(D,G)\tkzGetSecondPoint{L}
\end{verbatim}

Like the intersection of two circles, it's easy to find the intersection of a line and a circle with \texttt{tkz-euclide}. We don't need \(F\)

\begin{verbatim}
\tkzInterLC(B,D)(B,C)\tkzGetFirstPoint{G}
\end{verbatim}

There are no more difficulties. Here the final code with some simplications. We draw the circle \(\mathcal{K}\) with center \(D\) and passing through \(G\). It intersects the line \(AD\) at point \(L\). \(AL = BC\).

\begin{verbatim}
\tkzDrawCircle(D,G) \tkzInterLC(D,A)(D,G)\tkzGetSecondPoint{L}
\end{verbatim}
2. Presentation and Overview

2.3. \texttt{tkz-euclide4} vs \texttt{tkz-euclide3}

Now I am no longer a Mathematics teacher, and I only spend a few hours studying geometry. I wanted to avoid multiple complications by trying to make \texttt{tkz-euclide} independent of \texttt{tkz-base}. Thus was born \texttt{tkz-euclide 4}. The latter is a simplified version of its predecessor. The macros of \texttt{tkz-euclide 3} have been retained. The unit is now \texttt{cm}. If you need some macros from \texttt{tkz-base}, you may need to use the \texttt{tkzInit}.

2.4. How to use the \texttt{tkz-euclide} package?

2.4.1. Let's look at a classic example

In order to show the right way, we will see how to build an equilateral triangle. Several possibilities are open to us, we are going to follow the steps of Euclid.

- First of all, you have to use a document class. The best choice to test your code is to create a single figure with the class \texttt{standalone}.

\begin{verbatim}
\documentclass{standalone}
\end{verbatim}

- Then load the \texttt{tkz-euclide} package:

\begin{verbatim}
\usepackage{tkz-euclide}
\end{verbatim}

You don't need to load Ti\textit{k}Z because the \texttt{tkz-euclide} package works on top of TikZ and loads it.

- Start the document and open a TikZ picture environment:

\begin{verbatim}
\begin{document}
\begin{tikzpicture}
\end{verbatim}

- Now we define two fixed points:

\begin{verbatim}
\tkzDefPoint(0,0){A}
\tkzDefPoint(5,2){B}
\end{verbatim}
Two points define two circles, let's use these circles: circle with center A through B and circle with center B through A. These two circles have two points in common.

\tkzInterCC(A,B)(B,A)

We can get the points of intersection with

\tkzGetPoints{C}{D}

All the necessary points are obtained, we can move on to the final steps including the plots.

\tkzDrawCircles[gray,dashed](A,B,B,A)
\tkzDrawPolygon(A,B,C)% The triangle

Draw all points A, B, C and D:

\tkzDrawPoints(A,...,D)

The final step, we print labels to the points and use options for positioning:

\tkzLabelSegments[swap](A,B){$c$}
\tkzLabelPoints(A,B,D)
\tkzLabelPoints[above](C)

We finally close both environments

\end{tikzpicture}
\end{document}

The complete code

\begin{tikzpicture}[scale=.5]
% fixed points
\tkzDefPoint(0,0){A}
\tkzDefPoint(5,2){B}
% calculus
\tkzInterCC(A,B)(B,A)
\tkzGetPoints{C}{D}
% drawings
\tkzDrawCircles(A,B,B,A)
\tkzDrawPolygon(A,B,C)
\tkzDrawPoints(A,...,D)
% marking
\tkzMarkSegments[mark=s||](A,B B,C C,A)
% labelling
\tkzLabelSegments[swap](A,B){$c$}
\tkzLabelPoints(A,B,D)
\tkzLabelPoints[above](C)
\end{tikzpicture}
2.4.2. Part I: golden triangle

Let's analyze the figure

1. CBD and DBE are isosceles triangles;
2. BC = BE and (BD) is a bisector of the angle CBE;
3. From this we deduce that the CBD and DBE angles are equal and have the same measure $\alpha$

$$\angle BAC + \angle ABC + \angle BCA = 180^\circ$$ in the triangle BAC

$$3\alpha + \angle BCA = 180^\circ$$ in the triangle CBD

then

$$\alpha + 2\angle BCA = 180^\circ$$

or

$$\angle BCA = 90^\circ - \alpha/2$$

4. Finally

$$\angle CBD = \alpha = 36^\circ$$

the triangle CBD is a "gold" triangle.

How construct a gold triangle or an angle of $36^\circ$?

1. We place the fixed points C and D. \tkzDefPoint{0,0}{C} and \tkzDefPoint{4,0}{D};
2. We construct a square CDef and we construct the midpoint m of [Cf];
   We can do all of this with a compass and a rule;
3. Then we trace an arc with center m through e. This arc cross the line (Cf) at n;
4. Now the two arcs with center C and D and radius Cn define the point B.
After building the golden triangle $BCD$, we build the point $A$ by noticing that $BD = DA$. Then we get the point $E$ and finally the point $F$. This is done with already intersections of defined objects (line and circle).

\begin{tikzpicture}
\tkzDefPoint(0,0){C}
\tkzDefPoint(4,0){D}
\tkzDefSquare(C,D)
\tkzGetPoints{e}{f}
\tkzDefMidPoint(C,f)
\tkzGetPoint{m}
\tkzInterLC(C,f)(m,e)
\tkzGetSecondPoint{n}
\tkzInterCC[nodes](C,C,n)(D,C,n)
\tkzGetFirstPoint{B}
\tkzInterLC(C,D)(D,B) \tkzGetSecondPoint{A}
\tkzInterLL(B,D)(C,E) \tkzGetPoint{F}
\tkzDrawPoints(C,D,B)
\tkzDrawPolygon(B,...,D)
\tkzDrawPolygon(B,C,D)
\tkzDrawSegments(D,A A,B C,E)
\tkzDrawArc[delta=10](B,C)(E)
\tkzDrawPoints(A,...,F)
\tkzMarkRightAngle(B,F,C)
\tkzMarkAngles(C,B,D E,A,D)\{\alpha\}
\tkzLabelPoints{below}(A,C,D,E)
\tkzLabelPoints[above right](B,F)
\end{tikzpicture}

2.4.3. Part II: two others methods with golden and euclid triangle

\textbf{tkz-euclide} knows how to define a "golden" or "euclid" triangle. We can define $BCD$ and $BCA$ like gold triangles.

\begin{tikzpicture}
\tkzDefPoint(0,0){C}
\tkzDefPoint(4,0){D}
\tkzDefSquare(C,D)
\tkzGetPoints{e}{f}
\tkzDefMidPoint(C,f)
\tkzGetPoint{m}
\tkzInterLC(C,f)(m,e)
\tkzGetSecondPoint{n}
\tkzInterCC[nodes](C,C,n)(D,C,n)
\tkzGetFirstPoint{B}
\tkzInterLC(C,D)(D,B) \tkzGetSecondPoint{A}
\tkzInterLL(B,D)(C,E) \tkzGetPoint{F}
\end{tikzpicture}
2. Presentation and Overview

\begin{tikzpicture}
\tkzDefPoint(0,0){C}
\tkzDefPoint(4,0){D}
\tkzDefTriangle[euclid](C,D)
\tkzGetPoint{B}
\tkzDefTriangle[euclid](B,C)
\tkzGetPoint{A}
\tkzInterLC(B,A)(B,D) \tkzGetSecondPoint{E}
\tkzInterLL(B,D)(C,E) \tkzGetPoint{F}
\tkzDrawPoints(C,D,B)
\tkzDrawPolygon(B,...,D)
\tkzDrawPolygon(B,C,D)
\tkzDrawSegments(D,A A,B C,E)
\tkzDrawArc[delta=10](B,C)(E)
\tkzDrawPoints(A,...,F)
\tkzMarkRightAngle(B,F,C)
\tkzMarkAngles[C,B,D E,A,D]{\alpha}
\tkzLabelPoints[below](A,C,D,E)
\tkzLabelPoints[above right](B,F)
\end{tikzpicture}

Here is a final method that uses rotations:

\begin{tikzpicture}
\tkzDefPoint(0,0){C}
\tkzDefPoint[below:$C$](0,0){C}
\tkzDefPoint(2,6){B}
\tkzDefPointBy[rotation= center B angle 36](C) \tkzGetPoint{D}
\tkzDefPointBy[rotation= center B angle 72](C) \tkzGetPoint{E}
\tkzInterLL(B,E)(C,D) \tkzGetPoint{A}
\tkzInterLL(C,E)(B,D) \tkzGetPoint{H}
\tkzDrawArc[delta=10](B,C)(E)
\tkzDrawPolygon(C,B,D)
\tkzDrawSegments(D,A B,A C,E)
\tkzMarkAngles[C,B,D E,A,D]{\alpha}
\tkzLabelPoints[below]{$A,C,D,E$}
\tkzLabelPoints[above right]{$B,F$}
\end{tikzpicture}

2.4.4. Complete but minimal example

A unit of length being chosen, the example shows how to obtain a segment of length $\sqrt{a}$ from a segment of length $a$, using a ruler and a compass.

IB = a, AI = 1
2. Presentation and Overview

Comments

– The Preamble

Let us first look at the preamble. If you need it, you have to load \texttt{xcolor} before \texttt{tkz-euclide}, that is, before \texttt{Ti\kern-0.1em kZ}. \texttt{Ti\kern-0.1em kZ} may cause problems with the active characters, but... provides a library in its latest version that's supposed to solve these problems \texttt{babel}.

\begin{verbatim}
\documentclass{standalone} \% or another class
  \% \usepackage{xcolor} \% before \texttt{tikz} or \texttt{tkz-euclide} if necessary
\usepackage{tkz-euclide} \% no need to load \texttt{TikZ}
  \% \usetkzobj{all} is no longer necessary
  \% \usetikzlibrary{babel} if there are problems with the active characters
\end{verbatim}

The following code consists of several parts:

– Definition of fixed points: the first part includes the definitions of the points necessary for the construction, these are the fixed points. The macros \texttt{\texttt{\texttt{tkzInit}}} and \texttt{\texttt{\texttt{tkzClip}}} in most cases are not necessary.

\begin{verbatim}
\tkzDefPoint(0,0){A}
\tkzDefPoint(1,0){I}
\end{verbatim}

– The second part is dedicated to the creation of new points from the fixed points; a B point is placed at 10 cm from A. The middle of [AB] is defined by M and then the orthogonal line to the (AB) line is searched for at the I point. Then we look for the intersection of this line with the semi-circle of center M passing through A.

\begin{verbatim}
\tkzDefPointBy[homothety=center A ratio 10 ](I)
\tkzGetPoint{B}
\tkzDefMidPoint(A,B)
\tkzGetPoint{M}
\tkzDefPointWith[orthogonal](I,M)
\tkzGetPoint{H}
\tkzInterLC(I,H)(M,B)
\tkzGetSecondPoint{C}
\end{verbatim}

– The third one includes the different drawings;
2. Presentation and Overview

- Marking: the fourth is devoted to marking:

\tkzMarkRightAngle[ra](A,I,C)

- Labelling: the latter only deals with the placement of labels.

\tkzLabelPoint[left](A){$A(0,0)$}
\tkzLabelPoint[right](B){$B(10,0)$}
\tkzLabelSegment[right=4pt](I,C){$\sqrt{a^2}=a \ (a>0)$}

- The full code:

\begin{tikzpicture}[scale=1,ra/.style={fill=gray!20}]
% fixed points
\tkzDefPoint(0,0){A}
\tkzDefPoint(1,0){I}
% calculation
\tkzDefPointBy[homothety=center A ratio 10](I) \tkzGetPoint{B}
\tkzDefMidPoint(A,B) \tkzGetPoint{M}
\tkzDefPointWith[orthogonal](I,M) \tkzGetPoint{H}
\tkzInterLC(I,H)(M,B) \tkzGetSecondPoint{C}
\tkzDrawSegment[style=orange](I,C)
\tkzDrawArc(M,B)(A)
\tkzDrawSegment[dim={$1$,-16pt,}](A,I)
\tkzDrawSegment[dim={$a/2$,-16pt,}](I,M)
\tkzDrawSegment[dim={$a/2$,-10pt,}](M,B)
\tkzMarkRightAngle[ra](A,I,C)
\tkzDrawPoints(I,A,B,C,M)
\tkzLabelPoint[left](A){$A(0,0)$}
\tkzLabelPoints[above right](I,M)
\tkzLabelPoints[above left](C)
\tkzLabelPoint[right](B){$B(10,0)$}
\tkzLabelSegment[right=4pt](I,C){$\sqrt{a^2}=a \ (a>0)$}
\end{tikzpicture}
3. The Elements of tkz code

To work with my package, you need to have notions of \LaTeX as well as Ti\kZ.
In this paragraph, we start looking at the "rules" and "symbols" used to create a figure with \texttt{tkz-euclide}.

3.1. Objects and language

The primitive objects are points. You can refer to a point at any time using the name given when defining it. (it is possible to assign a different name later on).
To get new points you will use macros. \texttt{tkz-euclide} macros have a name beginning with \texttt{tkz}. There are four main categories starting with: \texttt{tkzDef...}\texttt{tkzDraw...}\texttt{tkzMark...} and \texttt{tkzLabel...}. The used points are passed as parameters between parentheses while the created points are between braces.
The code of the figures is placed in an environment \texttt{tikzpicture}

\begin{tikzpicture}
  \node (A) at (0,0) {A};
  \node (B) at (8,0) {B};
  \draw (A) -- (B);
\end{tikzpicture}

Contrary to Ti\kZ, you should not end a macro with ";". We thus lose the important notion which is the \texttt{path}.
However, it is possible to place some code between the macros \texttt{tkz-euclide}.
Among the first category, \texttt{tkzDefPoint} allows you to define fixed points. It will be studied in detail later. Here we will see in detail the macro \texttt{tkzDefTriangle}.
This macro makes it possible to associate to a pair of points a third point in order to define a certain triangle \texttt{tkzDefTriangle(A,B)}. The obtained point is referenced \texttt{tkzPointResult} and it is possible to choose another reference with \texttt{tkzGetPoint(C)} for example.
\texttt{tkzDefTriangle[euclid}(A,B) \texttt{tkzGetPoint}{C}
Parentheses are used to pass arguments. In \texttt{(A,B)} \texttt{A} and \texttt{B} are the points with which a third will be defined.
However, in \texttt{[C]} we use braces to retrieve the new point.
In order to choose a certain type of triangle among the following choices: equilateral, isosceles right, half, pythagoras, school, golden or sublime, euclid, gold, cheops... and two angles you just have to choose between hooks, for example:

\begin{tikzpicture}[scale=.5]
  \tkzDefPoints{0/0/A,8/0/B}
  \tkzDrawPoints(A,B)
  \foreach \tr in {euclid,gold} {
    \tkzDefTriangle[\tr](A,B) \tkzGetPoint{C}
    \tkzDrawPoint(C)
    \tkzLabelPoint[below](C){\tr}
    \tkzDrawSegments(A,C C,B)}
\end{tikzpicture}
3.2. Notations and conventions

I deliberately chose to use the geometric French and personal conventions to describe the geometric objects represented. The objects defined and represented by \texttt{tkz-euclide} are points, lines and circles located in a plane. They are the primary objects of Euclidean geometry from which we will construct figures. According to Euclid, these figures will only illustrate pure ideas produced by our brain. Thus a point has no dimension and therefore no real existence. In the same way the line has no width and therefore no existence in the real world. The objects that we are going to consider are only representations of ideal mathematical objects. \texttt{tkz-euclide} will follow the steps of the ancient Greeks to obtain geometrical constructions using the ruler and the compass.

Here are the notations that will be used:

- The points are represented geometrically either by a small disc or by the intersection of two lines (two straight lines, a straight line and a circle or two circles). In this case, the point is represented by a cross.

  \begin{tikzpicture}
  \tkzDefPoints{0/0/A,4/2/B}
  \tkzDrawPoints(A,B)
  \tkzLabelPoints(A,B)
  \end{tikzpicture}

- The line segments are designated by two points representing their ends in square brackets: [AB].

  \begin{tikzpicture}
  \tkzDefPoints{0/0/A,4/2/B}
  \tkzSetPoint[shape=cross, color=red](A)
  \tkzDefPoints{0/0/A,4/2/B}
  \tkzDrawPoints(A,B)
  \tkzLabelPoints(A,B)
  \end{tikzpicture}

The existence of a point being established, we can give it a label which will be a capital letter (with some exceptions) of the Latin alphabet such as A, B or C. For example:

- O is a center for a circle, a rotation, etc.;
- M defined a midpoint;
- H defined the foot of an altitude;
- P' is the image of P by a transformation ;

It is important to note that the reference name of a point in the code may be different from the label to designate it in the text. So we can define a point A and give it as label P. In particular the style will be different, point A will be labeled A.

  \begin{tikzpicture}
  \tkzDefPoint(0,0){A}
  \tkzDrawPoints(A)
  \tkzLabelPoint(A){$P$}
  \end{tikzpicture}

Exceptions: some points such as the middle of the sides of a triangle share a characteristic, so it is normal that their names also share a common character. We will designate these points by M_a, M_b and M_c or M_A, M_B and M_C.

In the code, these points will be referred to as: M_A, M_B and M_C.

Another exception relates to intermediate construction points which will not be labelled. They will often be designated by a lowercase letter in the code.

- The line segments are designated by two points representing their ends in square brackets: [AB].
3. The Elements of tkz code

- The straight lines are in Euclidean geometry defined by two points so A and B define the straight line \((AB)\). We can also designate this straight line using the Greek alphabet and name it \((\delta)\) or \((\Delta)\). It is also possible to designate the straight line with lowercase letters such as \(d\) and \(d'\).

- The semi-straight line is designated as follows \([AB)\).

- Relation between the straight lines. Two perpendicular \((AB)\) and \((CD)\) lines will be written \((AB) \perp (CD)\) and if they are parallel we will write \((AB) \parallel (CD)\).

- The lengths of the sides of triangle ABC are \(AB\), \(AC\) and \(BC\). The numbers are also designated by a lowercase letter so we will write: \(AB = c\), \(AC = b\) and \(BC = a\). The letter \(a\) is also used to represent an angle, and \(r\) is frequently used to represent a radius, \(d\) a diameter, \(l\) a length, \(d\) a distance.

- Polygons are designated afterwards by their vertices so ABC is a triangle, EFGH a quadrilateral.

- Angles are generally measured in degrees (ex \(60^\circ\)) and in an equilateral ABC triangle we will write \(\hat{ABC} = \hat{B} = 60^\circ\).

- The arcs are designated by their extremities. For example if A and B are two points of the same circle then \(\widehat{AB}\).

- Circles are noted either \(\mathcal{C}\) if there is no possible confusion or \(\mathcal{C}(O ; A)\) for a circle with center O and passing through the point A or \(\mathcal{C}(O ; 1)\) for a circle with center O and radius 1 cm.

- Name of the particular lines of a triangle: I used the terms bisector, bisector out, mediator (sometimes called perpendicular bisectors), altitude, median and symmedian.

- \((x_1, y_1)\) coordinates of the point \(A_1\), \((x_A, y_A)\) coordinates of the point A.

3.3. Set, Calculate, Draw, Mark, Label

The title could have been: Separation of Calculus and Drawings

When a document is prepared using the \(\LaTeX\) system, the source code of the document can be divided into two parts: the document body and the preamble. Under this methodology, publications can be structured, styled and typeset with minimal effort. I propose a similar methodology for creating figures with \texttt{tkz-euclide}.

The first part defines the fixed points, the second part allows the creation of new points. \texttt{Set and Calculate} are the two main parts. All that is left to do is to draw (or fill), mark and label. It is possible that \texttt{tkz-euclide} is insufficient for some of these latter actions but you can use \texttt{TikZ}.

One last remark that I think is important, it is best to avoid introducing coordinates within a code as much as possible. I think that the coordinates should appear at the beginning of the code with the fixed points. Then the use of references is recommended. Most macros have the option \texttt{nodes} or \texttt{with nodes}.

I also think it’s best to define the styles of the different objects from the beginning.
4. News and compatibility

Some changes have been made to make the syntax more homogeneous and especially to distinguish the definition and search for coordinates from the rest, i.e. drawing, marking and labelling. In the future, the definition macros being isolated, it will be easier to introduce a phase of coordinate calculations using Lua. Here are some of the changes. I’m sorry but the list of changes and novelties is made in the greatest disorder!

– An important novelty is the recent replacement of the \texttt{fp} package by \texttt{xfp}. This is to improve the calculations a little bit more and to make it easier to use;

– Improved code and bug fixes;

– First of all, you don’t have to deal with \texttt{Tik Z} the size of the bounding box. Early versions of \texttt{tkz-euclide} did not control the size of the bounding box. The bounding box is now controlled in each macro (hopefully) to avoid the use of \texttt{\tkzInit} followed by \texttt{\tkzClip};

– With \texttt{tkz-euclide} loads all objects, so there’s no need to place \texttt{\usetkzobj{all}};

– Added macros for the bounding box: \texttt{\tkzSaveBB \tkzClipBB} and so on;

– Logically most macros accept TiKZ options. So I removed the "duplicate" options when possible thus the "label options" option is removed;

– The unit is now the cm;

– \texttt{\tkzCalcLength \tkzGetLength} gives result in cm;

– \texttt{\tkzMarkArc} and \texttt{\tkzLabelArc} are new macros;

– Now \texttt{\tkzClipCircle} and \texttt{\tkzClipPolygon} have an option \texttt{out}. To use this option you must have a Bounding Box that contains the object on which the Clip action will be performed. This can be done by using an object that encompasses the figure or by using the macro \texttt{\tkzInit};

– The options \texttt{end} and \texttt{start} which allowed to give a label to a straight line are removed. You now have to use the macro \texttt{\tkzLabelLine};

– Introduction of the libraries \texttt{quotes} and \texttt{angles}; it allows to give a label to a point, even if I am not in favour of this practice;

– The notion of vector disappears, to draw a vector just pass "->" as an option to \texttt{\tkzDrawSegment};

– \texttt{\tkzDrawMedian}, \texttt{\tkzDrawBisector}, \texttt{\tkzDrawAltitude}, \texttt{\tkzDrawMedians}, \texttt{\tkzDrawBisectors} et \texttt{\tkzDrawAltitudes} do not exist anymore. The creation and drawing separation is not respected so it is preferable to first create the coordinates of these points with \texttt{\tkzDefSpcTriangle[median]} and then to choose the ones you are going to draw with \texttt{\tkzDrawSegments} or \texttt{\tkzDrawLines};

– \texttt{\tkzDefIntSimilitudeCenter} and \texttt{\tkzDefExtSimilitudeCenter} do not exist anymore;

– \texttt{\tkzDrawTriangle} has been deleted. \texttt{\tkzDrawTriangle[equilateral]} was handy but it is better to get the third point with \texttt{\tkzDefTriangle[equilateral]} and then draw with \texttt{\tkzDrawPolygon}; idem for \texttt{\tkzDrawSquare} and \texttt{\tkzDrawGoldRectangle};
4. News and compatibility

- \texttt{tkzDefRandPointOn} is replaced by \texttt{tkzGetRandPointOn};

- now \texttt{tkzTangent} is replaced by \texttt{tkzDefTangent};

- An option of the macro \texttt{tkzDefTriangle} has changed, in the previous version the option was “euclide” with an “e”. Now it’s "euclid”;

- Random points are now in \texttt{tkz-euclide} and the macro \texttt{tkzGetRandPointOn} is replaced by \texttt{tkzDefRandPointOn}. For homogeneity reasons, the points must be retrieved with \texttt{tkzGetPoint};

- New macros have been added: \texttt{tkzDrawSemiCircles}, \texttt{tkzDrawPolygons}, \texttt{tkzDrawTriangles};

- Option "isosceles right” is a new option of the macro \texttt{tkzDefTriangle};

- Appearance of the macro \texttt{usetkztool} which allows to load new "tools”;

- The styles can be modified with the help of the following macros: \texttt{tkzSetUpPoint}, \texttt{tkzSetUpLine}, \texttt{tkzSetUpArc}, \texttt{tkzSetUpCompass}, \texttt{tkzSetUpLabel} and \texttt{tkzSetUpStyle}. The last one allows you to create a new style.
Part II.

Setting
5. First step: fixed points

The first step in a geometric construction is to define the fixed points from which the figure will be constructed. The general idea is to avoid manipulating coordinates and to prefer to use the references of the points fixed in the first step or obtained using the tools provided by the package. Even if it's possible, I think it's a bad idea to work directly with coordinates. Preferable is to use named points.

\texttt{tkz-euclide} uses macros and vocabulary specific to geometric construction. It is of course possible to use the tools of \texttt{TikZ} but it seems more logical to me not to mix the different syntaxes.

A point in \texttt{tkz-euclide} is a particular "node" for \texttt{TikZ}. In the next section we will see how to define points using coordinates. The style of the points (color and shape) will not be discussed. You will find some indications in some examples; for more information you can read the following section 36.

6. Definition of a point : \texttt{\tkzDefPoint} or \texttt{\tkzDefPoints}

Points can be specified in any of the following ways:

- Cartesian coordinates;
- Polar coordinates;
- Named points;
- Relative points.

A point is defined if it has a name linked to a unique pair of decimal numbers. Let \((x,y)\) or \((a:d)\) i.e. \((x\text{ abscissa}, y\text{ ordinate})\) or \((a\text{ angle: d distance})\). This is possible because the plan has been provided with an orthonormed Cartesian coordinate system. The working axes are (ortho)normed with unity equal to 1 cm.

The Cartesian coordinate \((a,b)\) refers to the point \(a\text{ centimeters in the }x\text{-direction and }b\text{ centimeters in the }y\text{-direction.}

A point in polar coordinates requires an angle \(\alpha\), in degrees, and a distance \(d\) from the origin with a dimensional unit by default it’s the \(\text{cm.}\)

The \texttt{\tkzDefPoint} macro is used to define a point by assigning coordinates to it. This macro is based on \texttt{\coordinate}, a macro of \texttt{TikZ}. It can use \texttt{TikZ}-specific options such as \texttt{shift}. If calculations are required then the \texttt{xfp} package is chosen. We can use Cartesian or polar coordinates.

Cartesian coordinates

\begin{tikzpicture}[scale=1]
  \tkzInit[xmax=5,ymax=5]
  \tkzDrawX[>=latex]
  \tkzDrawY[>=latex]
  \tkzDefPoints{0/0/O,1/0/I,0/1/J}
  \tkzDefPoint(3,4){A}
  \tkzDrawPoints(O,A)
  \tkzLabelPoint(A){$A_1 (x_1,y_1)$}
  \tkzShowPointCoord[xlabel=$x_1$,ylabel=$y_1$](A)
  \tkzLabelPoints(O,I,J)
\end{tikzpicture}

Polar coordinates

\begin{tikzpicture}[scale=1]
  \tkzInit[xmax=5,ymax=5]
  \tkzDrawX[>=latex]
  \tkzDrawY[>=latex]
  \tkzDefPoints{0/0/O,1/0/I,0/1/J}
  \tkzDefPoint(40:4){P}
  \tkzDrawSegment[dim={$d$,16pt,above=6pt}](O,P)
  \tkzDrawPoints(O,P)
  \tkzMarkAngle[mark=none,->](I,O,P)
  \tkzFillAngle[opacity=.5](I,O,P){\tkzLabelAngle[pos=1.25](I,O,P){$\alpha$}}
  \tkzLabelPoint(P){$P (\alpha : d)$}
  \tkzDrawPoints[shape=cross](I,J)
  \tkzLabelPoints(O,I,J)
\end{tikzpicture}
6. Definition of a point: \texttt{\texttt{tkzDefPoint}} or \texttt{\texttt{tkzDefPoints}}

\begin{equation}
A(x_1, y_1)
\end{equation}

6.1. Defining a named point \texttt{\texttt{tkzDefPoint}}

\begin{verbatim}
\texttt{\texttt{tkzDefPoint}}[(\texttt{local options})](\texttt{(x,y)})\{(\texttt{ref})\} \texttt{or} \texttt{(\texttt{α:d})}\{(\texttt{ref})\}
\end{verbatim}

<table>
<thead>
<tr>
<th>arguments</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>(x,y)</td>
<td>no default</td>
<td>x and y are two dimensions, by default in cm.</td>
</tr>
<tr>
<td>(α:d)</td>
<td>no default</td>
<td>α is an angle in degrees, d is a dimension</td>
</tr>
<tr>
<td>{ref}</td>
<td>no default</td>
<td>Reference assigned to the point: A, T_a ,P1 or P_1</td>
</tr>
</tbody>
</table>

The obligatory arguments of this macro are two dimensions expressed with decimals, in the first case they are two measures of length, in the second case they are a measure of length and the measure of an angle in degrees. Do not confuse the reference with the name of a point. The reference is used by calculations, but frequently, the name is identical to the reference.

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>label</td>
<td>no default</td>
<td>allows you to place a label at a predefined distance</td>
</tr>
<tr>
<td>shift</td>
<td>no default</td>
<td>adds (x,y) or (α:d) to all coordinates</td>
</tr>
</tbody>
</table>

6.1.1. Cartesian coordinates

\begin{verbatim}
\begin{tikzpicture}
\tkzInit[xmax=5,ymax=5] % limits the size of the axes
\tkzDrawX[>=latex]
\tkzDrawY[>=latex]
\tkzDefPoint(0,0){A}
\tkzDefPoint(4,0){B}
\tkzDefPoint(0,3){C}
\tkzDrawPolygon(A,B,C)
\tkzDrawPoints(A,B,C)
\end{tikzpicture}
\end{verbatim}

\texttt{tkz-euclide} AlterMundus
6. Definition of a point: \texttt{tkzDefPoint} or \texttt{tkzDefPoints}

6.1.2. Calculations with xfp

\begin{tikzpicture}[scale=1]
\tkzInit[xmax=4,ymax=4]
\tkzDrawX\tkzDrawY
\tkzDefPoint(-1+2,sqrt(4)){O}
\tkzDefPoint({3*ln(exp(1))},{exp(1)}){A}
\tkzDefPoint({4*sin(pi/6)},{4*cos(pi/6)}){B}
\tkzDrawPoints(O,B,A)
\end{tikzpicture}

6.1.3. Polar coordinates

\begin{tikzpicture}
\foreach \an [count=\i] in {0,60,...,300}
{ \tkzDefPoint(\an:3){A_\i}}
\tkzDrawPolygon(A_1,A_...,A_6)
\tkzDrawPoints(A_1,A_...,A_6)
\end{tikzpicture}

6.1.4. Relative points

First, we can use the \texttt{scope} environment from Ti\textit{k}Z. In the following example, we have a way to define an equilateral triangle.

\begin{tikzpicture}[scale=1]
\begin{scope}[rotate=30]
\tkzDefPoint(2,3){A}
\begin{scope}[shift=(A)]
\tkzDefPoint(90:5){B}
\tkzDefPoint(30:5){C}
\end{scope}
\end{scope}
\tkzDrawPolygon(A,B,C)
\tkzLabelPoints[above](B,C)
\tkzLabelPoints[below](A)
\tkzDrawPoints(A,B,C)
\end{tikzpicture}

6.2. Point relative to another: \texttt{tkzDefShiftPoint}
6. Definition of a point: \texttt{tkzDefPoint} or \texttt{tkzDefPoints}

<table>
<thead>
<tr>
<th>arguments</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>\langle x, y \rangle</td>
<td>none default</td>
<td>(x) and (y) are two dimensions, by default in cm.</td>
</tr>
<tr>
<td>\langle \alpha, d \rangle</td>
<td>none default</td>
<td>(\alpha) is an angle in degrees, (d) is a dimension</td>
</tr>
<tr>
<td>{\text{ref}}</td>
<td>none default</td>
<td>Reference assigned to the point: A, T_a, P_1 or P_i</td>
</tr>
</tbody>
</table>

options default definition:

\texttt{[pt]} no default \texttt{tkzDefShiftPoint[A](0:4){B}}

6.2.1. Isosceles triangle

This macro allows you to place one point relative to another. This is equivalent to a translation. Here is how to construct an isosceles triangle with main vertex \(A\) and angle at vertex of 30°.

\begin{tikzpicture}[rotate=-30]
\tkzDefPoint(2,3){A}
\tkzDefShiftPoint[A](0:4){B}
\tkzDefShiftPoint[A](30:4){C}
\tkzDrawSegments(A,B B,C C,A)
\tkzMarkSegments[mark=\|](A,B A,C)
\tkzDrawPoints(A,B,C)
\tkzLabelPoints(B,C)
\tkzLabelPoints[above left](A)
\end{tikzpicture}

6.2.2. Equilateral triangle

Let’s see how to get an equilateral triangle (there is much simpler)

\begin{tikzpicture}[scale=1]
\tkzDefPoint(2,3){A}
\tkzDefShiftPoint[A](30:3){B}
\tkzDefShiftPoint[A](-30:3){C}
\tkzDrawPolygon(A,B,C)
\tkzDrawPoints(A,B,C)
\tkzLabelPoints(B,C)
\tkzLabelPoints[above left](A)
\tkzMarkSegments[mark=\|](A,B A,C B,C)
\end{tikzpicture}

6.2.3. Parallelogram

There’s a simpler way

\begin{tikzpicture}
\tkzDefPoint(0,0){A}
\tkzDefPoint(30:3){B}
\tkzDefShiftPointCoord[B](10:2){C}
\tkzDefShiftPointCoord[A](10:2){D}
\tkzDrawPolygon(A,...,D)
\tkzDrawPoints(A,...,D)
\end{tikzpicture}
6. Definition of a point: \texttt{\textbackslash tkzDefPoint} or \texttt{\textbackslash tkzDefPoints}

6.3. Definition of multiple points: \texttt{\textbackslash tkzDefPoints}

\begin{verbatim}
\texttt{\textbackslash tkzDefPoints[(local options)]\{(x_1/y_1/n_1,x_2/y_2/r_2, \ldots)\}}
\end{verbatim}

\textit{x_i} and \textit{y_i} are the coordinates of a referenced point \textit{r_i}

\begin{tabular}{ll}
arguments & default example \\
\hline
\textit{x_i/y_i/r_i} & \texttt{\textbackslash tkzDefPoints\{O/O,2/2/A\}} \\
\textbf{options} & \textbf{default} definition \\
\textbf{shift} & no default Adds (x,y) or (α:d) to all coordinates \\
\end{tabular}

6.4. Create a triangle

\begin{tikzpicture}[scale=.75]
\tkzDefPoints{0/0/A,4/0/B,4/3/C}
\tkzDrawPolygon(A,B,C)
\tkzDrawPoints(A,B,C)
\end{tikzpicture}

6.5. Create a square

Note here the syntax for drawing the polygon.

\begin{tikzpicture}[scale=1]
\tkzDefPoints{0/0/A,2/0/B,2/2/C,0/2/D}
\tkzDrawPolygon(A,B,...,D)
\tkzDrawPoints(A,...,D)
\end{tikzpicture}
Part III.

Calculating
Now that the fixed points are defined, we can with their references using macros from the package or macros that you will create get new points. The calculations may not be apparent but they are usually done by the package. You may need to use some mathematical constants, here is the list of constants defined by the package. You may need to use some mathematical constants, here is the list of constants defined by the package.

7. Auxiliary tools

7.1. Constants

*tkz-euclide* knows some constants, here is the list:

\begin{verbatim}
\def\tkzPhi{1.618034}
\def\tkzInvPhi{0.618034}
\def\tkzSqrtPhi{1.27202}
\def\tkzSqrTwo{1.414213}
\def\tkzSqrThree{1.7320508}
\def\tkzSqrFive{2.2360679}
\def\tkzSqrTwobyTwo{0.7071065}
\def\tkzPi{3.1415926}
\def\tkzEuler{2.71828182}
\end{verbatim}

7.2. New point by calculation

When a macro of *tkznameofpack* creates a new point, it is stored internally with the reference \texttt{tkzPointResult}. You can assign your own reference to it. This is done with the macro \texttt{tkzGetPoint}. A new reference is created, your choice of reference must be placed between braces.

\begin{verbatim}
\tkzGetPoint{(ref)}
\end{verbatim}

If the result is in \texttt{tkzPointResult}, you can access it with \texttt{tkzGetPoint}.

<table>
<thead>
<tr>
<th>arguments</th>
<th>default</th>
<th>example</th>
</tr>
</thead>
<tbody>
<tr>
<td>ref</td>
<td>no</td>
<td>\texttt{tkzGetPoint{M}} see the next example</td>
</tr>
</tbody>
</table>

Sometimes you need to get two points. It's possible with

\begin{verbatim}
\tkzGetPoints{(ref1)}{(ref2)}
\end{verbatim}

The result is in \texttt{tkzPointFirstResult} and \texttt{tkzPointSecondResult}.

<table>
<thead>
<tr>
<th>arguments</th>
<th>default</th>
<th>example</th>
</tr>
</thead>
<tbody>
<tr>
<td>{ref1,ref2}</td>
<td>no</td>
<td>\texttt{tkzGetPoints{M,N}} It's the case with \texttt{tkzInterCC}</td>
</tr>
</tbody>
</table>

If you need only the first or the second point you can also use:

\begin{verbatim}
\tkzGetFirstPoint{(ref1)}
\end{verbatim}

<table>
<thead>
<tr>
<th>arguments</th>
<th>default</th>
<th>example</th>
</tr>
</thead>
<tbody>
<tr>
<td>ref1</td>
<td>no</td>
<td>\texttt{tkzGetFirstPoint{M}}</td>
</tr>
</tbody>
</table>
8. Special points

Here are some special points.

8.1. Middle of a segment \texttt{tkzDefMidPoint}

It is a question of determining the middle of a segment.

\begin{tikzpicture}[scale=1]
\tkzDefPoint(2,3){A}
\tkzDefPoint(6,2){B}
\tkzDefMidPoint(A,B)
\tkzGetPoint{M}
\tkzDrawSegment(A,B)
\tkzDrawPoints(A,B,M)
\tkzLabelPoints[below](A,B,M)
\end{tikzpicture}

8.2. Golden ratio

From Wikipedia: In mathematics, two quantities are in the golden ratio if their ratio is the same as the ratio of their sum to the larger of the two quantities. Expressed algebraically, for quantities \(a, b\) such as \(a > b > 0\); \(a + b\) is to \(a\) as \(a\) is to \(b\).
8. Special points

\[ a + b = \frac{\phi}{\phi} = \frac{1 + \sqrt{5}}{2} \]

One of the two solutions to the equation \( x^2 - x - 1 = 0 \) is the golden ratio \( \phi = \frac{1 + \sqrt{5}}{2} \).

8.2.1. Use the golden ratio to divide a line segment

\begin{tikzpicture}
\tkzDefPoints{0/0/A,6/0/C}
\tkzDefMidPoint(A,C) \tkzGetPoint{I}
\tkzDefGoldenRatio(A,C) \tkzGetPoint{B}
\tkzDrawSegments(A,C)
\tkzDrawPoints(A,B,C)
\tkzLabelPoints(A,B,C)
\end{tikzpicture}

It is also possible to use the following macro.

8.3. Barycentric coordinates

Let \( pt_1, pt_2, \ldots, pt_n \) be \( n \) points, they define \( n \) vectors \( \vec{v}_1, \vec{v}_2, \ldots, \vec{v}_n \) with the origin of the referential as the common endpoint. \( \alpha_1, \alpha_2, \ldots, \alpha_n \) are \( n \) numbers, the vector obtained by:

\[
\frac{\alpha_1 \vec{v}_1 + \alpha_2 \vec{v}_2 + \cdots + \alpha_n \vec{v}_n}{\alpha_1 + \alpha_2 + \cdots + \alpha_n}
\]

defines a single point.

8.3.1. Using \( \texttt{tkzDefBarycentricPoint} \) with two points

In the following example, we obtain the barycenter of points A and B with coefficients 1 and 2, in other words:

\[
\overrightarrow{AI} = \frac{2}{3} \overrightarrow{AB}
\]
8. Special points

8.3.2. Using \tkzDefBarycentricPoint with three points

This time M is simply the center of gravity of the triangle. For reasons of simplification and homogeneity, there is also \tkzCentroid.

\begin{tikzpicture}[scale=.8]
\tkzDefPoints{2/1/A,5/3/B,0/6/C}
\tkzDefBarycentricPoint(A=1,B=1,C=1)
\tkzGetPoint{G}
\tkzDefMidPoint(A,B) \tkzGetPoint{C'}
\tkzDefMidPoint(A,C) \tkzGetPoint{B'}
\tkzDefMidPoint(C,B) \tkzGetPoint{A'}
\tkzDrawPolygon(A,B,C)
\tkzDrawLines[add=0 and 1,new](A,G B,G C,G)
\tkzLabelPoint(G){$G$}
\tkzDrawPoints[affect](A',B',C',G)
\tkzDrawPoints(A,B,C)
\tkzAutoLabelPoints[center=G](A,B,C)
\tkzAutoLabelPoints[center=G,above right](A',B',C')
\end{tikzpicture}

8.4. Internal and external Similitude Center

The centers of the two homotheties in which two circles correspond are called external and internal centers of similitude. You can use \tkzDefIntSimilitudeCenter and \tkzDefExtSimilitudeCenter but the next macro is better.

\begin{verbatim}
\tkzDefSimilitudeCenter[\var]{⟨O,A⟩}{⟨O',B⟩} or ⟨O,r⟩{⟨O',r'⟩}
\end{verbatim}

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>⟨pt1,pt2⟩⟨pt3,pt4⟩</td>
<td>⟨O,A⟩⟨O',B⟩</td>
<td>r = OA,r' = O'B</td>
</tr>
<tr>
<td>⟨pt1,r1⟩⟨pt2,r2⟩</td>
<td>⟨A,1⟩⟨B,2⟩</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>ext</td>
<td>ext</td>
<td>external center</td>
</tr>
<tr>
<td>int</td>
<td>ext</td>
<td>internal center</td>
</tr>
<tr>
<td>node</td>
<td>node</td>
<td>Circles are defined by two points: center and point on the circle</td>
</tr>
<tr>
<td>R</td>
<td>node</td>
<td>Circles are defined by the center and the radius</td>
</tr>
</tbody>
</table>

\tkz-euclide AlterMundus
8. Special points

8.4.1. Internal and external with node

\begin{tikzpicture}[scale=.75]
\tkzDefPoints{0/0/O,4/-5/A,3/0/B,5/-5/C}
\tkzDefSimilitudeCenter[ini](O,B)(A,C) \tkzGetPoint{I}
\tkzDefSimilitudeCenter[ext](O,B)(A,C) \tkzGetPoint{J}
\tkzDefTangent[from = I](O,B) \tkzGetPoints{D}{E}
\tkzDefTangent[from = I](A,C) \tkzGetPoints{D'}{E'}
\tkzDefTangent[from = J](O,B) \tkzGetPoints{F}{G}
\tkzDefTangent[from = J](A,C) \tkzGetPoints{F'}{G'}
\tkzDrawCircles(O,B A,C)
\tkzDrawSegments[add = .5 and .5,new](D,D' E,E')
\tkzDrawSegments[add= 0 and 0.25,new](J,F J,G)
\tkzDrawPoints(O,A,I,J,D,E,F,G,D',E',F',G')
\end{tikzpicture}

You can use \texttt{\tkzDefBarycentricPoint} to find a homothetic center
\begin{verbatim}
\tkzDefBarycentricPoint(O={-r},A=\R) \tkzGetPoint{J}
\end{verbatim}

8.4.2. Example with node

\begin{tikzpicture}[rotate=60,scale=.5]
\tkzDefPoints{0/0/A,5/0/C}
\tkzDefGoldenRatio(A,C) \tkzGetPoint{B}
\tkzDefSimilitudeCenter(A,B)(C,B) \tkzGetPoint{J}
\tkzDefTangent[from = J](A,B) \tkzGetPoints{F}{G}
\tkzDefTangent[from = J](C,B) \tkzGetPoints{F'}{G'}
\tkzDrawCircles(A,B C,B)
\tkzDrawSegments[add= 0 and 0.25,cyan](J,F J,G)
\tkzDrawPoints(A,J,F,G,F',G')
\end{tikzpicture}
8.5. Harmonic division

\begin{align*}
\text{\texttt{\textbackslash tkzDefHarmonic[[options]]((pt1,pt2,pt3)) or ((pt1,pt2))}}
\end{align*}

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>both</td>
<td>both</td>
<td>((A,B)) we look for C and D such that ((A;B;C,D) = -1)</td>
</tr>
<tr>
<td>ext</td>
<td>both</td>
<td>((A,B,C)) we look for D such that ((A,B;C,D) = -1)</td>
</tr>
<tr>
<td>int</td>
<td>both</td>
<td>((A,B,D)) we look for C such that ((A,B,C,D) = -1)</td>
</tr>
</tbody>
</table>

8.5.1. options ext and int

\begin{tikzpicture}
\tkzDefPoints{0/0/A,6/0/B,4/0/C}
\tkzDefHarmonic[ext](A,B,C) \tkzGetPoint{J}
\tkzDefHarmonic[int](A,B,J) \tkzGetPoint{I}
\tkzDrawPoints(A,B,I,J)
\tkzDrawLine[add=.5 and 1](A,B)
\tkzLabelPoints(A,B,I,J)
\end{tikzpicture}

8.5.2. option both

\begin{tikzpicture}
\tkzDefPoints{0/0/A,6/0/B}
\tkzDefHarmonic(A,B,{1/2}) \tkzGetPoints{I}{J}
\tkzDrawPoints(A,B,I,J)
\tkzDrawLine[add=1 and .5](A,B)
\tkzLabelPoints(A,B,I,J)
\end{tikzpicture}

8.6. Equidistant points

8.6.1. \texttt{\textbackslash tkzDefEquiPoints}

\begin{align*}
\text{\texttt{\textbackslash tkzDefEquiPoints[[local options]]((pt1,pt2))}}
\end{align*}

<table>
<thead>
<tr>
<th>arguments</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>(pt1,pt2)</td>
<td>no default</td>
<td>unordered list of two items</td>
</tr>
<tr>
<td>options</td>
<td>default</td>
<td>definition</td>
</tr>
<tr>
<td>dist</td>
<td>2 (cm)</td>
<td>half the distance between the two points</td>
</tr>
<tr>
<td>from=pt</td>
<td>no default</td>
<td>reference point</td>
</tr>
<tr>
<td>show</td>
<td>false</td>
<td>if true displays compass traces</td>
</tr>
<tr>
<td>/compass/delta</td>
<td>0</td>
<td>compass trace size</td>
</tr>
</tbody>
</table>

This macro makes it possible to obtain two points on a straight line equidistant from a given point.
9. Point on line or circle

8.6.2. Using `\tkzDefEquiPoints` with options

\begin{tikzpicture}
\tkzSetUpCompass[color=purple,line width=1pt]
\tkzDefPoints{0/1/A,5/2/B,3/4/C}
\tkzDefEquiPoints[from=C,dist=1,show, /tkzcompass/delta=20](A,B)
\tkzGetPoints{E}{H}
\tkzDrawLines[color=blue](C,E C,H A,B)
\tkzDrawPoints[color=blue](A,B,C)
\tkzDrawPoints[color=red](E,H)
\tkzLabelPoints(E,H)
\tkzLabelPoints[color=blue](A,B,C)
\end{tikzpicture}

9. Point on line or circle

9.1. Point on a line

\begin{tikzpicture}
\tkzDefPoints{0/0/A,3/0/B}
\tkzDefPointOnLine[pos=1.2](A,B)\tkzGetPoint{P}
\tkzDefPointOnLine[pos=-0.2](A,B)\tkzGetPoint{R}
\tkzDefPointOnLine[pos=0.5](A,B) \tkzGetPoint{S}
\tkzDrawLine[new](A,B)
\tkzDrawPoints(A,B,P)
\tkzLabelPoints(A,B)
\tkzLabelPoint[above](P){pos=$1.2$}
\tkzLabelPoint[above](R){pos=$-0.2$}
\tkzLabelPoint[above](S){pos=$0.5$}
\tkzDrawPoints(A,B,P,R,S)
\tkzLabelPoints(A,B)
\end{tikzpicture}

9.2. Point on a circle

\begin{tikzpicture}
\tkzDefPoints{0/0/A,3/0/B}
\tkzDefPointOnCircle[through through = angle 30 center K1 point B](A,B)
\tkzGetPoint{P}
\tkzDrawPoints(A,B,P)
\tkzLabelPoints(A,B)
\tkzLabelPoints(A,B)
\end{tikzpicture}
9.2.1. Altshiller's Theorem

The two lines joining the points of intersection of two orthogonal circles to a point on one of the circles met the other circle in two diametrally opposite points. Altshiller p 176

\begin{tikzpicture}[scale=.4]
  \tkzDefPoints{0/0/P,5/0/Q,3/2/I}
  \tkzDefCircleBy[orthogonal from=P](Q,I)
  \tkzGetFirstPoint{E}
  \tkzDefCircles(P,E Q,E)
  \tkzInterCC[common=E](P,E)(Q,E) \tkzGetFirstPoint{F}
  \tkzDefPointOnCircle[through = angle 80 center P point E](A)
  \tkzInterLC[common=E](A,E)(Q,E) \tkzGetFirstPoint{C}
  \tkzInterLL(A,F)(C,Q) \tkzGetPoint{D}
  \tkzDrawLines:add=0 and .75(P,Q)
  \tkzDrawLines:add=0 and 2(A,E)
  \tkzDrawSegments(P,E F,E C A,F C,D)
  \tkzDrawPoints(P,Q,E,F,A,C,D)
  \tkzLabelPoints(P,Q,A,F,C,D)
  \end{tikzpicture}

9.2.2. Use of \texttt{tkzDefPointOnCircle}

\begin{tikzpicture}
  \tkzDefPoints{0/0/A,4/0/B,0.8/3/C}
  \tkzDefPointOnCircle[R = angle 90 center B radius 1](I)
  \tkzDefCircle[circum](A,B,C)
  \tkzGetPoint(G) \tkzGetLength[rG]
  \tkzDefPointOnCircle[R = angle 30 center G radius \rG](J)
  \tkzDrawCircle[R,teal](B,1)
  \tkzDrawCircle(G,J)
  \tkzDrawPoints(A,B,C,G,I,J)
  \tkzAutoLabelPoints[center=G](A,B,C,J)
  \tkzLabelPoints[below](G,I)
\end{tikzpicture}
10. Special points relating to a triangle

10.1. Triangle center: \texttt{\tkzDefTriangleCenter} 

\begin{verbatim}
\tkzDefTriangleCenter[(local options)]((A,B,C))
\end{verbatim}

This macro allows you to define the center of a triangle. Be careful, the arguments are lists of three points. This macro is used in conjunction with \texttt{\tkzGetPoint} to get the center you are looking for.

You can use \texttt{\tkzPointResult} if it is not necessary to keep the results.

<table>
<thead>
<tr>
<th>arguments</th>
<th>default</th>
<th>example</th>
</tr>
</thead>
<tbody>
<tr>
<td>(pt1,pt2,pt3)</td>
<td>no</td>
<td>\tkzDefTriangleCenter<a href="B,C,A">ortho</a></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>ortho</td>
<td>circum</td>
<td>intersection of the altitudes</td>
</tr>
<tr>
<td>orthic</td>
<td>circum</td>
<td>...</td>
</tr>
<tr>
<td>centroid</td>
<td>circum</td>
<td>intersection of the medians</td>
</tr>
<tr>
<td>median</td>
<td>circum</td>
<td>...</td>
</tr>
<tr>
<td>circum</td>
<td>circum</td>
<td>circle center circumscribed</td>
</tr>
<tr>
<td>in</td>
<td>circum</td>
<td>center of the circle inscribed in a triangle</td>
</tr>
<tr>
<td>ex</td>
<td>circum</td>
<td>center of a circle exscribed to a triangle</td>
</tr>
<tr>
<td>euler</td>
<td>circum</td>
<td>center of Euler’s circle</td>
</tr>
<tr>
<td>gergonne</td>
<td>circum</td>
<td>defined with the Contact triangle</td>
</tr>
<tr>
<td>symmedian</td>
<td>circum</td>
<td>Lemoine's point or symmedian center or Grebe's point</td>
</tr>
<tr>
<td>lemoine</td>
<td>circum</td>
<td>...</td>
</tr>
<tr>
<td>grebe</td>
<td>circum</td>
<td>...</td>
</tr>
<tr>
<td>spieker</td>
<td>circum</td>
<td>Spiker circle center</td>
</tr>
<tr>
<td>nagel</td>
<td>circum</td>
<td>Nagel Center</td>
</tr>
<tr>
<td>mittenpunkt</td>
<td>circum</td>
<td>Or middlepoint</td>
</tr>
<tr>
<td>feuerbach</td>
<td>circum</td>
<td>Feuerbach Point</td>
</tr>
</tbody>
</table>

10.1.1. Option ortho or orthic

The intersection $H$ of the three altitudes of a triangle is called the orthocenter.

\begin{verbatim}
\begin{tikzpicture}
\tkzDefPoint(0,0){A}
\tkzDefPoint(5,1){B}
\tkzDefPoint(1,4){C}
\tkzDefTriangleCenter[ortho](B,C,A)
\tkzGetPoint{H}
\tkzDefSpcTriangle[orthic,name=H](A,B,C){a,b,c}
\tkzDrawPolygon(A,B,C)
\tkzDrawSegments[new](A,Ha B,Hb C,Hc,A)
\tkzDrawPoints(A,B,C,H)
\tkzLabelPoint(H){$H$}
\tkzAutoLabelPoints[center=H](A,B,C)
\tkzMarkRightAngles(A,Ha,B B,Hb,C C,Hc,A)
\end{tikzpicture}
\end{verbatim}
10. Special points relating to a triangle

10.1.2. Option centroid

\begin{tikzpicture}[scale=.75]
\tkzDefPoints{0/0/A,5/0/B,1/4/C}
\tkzDefTriangleCenter[centroid](A,B,C)
\tkzGetPoint{G}
\tkzDrawPolygon(A,B,C)
\tkzDrawLines[add = 0 and 2/3,new](A,G B,G C,G)
\tkzDrawPoints(A,B,C,G)
\tkzLabelPoint(G){$G$}
\end{tikzpicture}

10.1.3. Option circum

\begin{tikzpicture}
\tkzDefPoints{0/1/A,3/2/B,1/4/C}
\tkzDefTriangleCenter[circum](A,B,C)
\tkzGetPoint{O}
\tkzDrawPolygon(A,B,C)
\tkzDrawCircle(O,A)
\tkzDrawPoints(A,B,C,O)
\tkzLabelPoint(O){$O$}
\end{tikzpicture}

10.1.4. Option in

In geometry, the incircle or inscribed circle of a triangle is the largest circle contained in the triangle; it touches (is tangent to) the three sides. The center of the incircle is a triangle center called the triangle’s incenter. The center of the incircle, called the incenter, can be found as the intersection of the three internal angle bisectors. The center of an excircle is the intersection of the internal bisector of one angle (at vertex $A$, for example) and the external bisectors of the other two. The center of this excircle is called the excenter relative to the vertex $A$, or the excenter of $A$. Because the internal bisector of an angle is perpendicular to its external bisector, it follows that the center of the incircle together with the three excircle centers form an orthocentric system.

(Article on Wikipedia)

We get the center of the inscribed circle of the triangle. The result is of course in \texttt{tkzPointResult}. We can retrieve it with \texttt{tkzGetPoint}.

\begin{tikzpicture}
\tkzDefPoints{0/0/A,6/0/B,0.8/4/C}
\tkzDefTriangleCenter[in](A,B,C)
\tkzGetPoint{I}
\tkzDrawLines(A,B B,C C,A)
\tkzDrawCircle[in](A,B,C)
\tkzDrawPoint[red](I)
\tkzDrawPoints(A,B,C)
\tkzLabelPoint(I){$I$}
\end{tikzpicture}

10.1.5. Option ex

An excircle or escribed circle of the triangle is a circle lying outside the triangle, tangent to one of its sides and tangent to the extensions of the other two. Every triangle has three distinct excircles, each tangent to one of the
10. Special points relating to a triangle

We get the center of an inscribed circle of the triangle. The result is of course in \texttt{tkzPointResult}. We can retrieve it with \texttt{tkzGetPoint}.

\begin{tikzpicture}[scale=.5]
\tkzDefPoints{0/1/A,3/2/B,1/4/C}
\tkzDefTriangleCenter[ex](B,C,A)
\tkzGetPoint{J_c}
\tkzDefPointBy[projection=onto A--B](J_c)
\tkzGetPoint{Tc}
\tkzDrawPolygon(A,B,C)
\tkzDrawCircle[new](J_c,Tc)
\tkzDrawLines[add=1.5 and 0](A,C B,C)
\tkzDrawPoints(A,B,C,J_c)
\tkzLabelPoints(J_c)
\end{tikzpicture}

10.1.6. Option euler

This macro allows to obtain the center of the circle of the nine points or euler's circle or Feuerbach's circle. The nine-point circle, also called Euler's circle or the Feuerbach circle, is the circle that passes through the perpendicular feet $H_A, H_B,$ and $H_C$ dropped from the vertices of any reference triangle $ABC$ on the sides opposite them. Euler showed in 1765 that it also passes through the midpoints $M_A, M_B, M_C$ of the sides of $ABC$. By Feuerbach's theorem, the nine-point circle also passes through the midpoints $E_A, E_B,$ and $E_C$ of the segments that join the vertices and the orthocenter $H$. These points are commonly referred to as the Euler points.

(https://mathworld.wolfram.com/Nine-PointCircle.html)

\begin{tikzpicture}[scale=1,rotate=90]
\tkzDefPoints{0/0/A,6/0/B,0.8/4/C}
\tkzDefSpcTriangle[medial,name=M](A,B,C){_A,_B,_C}
\tkzDefTriangleCenter[euler](A,B,C) \tkzGetPoint{N}
\tkzDefMidPoint(A,H) \tkzGetPoint{E_A}
\tkzDefMidPoint(C,H) \tkzGetPoint{E_C}
\tkzDefMidPoint(B,H) \tkzGetPoint{E_B}
\tkzDefSpcTriangle[ortho,name=H](A,B,C){_A,_B,_C}
\tkzDrawPolygon(A,B,C)
\tkzDrawCircle[new](N,E_A)
\tkzDrawSegments[new](A,H_A B,H_B C,H_C)
\tkzDrawPoints(A,B,C,N,H)
\tkzDrawPoints[new](M_A,M_B, M_C)
\tkzDrawPoints(H_A,H_B,H_C)
\tkzDrawPoints[green](E_A,E_B,E_C)
\tkzAutoLabelPoints[center=N, font=\scriptsize\scriptsize]{A,B,C,M_A,M_B,M_C,H_A,H_B,H_C,E_A,E_B,E_C}
\tkzLabelPoints[font=\scriptsize]{H,N}
\tkzMarkSegments[mark=s, size=3pt, color=blue, line width=1pt]{B,E_B E_B,H}
\end{tikzpicture}

10.1.7. Option symmedian

The point of concurrence $K$ of the symmedians, sometimes also called the Lemoine point (in England and France) or the Grebe point (in Germany).


\begin{tikzpicture}[scale=1,rotate=90]
\tkzDefPoints{0/0/A,6/0/B,0.8/4/C}
\tkzDefSpcTriangle[medial,name=M](A,B,C){_A,_B,_C}
\tkzDefTriangleCenter[euler](A,B,C) \tkzGetPoint{N}
\tkzDefMidPoint(A,H) \tkzGetPoint{E_A}
\tkzDefMidPoint(C,H) \tkzGetPoint{E_C}
\tkzDefMidPoint(B,H) \tkzGetPoint{E_B}
\tkzDefSpcTriangle[ortho,name=H](A,B,C){_A,_B,_C}
\tkzDrawPolygon(A,B,C)
\tkzDrawCircle[new](N,E_A)
\tkzDrawSegments[new](A,H_A B,H_B C,H_C)
\tkzDrawPoints(A,B,C,N,H)
\tkzDrawPoints[new](M_A,M_B, M_C)
\tkzDrawPoints(H_A,H_B,H_C)
\tkzDrawPoints[green](E_A,E_B,E_C)
\tkzAutoLabelPoints[center=N, font=\scriptsize\scriptsize]{A,B,C,M_A,M_B,M_C,H_A,H_B,H_C,E_A,E_B,E_C}
\tkzLabelPoints[font=\scriptsize]{H,N}
\tkzMarkSegments[mark=s, size=3pt, color=blue, line width=1pt]{B,E_B E_B,H}
\end{tikzpicture}
10. Special points relating to a triangle

10.1.8. Option spieker

The Spieker center is the center $Sp$ of the Spieker circle, i.e., the incenter of the medial triangle of a reference triangle.


```
\begin{tikzpicture}
\tkzDefPoint(0,0){A} \tkzDefPoint(5,0){B} \tkzDefPoint(1,4){C}
\tkzDefTriangleCenter[spm](A,B,C) \tkzGetPoint{K}
\tkzDefTriangleCenter[med](A,B,C) \tkzGetPoint{G}
\tkzDefTriangleCenter[in](A,B,C) \tkzGetPoint{I}
\tkzDefSpcTriangle[cent](A,B,C){a,b,c}
\tkzDefSpcTriangle[incent](A,B,C){a,b,c}
\tkzDrawPolygon(A,B,C)
\tkzDrawLines[add = 0 and 2/3,new](A,K B,K C,K)
\tkzDrawSegments[color=cyan](A,Ma B,Mb C,Mc)
\tkzDrawSegments[color=green](A,Ia B,Ib C,Ic)
\tkzDrawLine[add=2 and 2](G,I)
\tkzDrawPoints(A,B,C,K,G,I)
\tkzLabelPoints[font=\scriptsize](A,B,K,G,I)
\tkzLabelPoints[above,font=\scriptsize](C)
\end{tikzpicture}
```

10.1.9. Option gergonne

The Gergonne Point is the point of concurrency which results from connecting the vertices of a triangle to the opposite points of tangency of the triangle's incircle. (Joseph Gergonne French mathematician)

```
\begin{tikzpicture}
\tkzDefPoints{0/0/A,6/0/B,5/5/C} \tkzDefSpcTriangle[medial](A,B,C){Ma,Mb,Mc}
\tkzDefTriangleCenter[centroid](A,B,C) \tkzGetPoint{G}
\tkzDefTriangleCenter[spieker](A,B,C) \tkzGetPoint{Sp}
\tkzDrawPolygon[](A,B,C)
\tkzDrawPoints(A,B,C)
\tkzDrawCircle[in](Ma,Mb,Mc)
\tkzDrawPoints(B,C,A,Sp,Ma,Mb,Mc)
\tkzAutoLabelPoints[center=G,dist=.3](Ma,Mb,Mc)
\tkzAutoLabelPoints[right](Sp)
\tkzAutoLabelPoints[center=G](A,B,C)
\end{tikzpicture}
```

tkz-euclide  AlterMundus
10. Special points relating to a triangle

10.1.10. Option nagel

Let $T_a$ be the point at which the excircle with center $J_a$ meets the side $BC$ of a triangle $ABC$, and define $T_b$ and $T_c$ similarly. Then the lines $AT_a$, $BT_b$, and $CT_c$ concur in the Nagel point $N_a$.


10.1.11. Option mittenpunkt

The mittenpunkt (also called the middlespoint) of a triangle $ABC$ is the symmedian point of the excentral triangle, i.e., the point of concurrence $M$ of the lines from the excenters through the corresponding triangle side midpoints.

10. Special points relating to a triangle

10.1.12. Relation between gergonne, centroid and mittenpunkt

The Gergonne point $Ge$, triangle centroid $G$, and mittenpunkt $M$ are collinear, with $GeG/GM=2$. 

\begin{tikzpicture}
\tkzDefPoints{0/0/A,6/0/B,4/6/C}
\tkzDefSpcTriangle[centroid](A,B,C){Ma,Mb,Mc}
\tkzDefSpcTriangle[ex](A,B,C){Ja,Jb,Jc}
\tkzDefSpcTriangle[extouch](A,B,C){Ta,Tb,Tc}
\tkzDefTriangleCenter[mittenpunkt](A,B,C)
\tkzGetPoint{Mi}
\tkzDrawPoints[draw,new](Ma,Mb,Mc,Ja,Jb,Jc)
\tkzClipBB
\tkzDrawPolygon[blue](A,B,C)
\tkzDrawLines[add=0 and 1](Ja,Ma
Jb,Mb Jc,Mc)
\tkzDrawLines[add=1 and 1](A,B A,C B,C)
\tkzDrawCircles[draw,new](Ja,Ta Jb,Tb Jc,Tc)
\tkzDrawPoints(Ma,Mc,Ja,Jc)
\tkzLabelPoints(Ma,Mc,Ja,Jb,Jc)
\end{tikzpicture}
These transformations are:

- translation;
- homothety;
- orthogonal reflection or symmetry;
- central symmetry;
- orthogonal projection;
- rotation (degrees or radians);
- inversion with respect to a circle.

The choice of transformations is made through the options. There are two macros, one for the transformation of a single point \texttt{\tkzDefPointBy} and the other for the transformation of a list of points \texttt{\tkzDefPointsBy}. By default the image of A is $A'$. For example, we’ll write:

\begin{verbatim}
\tkzDefPointBy[translation= from A to A'](B)
\end{verbatim}

The result is in \texttt{tkzPointResult}

\begin{verbatim}
\tkzDefPointBy[(local options)](pt)
\end{verbatim}

The argument is a simple existing point and its image is stored in \texttt{tkzPointResult}. If you want to keep this point then the macro \texttt{\tkzGetPoint{M}} allows you to assign the name \texttt{M} to the point.

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<td></td>
</tr>
<tr>
<td>inversion negative = center #1 through #2</td>
<td>...</td>
<td></td>
</tr>
</tbody>
</table>

The image is only defined and not drawn.
11. Definition of points by transformation: \tkzDefPointBy

11.1. Examples of transformations

11.1.1. translation

\begin{tikzpicture}[>=latex]
\tkzDefPoints{0/0/A,3/1/B,3/0/C}
\tkzDefPointBy[translation= from B to A](C)
\tkzGetPoint{D}
\tkzDrawPoints[teal](A,B,C,D)
\tkzLabelPoints[teal](A,B,C,D)
\tkzDrawSegments[orange,->](A,B D,C)
\end{tikzpicture}

11.1.2. reflection (orthogonal symmetry)

\begin{tikzpicture}[scale=.75]
\tkzDefPoints{-2/-2/A,-1/-1/C,-4/2/D,-4/0/O}
\tkzDrawCircle(O,A)
\tkzDefPointBy[reflection = over C--D](A)
\tkzGetPoint{A'}
\tkzDefPointBy[reflection = over C--D](O)
\tkzGetPoint{O'}
\tkzDrawCircle(O',A')
\tkzDrawLine[add= .5 and .5](C,D)
\tkzDrawPoints(C,D,O,O')
\end{tikzpicture}

11.1.3. homothety and projection

\begin{tikzpicture}
\tkzDefPoints{0/1/A,5/3/B,3/4/C}
\tkzDefLine[bisector](B,A,C) \tkzGetPoint{a}
\tkzDrawLine[add=0 and 0, color=magenta!50](A,a)
\tkzDefPointBy[homothety=center A ratio .5](a)
\tkzGetPoint{a'}
\tkzDefPointBy[projection = onto A--B](a')
\tkzGetPoint{k'}
\tkzDefPointBy[projection = onto A--B](a)
\tkzGetPoint{k}
\tkzDrawLines[add= .3 and .3](A,k A,C)
\tkzDrawSegments[blue](a',k' a,k)
\tkzDrawPoints(a,a',k,k',A)
\tkzDrawCircles(a',k' a,k)
\tkzLabelPoints(a,a',k,A)
\end{tikzpicture}
11.1.4. projection

\begin{tikzpicture}[scale=1.5]
\tkzDefPoints{0/0/A,0/4/B}
\tkzDefTriangle[pythagore](B,A) \tkzGetPoint{C}
\tkzDefLine[bisector](B,C,A) \tkzGetPoint{c}
\tkzInterLL(C,c)(A,B) \tkzGetPoint{D}
\tkzDefPointBy[projection=onto B--C](D)
\tkzGetPoint{G}
\tkzInterLC(C,D)(D,A) \tkzGetPoints{E}{F}
\tkzDrawPolygon(A,B,C)
\tkzDrawSegment(C,D)
\tkzDrawCircle(D,A)
\tkzDrawSegment[new](D,G)
\tkzMarkRightAngle[fill=orange!10,opacity=.4](D,G,B)
\tkzDrawPoints(A,C,F)
\tkzLabelPoints(A,C,F)
\tkzDrawPoints(B,D,E,G)
\tkzLabelPoints[above right](B,D,E)
\tkzLabelPoints[above](G)
\end{tikzpicture}

11.1.5. symmetry

\begin{tikzpicture}[scale=1]
\tkzDefPoints{2/-1/A,2/2/B,0/0/O}
\tkzDefPointsBy[symmetry=center O](B,A){}
\tkzDrawLine(A,A')
\tkzDrawLine(B,B')
\tkzMarkAngle[mark=s,arc=lll,
size=1.5,mkcolor=red](A,O,B)
\tkzLabelAngle[pos=2,circle,draw,
fill=blue!10,font=\scriptsize](A,O,B){$60^\circ$}
\tkzDrawPoints(A,B,O,A',B')
\tkzLabelPoints(B,B')
\tkzLabelPoints[below](A,0,A')
\end{tikzpicture}
11.1.6. rotation

\begin{tikzpicture}[scale=0.5]
\tkzDefPoints{0/0/A,5/0/B}
\tkzDrawSegment(A,B)
\tkzDefPointBy[rotation=center A angle 60](B)
\tkzGetPoint{C}
\tkzDefPointBy[symmetry=center C](A)
\tkzGetPoint{D}
\tkzDrawSegment(A,tkzPointResult)
\tkzDrawLine(B,D)
\tkzDrawArc(A,B)(C) \tkzDrawArc(B,C)(A)
\tkzDrawArc(C,D)(D)
\tkzMarkRightAngle(D,B,A)
\tkzDrawPoints(A,B)
\tkzLabelPoints(A,B)
\tkzLabelPoints[above](C)
\tkzLabelPoints[right](D)
\end{tikzpicture}

11.1.7. rotation in radian

\begin{tikzpicture}
\tkzDefPoint["$A$" left](1,5){A}
\tkzDefPoint["$B$" right](4,3){B}
\tkzDefPointBy[rotation in rad= center A angle pi/3](B)
\tkzGetPoint{C}
\tkzDrawSegment(A,B)
\tkzDrawPoints(A,B,C)
\tkzCompass(A,C)
\tkzCompass(B,C)
\tkzLabelPoints(C)
\end{tikzpicture}

11.1.8. rotation with nodes

\begin{tikzpicture}
\tkzDefPoint(0,0){O}
\tkzDefPoint(0:2){A}
\tkzDefPoint(40:2){B}
\tkzDefPoint(20:4){C}
\tkzDrawLine(O,A)
\tkzDefPointBy[rotation with nodes=center O from A to B](C)
\tkzGetPoint{D}
\tkzDrawPoints(A,B,C,D)
\tkzDrawCircle(O,A)
\tkzLabelPoints(A,C,D)
\tkzLabelPoints[above](B)
\end{tikzpicture}

11.1.9. inversion

Inversion is the process of transforming points to a corresponding set of points known as their inverse points. Two points $P$ and $P'$ are said to be inverses with respect to an inversion circle having inversion center $O$ and inversion radius $k$ if $P'$ is the perpendicular foot of the altitude of $OQP$, where $Q$ is a point on the circle such that...
11. Definition of points by transformation: \texttt{tkzDefPointBy}

OQ is perpendicular to PQ.
The quantity $k^2$ is known as the circle power (Coxeter 1969, p. 81). ([https://mathworld.wolfram.com/Inversion.html](https://mathworld.wolfram.com/Inversion.html))

Some propositions:

- The inverse of a circle (not through the center of inversion) is a circle.
- The inverse of a circle through the center of inversion is a line.
- The inverse of a line (not through the center of inversion) is a circle through the center of inversion.
- A circle orthogonal to the circle of inversion is its own inverse.
- A line through the center of inversion is its own inverse.
- Angles are preserved in inversion.

Explanation:

Directly (Center $O$ power=$k^2=OA^2=OP \times OP'$)

\begin{tikzpicture}[scale=.5]
\tkzDefPoints{4/0/A,6/0/P,0/0/O}
\tkzDefCircle(O,A)
\tkzDefPointBy[inversion = center O through A](P)
\tkzGetPoint{P'}
\tkzDrawSegments(O,P)
\tkzDrawCircle(O,A)
\tkzLabelPoints[above right,font=\scriptsize](O,A,P,P')
\tkzDrawPoints(O,A,P,P')
\end{tikzpicture}
11. Definition of points by transformation: \texttt{tkzDefPointBy}

11.1.10. Inversion of lines

\begin{tikzpicture} [scale=.5]
\tkzDefPoints{0/0/O,3/0/I,4/3/P,6/-3/Q}
\tkzDrawCircle(O,I)
\tkzDefPointBy[projection= onto P--Q](O) \tkzGetPoint{A}
\tkzDefPointBy[inversion = center O through I](A) \tkzGetPoint{A'}
\tkzDefPointBy[inversion = center O through I](P) \tkzGetPoint{P'}
\tkzDrawCircle[new,diameter](O,A') \tkzDrawPoints(A',P')
\tkzDrawCircle[new,diameter](O,A') \tkzDrawPoints(A',P')
\tkzDrawLines[add=.25 and .25,red](P,Q) \tkzDrawLines[add=.25 and .25](O,A)
\tkzDrawSegments(O,P) \tkzDrawPoints(A,P,O) \tkzDrawPoints(new)(A',P')
\end{tikzpicture}

\begin{tikzpicture} [scale=.5]
\tkzDefPoints{0/0/O,3/0/I,3/2/P,3/-2/Q}
\tkzDrawCircle(O,I)
\tkzDefPointBy[projection= onto P--Q](O) \tkzGetPoint{A}
\tkzDefPointBy[inversion = center O through I](A) \tkzGetPoint{A'}
\tkzDefPointBy[inversion = center O through I](P) \tkzGetPoint{P'}
\tkzDrawCircle[new,diameter](O,A') \tkzDrawPoints(A',P')
\tkzDrawLines[add=.25 and .25,red](P,Q) \tkzDrawLines[add=.25 and .25](O,A)
\tkzDrawSegments(O,P) \tkzDrawPoints(A,P,O) \tkzDrawPoints(new)(A',P')
\end{tikzpicture}

\begin{tikzpicture} [scale=.5]
\tkzDefPoints{0/0/O,3/0/I,2/1/P,2/-2/Q}
\tkzDrawCircle(O,I)
\tkzDefPointBy[projection= onto P--Q](O) \tkzGetPoint{A}
\tkzDefPointBy[inversion = center O through I](A) \tkzGetPoint{A'}
\tkzDefPointBy[inversion = center O through I](P) \tkzGetPoint{P'}
\tkzDrawCircle[new,diameter](O,A') \tkzDrawPoints(A',P')
\tkzDrawLines[add=.25 and .75,red](P,Q) \tkzDrawLines[add=.25 and .25](O,A')
\tkzDrawSegments(O,P') \tkzDrawPoints(A,P,O) \tkzDrawPoints(new)(A',P')
\end{tikzpicture}
11. Definition of points by transformation

11.1.11. Inversion of circle

\begin{tikzpicture}[scale=.5]
\tkzDefPoints{0/0/O,3/2/A,2/1/P}
\tkzDefTangent[from = O](A,P) \tkzGetPoints(T){X}
\tkzDefPointsBy[homothety=center O ratio 1.25](A,P,T)\tkzGetPoints(C){D}
\tkzCalcLength(A,P)
\tkzGetLength{rAP}
\tkzDefPointOnCircle[R= angle 190 center A radius \rAP](A,P)
\tkzDefPointsBy[inversion = center O through C](M)
\tkzDrawCircles(A,P A',P')
\tkzDrawCircle(O,C)
\tkzDrawLines[add=0 and .5](O,T' O,A' O,M' O,P')
\tkzLabelPoints(O,T,T')
\tkzLabelPoints[above left](M,M')
\tkzLabelPoints[below](P,P')
\end{tikzpicture}

11.1.12. Inversion of Triangle with respect to the Incircle

\begin{tikzpicture}[scale=1]
\tkzDefPoints{0/0/A,5/1/B,3/6/C}
\tkzDefTriangleCenter[in](A,B,C) \tkzGetPoint{O}
\tkzDefPointBy[projection= onto A--C](O) \tkzGetPoint{b}
\tkzDefPointBy[projection= onto A--C](O) \tkzGetPoint{b}
\tkzDefPointBy[projection= onto B--C](O) \tkzGetPoint{a}
\tkzDefPointBy[projection= onto A--B](O) \tkzGetPoint{c}
\tkzDefPointsBy[inversion = center O through b](a,b,c)\tkzGetPoints{Ia,Ib,Ic}
\tkzDefMidPoint(O,Ia) \tkzGetPoint{Ja}
\tkzDefMidPoint(O,Ib) \tkzGetPoint{Jb}
\tkzDefMidPoint(O,Ic) \tkzGetPoint{Jc}
\tkzInterCC(Ja,O)(Jb,O) \tkzGetPoints{O}{x}
\tkzInterCC(Ja,O)(Jc,O) \tkzGetPoints{y}{O}
\tkzInterCC(Jb,O)(Jc,O) \tkzGetPoints{z}{O}
\tkzDrawPolygon(A,B,C)
\tkzDrawCircle(O,b)\tkzDrawPoints(A,B,C,O)
\tkzDrawCircles[dashed,gray](Ja,y Jb,x Jc,z)
\tkzDrawArc[line width=1pt,orange](Ja,x)(z)
\tkzDrawArc[line width=1pt,orange](Jc,z)(y)
\tkzDrawArc[line width=1pt,orange](Ja,y)(x)
\tkzLabelPoint[below](A){\$A\$}\tkzLabelPoint[above](C){\$C\$}
\tkzLabelPoint[below](O){\$O\$}
\end{tikzpicture}

11.1.13. Inversion: orthogonal circle with inversion circle

The inversion circle itself, circles orthogonal to it, and lines through the inversion center are invariant under inversion. If the circle meets the reference circle, these invariant points of intersection are also on the inverse circle. See I and J in the next figure.
11. Definition of points by transformation:

\begin{tikzpicture}[scale=1]
\tkzDefPoint(0,0){O}\tkzDefPoint(1,0){A}
\tkzDefPoint(-1.5,-1.5){z1} \tkzDefPoint(1.5,-1.25){z2}
\tkzDefCircleBy[orthogonal through=z1 and z2](O,A)
\tkzGetPoint{c}
\tkzDrawCircle[new](c,z1)
\tkzDefPointBy[inversion = center O through A](z1)
\tkzGetPoint{Z1}
\tkzInterCC(O,A)(c,z1) \tkzGetPoints{I}{J}
\tkzDefPointBy[inversion = center O through A](I)
\tkzGetPoint{I'}
\tkzDrawCircle(O,A)
\tkzDrawPoints(O,A,z1,z2)
\tkzDrawPoints[new](c,Z1,I,J)
\end{tikzpicture}

11.1.14. Inversion and homothety

\begin{tikzpicture}[scale=.75]
\tkzDefPoints{0/0/O,3/2/A,2/1/P}
\tkzDefTangent[from = O](A,P) \tkzGetPoints{T}{X}
\tkzDefPointsBy[homothety = center O ratio 1.25](A,P,T){}
\tkzInterCC(A,P)(A',P') \tkzGetPoints{C}{D}
\tkzCalcLength(A,P) \tkzGetLength{rAP}
\tkzDefPointOnCircle[R= angle 190 center A radius \rAP]
\tkzDefPointBy[inversion = center O through C](M)
\tkzDrawCircles[new](A,P A',P')
\tkzDrawCircle(O,C)
\tkzDrawLines[add=0 and .5](O,T' O,A' O,M' O,P')
\tkzLabelPoints(O,T,T',M,M',P,P')
\end{tikzpicture}

For a more complex example see Pappus 45.25

11.1.15. Inversion negative

It's an inversion followed by a symmetry of center O
11. Definition of points by transformation : \texttt{\textbackslash{tkzDefPointBy}}

\begin{tikzpicture}[scale=1.5]
\tkzDefPoints{1/0/A,0/0/O}
\tkzDefPoint(-1.5,-1.5){z1}
\tkzDefPoint(0.35,-2){z2}
\tkzDefPointBy[inversion negative = center O through A](z1)
\tkzGetPoint{Z1}
\tkzDefPointBy[inversion negative = center O through A](z2)
\tkzGetPoint{Z2}
\tkzDrawCircle(O,A)
\tkzDrawPoints[color=black, fill=red,size=4](Z1,Z2)
\tkzDrawSegments(z1,Z1 z2,Z2)
\tkzDrawPoints[color=black, fill=red,size=4](O,z1,z2)
\tkzLabelPoints[font=\scriptsize](O,A,z1,z2,Z1,Z2)
\end{tikzpicture}
11. Definition of points by transformation: \texttt{tkzDefPointBy}

11.2. Transformation of multiple points; \texttt{tkzDefPointsBy}

Variant of the previous macro for defining multiple images. You must give the names of the images as arguments, or indicate that the names of the images are formed from the names of the antecedents, leaving the argument empty.

\texttt{tkzDefPointsBy[translation= from A to A'](B,C){}}

The images are B' and C'.

\texttt{tkzDefPointsBy[translation= from A to A'](B,C){D,E}}

The images are D and E.

\texttt{tkzDefPointsBy[translation= from A to A'](B){}}

The image is B'.

If the list of images is empty then the name of the image is the name of the antecedent to which “’” is added.

\begin{tabular}{|l|l|}
\hline
options & examples \\
\hline
\texttt{translation = from #1 to #2} & \texttt{[translation=from A to B](E){}} \\
\texttt{homothety = center #1 ratio #2} & \texttt{[homothety=center A ratio .5](E){F}} \\
\texttt{reflection = over #1--#2} & \texttt{[reflection=over A--B](E){F}} \\
\texttt{symmetry = center #1} & \texttt{[symmetry=center A](E){F}} \\
\texttt{projection = onto #1--#2} & \texttt{[projection=onto A--B](E){F}} \\
\texttt{rotation = center #1 angle #2} & \texttt{[rotation=center angle 30](E){F}} \\
\texttt{rotation in rad = center #1 angle #2} & \texttt{for instance angle pi/3} \\
\texttt{rotation with nodes = center #1 from #2 to #3} & \texttt{[center 0 from A to B](E){F}} \\
\texttt{inversion = center #1 through #2} & \texttt{[inversion = center 0 through A](E){F}} \\
\texttt{inversion negative = center #1 through #2} & \texttt{...} \\
\hline
\end{tabular}

The points are only defined and not drawn.

11.2.1. Example of translation

\begin{tikzpicture}
\tkzDefPoints{0/0/A,3/0/B,3/1/A',1/2/C}
\tkzDefPointsBy[translation= from A to A'](B,C){}
\tkzDrawPolygon(A,B,C)
\tkzDrawPoints(A,B,C)
\tkzLabelPoints(A,B,A',B',C,C')
\tkzDrawSegments[color = gray,->, style=dashed](A,A' B,B' C,C')
\end{tikzpicture}
11.2.2. Example of symmetry: an oval

\begin{tikzpicture}[scale=0.4]
  \tkzDefPoint(-4,0){I}
  \tkzDefPoint(4,0){J}
  \tkzDefPoint(0,0){O}
  \tkzInterCC(J,O)(O,J) \tkzGetPoints{L}{H}
  \tkzInterCC(I,O)(O,I) \tkzGetPoints{K}{G}
  \tkzInterLL(I,K)(J,H) \tkzGetPoint{M}
  \tkzInterLL(I,G)(J,L) \tkzGetPoint{N}
  \tkzDefPointsBy[symmetry=center J](L,H){D,E}
  \tkzDefPointsBy[symmetry=center I](G,K){C,F}
  \begin{scope}[line style/.style = {very thin,teal}]
    \tkzDrawLines[add=1.5 and 1.5](I,K I,G J,H J,L)
    \tkzDrawLines[add=.5 and .5](I,J)
    \tkzDrawCircles(O,I I,O J,O)
    \tkzDrawArc[delta=0,orange](N,D)(C)
    \tkzDrawArc[delta=0,orange](M,F)(E)
    \tkzDrawArc[delta=0,orange](J,E)(D)
    \tkzDrawArc[delta=0,orange](I,C)(F)
  \end{scope}
\end{tikzpicture}
12. Defining points using a vector

12.1. \texttt{tkzDefPointWith}

There are several possibilities to create points that meet certain vector conditions. This can be done with \texttt{tkzDefPointWith}. The general principle is as follows, two points are passed as arguments, i.e. a vector. The different options allow to obtain a new point forming with the first point (with some exceptions) a collinear vector or a vector orthogonal to the first vector. Then the length is either proportional to that of the first one, or proportional to the unit. Since this point is only used temporarily, it does not have to be named immediately. The result is in \texttt{tkzPointResult}. The macro \texttt{tkzGetPoint} allows you to retrieve the point and name it differently. There are options to define the distance between the given point and the obtained point. In the general case this distance is the distance between the 2 points given as arguments if the option is of the "normed" type then the distance between the given point and the obtained point is 1 cm. Then the \texttt{K} option allows to obtain multiples.

\begin{verbatim}
\texttt{tkzDefPointWith((pt1,pt2))}
\end{verbatim}

It is in fact the definition of a point meeting vectorial conditions.

<table>
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<tr>
<th>arguments</th>
<th>definition</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>(pt1,pt2)</td>
<td>point couple</td>
<td>the result is a point in \texttt{tkzPointResult}</td>
</tr>
</tbody>
</table>

In what follows, it is assumed that the point is recovered by \texttt{tkzGetPoint}\{C\}

<table>
<thead>
<tr>
<th>options</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>orthogonal</td>
<td>\texttt{[orthogonal]}(A,B)</td>
<td>(AC = AB ) and (\vec{AC} \perp \vec{AB})</td>
</tr>
<tr>
<td>orthogonal normed</td>
<td>\texttt{[orthogonal normed]}(A,B)</td>
<td>(AC = 1 ) and (\vec{AC} \perp \vec{AB})</td>
</tr>
<tr>
<td>linear</td>
<td>\texttt{[linear]}(A,B)</td>
<td>( \vec{AC} = K \times \vec{AB} )</td>
</tr>
<tr>
<td>linear normed</td>
<td>\texttt{[linear normed]}(A,B)</td>
<td>( AC = K ) and (\vec{AC} = k \times \vec{AB})</td>
</tr>
<tr>
<td>colinear= at #1</td>
<td>\texttt{[colinear= at C]}(A,B)</td>
<td>(\vec{CD} = \vec{AB})</td>
</tr>
<tr>
<td>colinear normed= at #1</td>
<td>\texttt{[colinear normed= at C]}(A,B)</td>
<td>(\vec{CD} = \vec{AB})</td>
</tr>
<tr>
<td>K</td>
<td>\texttt{[linear]}(A,B), (K=2)</td>
<td>(\vec{AC} = 2 \times \vec{AB})</td>
</tr>
</tbody>
</table>

12.1.1. Option \texttt{colinear at}, simple example

\begin{verbatim}
(\overrightarrow{AB} = \overrightarrow{CD})
\end{verbatim}

\begin{tikzpicture}[scale=1.2, vect/.style={->,shorten >=1pt,>=latex'}]
\tkzDefPoint(2,3){A} \tkzDefPoint(4,2){B}
\tkzDefPoint(0,1){C}
\tkzDefPointWith[\texttt{colinear=at C}](A,B)
\tkzGetPoint{D}
\tkzDrawPoints[new](A,B,C,D)
\tkzLabelPoints[above right=3pt](A,B,C,D)
\tkzDrawSegments[vect](A,B,C,D)
\end{tikzpicture}
12. Defining points using a vector

12.1.2. Option \texttt{colinear at}, complex example

\begin{tikzpicture}[scale=.75]
\tkzDefPoints{0/0/B,3.6/0/C,1.5/4/A}
\tkzDefSpcTriangle[ortho](A,B,C){Ha,Hb,Hc}
\tkzDefTriangleCenter[ortho](A,B,C) \tkzGetPoint{H}
\tkzDefSquare(A,C) \tkzGetPoints{R}{S}
\tkzDefSquare(B,A) \tkzGetPoints{M}{N}
\tkzDefSquare(C,B) \tkzGetPoints{P}{Q}
\tkzDefPointWith[colinear= at M](A,S) \tkzGetPoint{A'}
\tkzDefPointWith[colinear= at P](B,N) \tkzGetPoint{B'}
\tkzDefPointWith[colinear= at Q](C,R) \tkzGetPoint{C'}
\tkzDefPointBy[projection=onto P--Q](Ha) \tkzGetPoint{Pa}
\tkzDrawPolygon[teal,thick](A,C,R,S)\tkzDrawPolygon[teal,thick](A,B,N,M)
\tkzDrawPolygon[teal,thick](C,B,P,Q)
\tkzDrawPoints[teal,size=2](A,B,C,C',P,Q)
\tkzDrawSegments[ultra thin,teal,dashed](A,Ha,B,Hb,C,Hc)
\tkzDefPointBy[rotation=center A angle 90](S) \tkzGetPoint{S'}
\tkzDrawSegments[ultra thin,teal,dashed](S,S',A,A',A',M,S',B',Q,P,C',M,S,Ha,Pa)
\tkzDrawArc(A,S)(S')
\end{tikzpicture}

12.1.3. Option \texttt{colinear at}

How to use K
12. Defining points using a vector

\begin{tikzpicture}[vect/.style={->, shorten >=1pt, >=latex'}]
\tkzDefPoints{0/0/A,5/0/B,1/2/C}
\tkzDefPointWith[colinear=at C](A,B)
\tkzGetPoint{G}
\tkzDefPointWith[colinear=at C, K=0.5](A,B)
\tkzGetPoint{H}
\tkzLabelPoints(A,B,C,G,H)
\tkzDrawPoints(A,B,C,G,H)
\tkzDrawSegments[vect](A,B C,H)
\end{tikzpicture}

12.1.4. Option colinear at

With $K = \frac{\sqrt{2}}{2}$

\begin{tikzpicture}[vect/.style={->, shorten >=1pt, >=latex'}]
\tkzDefPoints{1/1/A,4/2/B,2/2/C}
\tkzDefPointWith[colinear=at C,K=sqrt(2)/2](A,B)
\tkzGetPoint{D}
\tkzDrawPoints[color=red](A,B,C,D)
\tkzDrawSegments[vect](A,B C,D)
\end{tikzpicture}

12.1.5. Option orthogonal

AB=AC since $K = 1$.

\begin{tikzpicture}[scale=1.2, vect/.style={->, shorten >=1pt, >=latex'}]
\tkzDefPoints{2/3/A,4/2/B}
\tkzDefPointWith[orthogonal,K=1](A,B)
\tkzGetPoint{C}
\tkzDrawPoints[color=red](A,B,C)
\tkzLabelPoints[right=3pt](B,C)
\tkzLabelPoints[below=3pt](A)
\tkzDrawSegments[vect](A,B A,C)
\tkzMarkRightAngle(B,A,C)
\end{tikzpicture}

12.1.6. Option orthogonal

With $K = -1$ OK=OI since $|K| = 1$ then OI=OJ=OK.

\begin{tikzpicture}[scale=.75]
\tkzDefPoints{1/2/O,2/5/I}
\tkzDefPointWith[orthogonal](O,I)
\tkzGetPoint{J}
\tkzDefPointWith[orthogonal,K=-1](O,I)
\tkzGetPoint{K}
\tkzDrawSegment(O,I)
\tkzDrawSegments[->](O,J O,K)
\tkzMarkRightAngles(I,O,J I,O,K)
\tkzDrawPoints(O,I,J,K)
\tkzLabelPoints(O,I,J,K)
\end{tikzpicture}
12.1.7. Option orthogonal more complicated example

\begin{tikzpicture}[scale=.75]
\tkzDefPoints{0/0/A,6/0/B}
\tkzDefMidPoint(A,B)
\tkzGetPoint{I}
\tkzDefPointWith[orthogonal,K=-.75](B,A)
\tkzGetPoint{C}
\tkzInterLC(B,C)(B,I)
\tkzGetPoints{D}{F}
\tkzDuplicateSegment(B,F)(A,F)
\tkzGetPoint{E}
\tkzDrawArc[delta=10](F,E)(B)
\tkzInterLC(A,B)(A,E)
\tkzGetPoints{N}{M}
\tkzDrawArc[delta=10](A,M)(E)
\tkzDrawLines(A,B B,C A,F)
\tkzCompass(B,F)
\tkzDrawPoints(A,B,C,F,M,E)
\tkzLabelPoints(A,B,C,F,M)
\tkzLabelPoints[above](E)
\end{tikzpicture}

12.1.8. Options colinear and orthogonal

\begin{tikzpicture}[scale=1.2,
vect/.style={->,shorten >=1pt,>=latex'}]
\tkzDefPoints{2/1/A,6/2/B}
\tkzDefPointWith[orthogonal,K=.5](A,B)
\tkzGetPoint{C}
\tkzDefPointWith[colinear=at C,K=.5](A,B)
\tkzGetPoint{D}
\tkzMarkRightAngle[fill=gray!20](B,A,C)
\tkzDrawSegments[vect](A,B A,C C,D)
\tkzDrawPoints(A,...,D)
\end{tikzpicture}

12.1.9. Option orthogonal normed

K = 1 AC = 1.

\begin{tikzpicture}[scale=1.2,
vect/.style={->,shorten >=1pt,>=latex'}]
\tkzDefPoints{2/3/A,4/2/B}
\tkzDefPointWith[orthogonal normed](A,B)
\tkzGetPoint{C}
\tkzDrawPoints[fill=red](A,B,C)
\tkzDrawSegments[vect](A,B A,C)
\tkzMarkRightAngle[fill=gray!20](B,A,C)
\end{tikzpicture}

12.1.10. Option orthogonal normed and K=2

K = 2 therefore AC = 2.
12. Defining points using a vector

12.1.11. Option linear

Here $K = 0.5$.
This amounts to applying a homothety or a multiplication of a vector by a real. Here is the middle of $[AB]$.

12.1.12. Option linear normed

In the following example $AC = 1$ and $C$ belongs to $(AB)$.

12.2. \texttt{tkzGetVectxy}

Retrieving the coordinates of a vector.

\begin{verbatim}
\texttt{tkzGetVectxy(A,B)}{(text)}
\end{verbatim}

Allows to obtain the coordinates of a vector.

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>\texttt{\langle point\rangle{name of macro}}</td>
<td>\texttt{tkzGetVectxy(A,B)}{V}</td>
<td>$V_x, V_y$: coordinates of $\overrightarrow{AB}$</td>
</tr>
</tbody>
</table>
12.2.1. Coordinate transfer with \texttt{tkzGetVectxy}

\begin{tikzpicture}
\tkzDefPoints{0/0/O,1/1/A,4/2/B}
\tkzGetVectxy(A,B){v}
\tkzDefPoint(\vx,\vy){V}
\tkzDrawSegment[->,color=red](O,V)
\tkzDrawSegment[->,color=blue](A,B)
\tkzDrawPoints(A,B,O)
\tkzLabelPoints(A,B,O,V)
\end{tikzpicture}
13. Straight lines

It is of course essential to draw straight lines, but before this can be done, it is necessary to be able to define certain particular lines such as mediators, bisectors, parallels or even perpendiculars. The principle is to determine two points on the straight line.

13.1. Definition of straight lines

\tkzDefLine[(local options)]{(pt1,pt2)} or (pt1,pt2,pt3)

The argument is a list of two or three points. Depending on the case, the macro defines one or two points necessary to obtain the line sought. Either the macro \tkzGetPoint or the macro \tkzGetPoints must be used. I used the term “mediator” to designate the perpendicular bisector line at the middle of a line segment.

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>(pt1,pt2)</td>
<td>(A,B)</td>
<td><a href="A,B">mediator</a></td>
</tr>
<tr>
<td>(pt1,pt2,pt3)</td>
<td>(A,B,C)</td>
<td><a href="B,A,C">bisector</a></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>mediator</td>
<td></td>
<td>perpendicular bisector of a line segment</td>
</tr>
<tr>
<td>perpendicular=through...</td>
<td>mediator</td>
<td>perpendicular to a straight line passing through a point</td>
</tr>
<tr>
<td>orthogonal=through...</td>
<td>mediator</td>
<td>see above</td>
</tr>
<tr>
<td>parallel=through...</td>
<td>mediator</td>
<td>parallel to a straight line passing through a point</td>
</tr>
<tr>
<td>bisector</td>
<td>mediator</td>
<td>bisector of an angle defined by three points</td>
</tr>
<tr>
<td>bisector out</td>
<td></td>
<td>Exterior Angle Bisector</td>
</tr>
<tr>
<td>K</td>
<td>1</td>
<td>coefficient for the perpendicular line</td>
</tr>
<tr>
<td>normed</td>
<td>false</td>
<td>normalizes the created segment</td>
</tr>
</tbody>
</table>

13.1.1. Example with mediator

\begin{tikzpicture}[rotate=25]
\tkzDefPoints{-2/0/A,1/2/B}
\tkzDefLine[mediator](A,B) \tkzGetPoints{C}{D}
\tkzDefPointWith[linear,K=.75](C,D) \tkzGetPoint{D}
\tkzDefMidPoint(A,B) \tkzGetPoint{I}
\tkzFillPolygon[color=teal!20](A,C,B,D)
\tkzDrawSegments(A,B C,D)
\tkzMarkRightAngle(B,I,C)
\tkzDrawSegments(D,B D,A)
\tkzDrawSegments(C,B D,A)
\end{tikzpicture}
13. Straight lines

13.1.2. Example with bisector and normed

\begin{tikzpicture}[rotate=25,scale=.75]
\tkzDefPoints{0/0/C, 2/-3/A, 4/0/B}
\tkzDefLine[bisector,normed](B,A,C) \tkzGetPoint{a}
\tkzDrawLines[add= 0 and .5](A,B A,C)
\tkzShowLine[bisector,gap=4,size=2,color=red](B,A,C)
\tkzDrawLines[new,dashed,add= 0 and 3](A,a)
\end{tikzpicture}

13.1.3. Example with orthogonal and parallel

\begin{tikzpicture}
\tkzDefPoints{-1.5/-0.25/A,1/-0.75/B,-0.7/1/C}
\tkzDrawLine(A,B)
\tkzLabelLine[pos=1.25,below left](A,B){\((d_1)\)}
\tkzDrawPoints(A,B,C)
\tkzDefLine[orthogonal=through C](B,A) \tkzGetPoint{c}
\tkzDrawLine(C,c)
\tkzLabelLine[pos=1.25,left](C,c){\((\delta)\)}
\tkzInterLL(A,B)(C,c) \tkzGetPoint{I}
\tkzMarkRightAngle(C,I,B)
\tkzDefLine[parallel=through C](A,B) \tkzGetPoint{c'}
\tkzDrawLine(C,c')
\tkzLabelLine[pos=1.25,below left](C,c'){\((d_2)\)}
\tkzMarkRightAngle(I,C,c')
\end{tikzpicture}

13.1.4. An envelope

Based on a figure from O. Reboux with pst-eucl by D Rodriguez.

\begin{tikzpicture}
\end{tikzpicture}
13. Straight lines

\begin{tikzpicture}[scale=.75]
\tkzInit[xmin=-6,ymin=-4,xmax=6,ymax=6] % necessary
\tkzClip
\tkzDefPoint(0,0){O}
\tkzDefPoint(132:4){A}
\tkzDefPoint(5,0){B}
\foreach \ang in {5,10,...,360}{%
   \tkzDefPoint(\ang:5){M}
   \tkzDefLine[mediator](A,M)
   \tkzDrawLine[color=magenta,add= 3 and 3](tkzFirstPointResult,tkzSecondPointResult)}
\end{tikzpicture}

13.1.5. A parabola

Based on a figure from O. Reboux with pst-eucl by D Rodriguez. It is not necessary to name the two points that define the mediator.

\begin{tikzpicture}[scale=.75]
\tkzInit[xmin=-6,ymin=-4,xmax=6,ymax=6]
\tkzClip
\tkzDefPoint(0,0){O}
\tkzDefPoint(132:5){A}
\tkzDefPoint(4,0){B}
\foreach \ang in {5,10,...,360}{%
   \tkzDefPoint(\ang:4){M}
   \tkzDefLine[mediator](A,M)
   \tkzDrawLine[color=teal,add= 3 and 3](tkzFirstPointResult,tkzSecondPointResult)}
\end{tikzpicture}

13.2. Specific lines: Tangent to a circle

Two constructions are proposed. The first one is the construction of a tangent to a circle at a given point of this circle and the second one is the construction of a tangent to a circle passing through a given point outside a disc.

\begin{tikzpicture}[scale=.75]
\tkzDefTangent[⟨local options⟩](⟨pt1,pt2⟩) or (⟨pt1,dim⟩)
\end{tikzpicture}

The parameter in brackets is the center of the circle or the center of the circle and a point on the circle or the center and the radius. This macro replaces the old one: \tkzTangent.
13. Straight lines

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>(pt1,pt2 or (pt1,dim))</td>
<td>(A,B) or ((A,2cm))</td>
<td>[AB] is radius A is the center</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>at=pt</td>
<td>at</td>
<td>tangent to a point on the circle</td>
</tr>
<tr>
<td>from=pt</td>
<td>at</td>
<td>tangent to a circle passing through a point</td>
</tr>
<tr>
<td>from with R=pt</td>
<td>idem, but the circle is defined by center = radius</td>
<td></td>
</tr>
</tbody>
</table>

The tangent is not drawn. With option at, a point of the tangent is given by \texttt{tkzPointResult}. With option from you get two points of the circle with \texttt{tkzFirstPointResult} and \texttt{tkzSecondPointResult}. You can choose between these two points by comparing the angles formed with the outer point, the contact point and the center. The two possible angles have different directions. Angle counterclockwise refers to \texttt{tkzFirstPointResult}.

13.2.1. Example of a tangent passing through a point on the circle

\begin{tikzpicture}[scale=.75]
\tkzDefPoint(0,0){O}
\tkzDefPoint(6,6){E}
\tkzDefRandPointOn[circle=center O radius 3](O)
\tkzGetPoint{A}
\tkzDrawSegment(O,A)
\tkzDrawCircle(O,A)
\tkzDefTangent[at=A](O)
\tkzGetPoint{h}
\tkzDrawLine[add = 4 and 3](A,h)
\tkzMarkRightAngle[fill=teal!30](O,A,h)
\end{tikzpicture}

13.2.2. Choice of contact point with tangents passing through an external point

\begin{tikzpicture}[scale=1,rotate=-30]
\tkzDefPoints{0 /0 /Q, 0 /2 /A, 6 /-1 /O}
\tkzDefTangent[from = O](Q,A) \tkzGetPoints{R}{S}
\tkzInterLC[near](O,Q)(Q,A) \tkzGetPoints{M}{N}
\tkzDrawCircle(Q,M)
\tkzDrawSegments[new,add = 0 and .2](O,R O,S)
\tkzDrawPoints(Q,R,S,M,N)
\tkzMarkAngle[gray,-stealth,size=1](O,R,Q) \tkzGetAngle{an}
\tkzLabelAngle(O,R,Q){$\pgfmathprintnumber\an^\circ$}
\tkzMarkAngle[gray,-stealth,size=1](O,S,Q) \tkzGetAngle{an}
\tkzLabelAngle(O,S,Q){$\pgfmathprintnumber\an^\circ$}
\tkzLabelPoints(Q,O,M,N,R)
\tkzLabelPoints[above,text=red](S)
\end{tikzpicture}
13. Straight lines

13.2.3. Example of tangents passing through an external point

\begin{tikzpicture}[scale=.8]
  \tkzDefPoints{0/0/c,1/0/d,3/0/a0}
  \def\tkzRadius{1}
  \tkzDrawCircle(c,d)
  \foreach \an in {0,10,...,350}{
    \tkzDefPointBy[rotation=center c angle \an](a0)
    \tkzGetPoint{a}
    \tkzDefTangent[from = a](c,d)
    \tkzGetPoints{e}{f}
    \tkzDrawLines(a,f a,e)
    \tkzDrawSegments(c,e c,f)
  }
\end{tikzpicture}

13.2.4. Example of Andrew Mertz

\begin{tikzpicture}[scale=.5]
  \tkzDefPoint(100:8){A}\tkzDefPoint(50:8){B}
  \tkzDefPoint(0,0){C} \tkzDefPoint(0,-4){R}
  \tkzDrawCircle(C,R)
  \tkzDefTangent[from = A](C,R) \tkzGetPoints{D}{E}
  \tkzDefTangent[from = B](C,R) \tkzGetPoints{F}{G}
  \tkzDrawSector[fill=teal!20,opacity=0.5](A,E)(D)
  \tkzFillSector[color=teal,opacity=0.5](B,G)(F)
\end{tikzpicture}

http://www.texample.net/tikz/examples/
13.2.5. Drawing a tangent option from

\begin{tikzpicture}[scale=.5]
\tkzDefPoint(0,0){B}
\tkzDefPoint(0,8){A}
\tkzDefSquare(A,B)
\tkzGetPoints{C}{D}
\tkzDrawSquare(A,B)
\tkzClipPolygon(A,B,C,D)
\tkzDefPoint(4,8){F}
\tkzDefPoint(4,0){E}
\tkzDefPoint(4,4){Q}
\tkzFillPolygon[color = green](A,B,C,D)
\tkzDrawCircle[fill = orange](B,A)
\tkzDrawCircle[fill = purple](E,B)
\tkzDefTangent[from=B](F,A)
\tkzInterLL(F,tkzSecondPointResult)(C,D)
\tkzInterLL(A,tkzPointResult)(F,E)
\tkzDrawCircle[fill = yellow](tkzPointResult,Q)
\tkzDefPointBy[projection= onto B--A](tkzPointResult)
\tkzDrawCircle[fill = blue!50!black](tkzPointResult,A)
\end{tikzpicture}
14. Triangles

14.1. Definition of triangles $\texttt{tkzDefTriangle}$

The following macros will allow you to define or construct a triangle from at least two points. At the moment, it is possible to define the following triangles:

- **two angles** determines a triangle with two angles;
- **equilateral** determines an equilateral triangle;
- **isosceles right** determines an isosceles right triangle;
- **half** determines a right-angled triangle such that the ratio of the measurements of the two adjacent sides to the right angle is equal to 2;
- **pythagore** determines a right-angled triangle whose side measurements are proportional to 3, 4 and 5;
- **school** determines a right-angled triangle whose angles are 30, 60 and 90 degrees;
- **golden** determines a right-angled triangle such that the ratio of the measurements on the two adjacent sides to the right angle is equal to $\Phi = 1.618034$, I chose "golden triangle" as the denomination because it comes from the golden rectangle and I kept the denomination "gold triangle" or "Euclid's triangle" for the isosceles triangle whose angles at the base are 72 degrees;
- **euclid** or **gold** for the gold triangle; in the previous version the option was "euclide" with an "e".
- **cheops** determines a third point such that the triangle is isosceles with side measurements proportional to 2, $\Phi$ and $\Phi$.

\[ \texttt{tkzDefTriangle[\{local options\}](\langle A,B \rangle)} \]

The points are ordered because the triangle is constructed following the direct direction of the trigonometric circle. This macro is either used in partnership with $\texttt{tkzGetPoint}$ or by using $\texttt{tkzPointResult}$ if it is not necessary to keep the name.

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>two angles= #1 and #2</td>
<td>no defaut triangle knowing two angles</td>
<td></td>
</tr>
<tr>
<td>equilateral</td>
<td>equilateral equilateral triangle</td>
<td></td>
</tr>
<tr>
<td>half</td>
<td>equilateral B rectangle AB = 2BC AC hypotenuse</td>
<td></td>
</tr>
<tr>
<td>isosceles right</td>
<td>equilateral isosceles right triangle</td>
<td></td>
</tr>
<tr>
<td>pythagore</td>
<td>equilateral proportional to the pythagorean triangle 3-4-5</td>
<td></td>
</tr>
<tr>
<td>pythagoras</td>
<td>equilateral same as above</td>
<td></td>
</tr>
<tr>
<td>egyptian</td>
<td>equilateral same as above</td>
<td></td>
</tr>
<tr>
<td>school</td>
<td>equilateral angles of 30, 60 and 90 degrees</td>
<td></td>
</tr>
<tr>
<td>gold</td>
<td>equilateral angles of 72, 72 and 36 degrees, A is the apex</td>
<td></td>
</tr>
<tr>
<td>euclid</td>
<td>equilateral same as above but ${AB}$ is the base</td>
<td></td>
</tr>
<tr>
<td>golden</td>
<td>equilateral B rectangle and $AB/AC = \Phi \Phi$</td>
<td></td>
</tr>
<tr>
<td>cheops</td>
<td>equilateral AC = BC, AC and BC are proportional to 2 and $\Phi$.</td>
<td></td>
</tr>
<tr>
<td>swap</td>
<td>false gives the symmetric point with respect to AB</td>
<td></td>
</tr>
</tbody>
</table>

$\texttt{tkzGetPoint}$ allows you to store the point otherwise $\texttt{tkzPointResult}$ allows for immediate use.
14.1.1. Option equilateral

```
\begin{tikzpicture}
    \tkzDefPoint(0,0){A}
    \tkzDefPoint(4,0){B}
    \tkzDefTriangle[equilateral](A,B)
    \tkzGetPoint{C}
    \tkzDrawPolygons(A,B,C)
    \tkzDefTriangle[equilateral](B,A)
    \tkzGetPoint{D}
    \tkzDrawPolygon(B,A,D)
    \tkzMarkSegments[mark=s\|](A,B B,C A,C A,D B,D)
\end{tikzpicture}
```

14.1.2. Option two angles

```
\begin{tikzpicture}
    \tkzDefPoint(0,0){A}
    \tkzDefPoint(5,0){B}
    \tkzDefTriangle[two angles = 50 and 70](A,B)
    \tkzGetPoint{C}
    \tkzDrawSegment(A,B)
    \tkzDrawPoints(A,B)
    \tkzLabelPoints(A,B)
    \tkzDrawSegments[\new](A,C B,C)
    \tkzDrawPoints[\new](C)
    \tkzLabelPoints[above,\new](C)
    \tkzLabelAngle[\pos=1.4](B,A,C){$50^\circ$}
    \tkzLabelAngle[\pos=0.8](C,B,A){$70^\circ$}
\end{tikzpicture}
```

14.1.3. Option school

The angles are 30, 60 and 90 degrees.

```
\begin{tikzpicture}
    \tkzDefPoints{0/0/A,4/0/B}
    \tkzDefTriangle[school](A,B)
    \tkzGetPoint{C}
    \tkzMarkRightAngles(C,B,A)
    \tkzLabelAngle[\pos=0.8](B,A,C){$30^\circ$}
    \tkzLabelAngle[\pos=0.8](C,B,A){$90^\circ$}
    \tkzLabelAngle[\pos=0.8](A,C,B){$60^\circ$}
    \tkzDrawSegments(A,B)
    \tkzDrawSegments[\new](A,C B,C)
\end{tikzpicture}
```

14.1.4. Option pythagore

This triangle has sides whose lengths are proportional to 3, 4 and 5.
14. Triangles

This triangle has sides whose lengths are proportional to 3, 4 and 5.

14.1.5. Option pythagore and swap

This triangle has sides whose lengths are proportional to 3, 4 and 5.

14.1.6. Option golden

14.1.7. Option isosceles right
14. Triangles

14.1.8. Option gold

\begin{tikzpicture}
\tkzDefPoints{0/0/A,4/0/B}
\tkzDefTriangle[gold](A,B)
\tkzGetPoint{C}
\tkzDrawPolygon(A,B,C)
\tkzDrawPoints(A,B,C)
\tkzLabelPoints(B) \tkzLabelPoints[below](A,C)
\tkzLabelAngle[pos=0.8](C,A,B){$36^\circ$}
\tkzLabelAngle[pos=0.8](A,B,C){$72^\circ$}
\tkzLabelAngle[pos=0.8](B,C,A){$72^\circ$}
\end{tikzpicture}

14.1.9. Option euclid

Euclid and gold are identical but the segment AB is a base in one and a side in the other.

\begin{tikzpicture}[scale=.75]
\tkzDefPoint(0,0){A} \tkzDefPoint(4,0){B}
\tkzDefTriangle[euclid](A,B) \tkzGetPoint{C}
\tkzDrawPolygon(A,B,C)
\tkzDrawPoints(A,B,C)
\tkzLabelPoints(A,B)
\tkzLabelPoints[above](C)
\tkzLabelAngle[pos=0.8](B,A,C){$72^\circ$}
\tkzLabelAngle[pos=0.8](C,B,A){$72^\circ$}
\tkzLabelAngle[pos=0.8](A,C,B){$36^\circ$}
\end{tikzpicture}

14.2. Specific triangles with \tkzDefSpcTriangle

The centers of some triangles have been defined in the "points" section, here it is a question of determining the three vertices of specific triangles.

\tkzDefSpcTriangle[⟨local options⟩](⟨p1,p2,p3⟩){⟨r1,r2,r3⟩}

The order of the points is important! p1p2p3 defines a triangle then the result is a triangle whose vertices have as reference a combination with name and r1,r2, r3. If name is empty then the references are r1,r2 and r3.

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>orthic</td>
<td>centroid</td>
<td>determined by endpoints of the altitudes ...</td>
</tr>
<tr>
<td>centroid or medial</td>
<td>centroid</td>
<td>intersection of the triangle's three triangle medians</td>
</tr>
<tr>
<td>in or incentral</td>
<td>centroid</td>
<td>determined with the angle bisectors</td>
</tr>
<tr>
<td>ex or excentral</td>
<td>centroid</td>
<td>determined with the excenters</td>
</tr>
<tr>
<td>extouch</td>
<td>centroid</td>
<td>formed by the points of tangency with the excircles each of the vertices</td>
</tr>
<tr>
<td>intouch or contact</td>
<td>centroid</td>
<td>formed by the points of tangency of the incircle</td>
</tr>
<tr>
<td>euler</td>
<td>centroid</td>
<td>formed by Euler points on the nine-point circle</td>
</tr>
<tr>
<td>symmedial</td>
<td>centroid</td>
<td>intersection points of the symmedians</td>
</tr>
<tr>
<td>tangential</td>
<td>centroid</td>
<td>formed by the lines tangent to the circumcircle</td>
</tr>
<tr>
<td>feuerbach</td>
<td>centroid</td>
<td>formed by the points of tangency of the nine-point ... circle with the excircles</td>
</tr>
<tr>
<td>name</td>
<td>empty</td>
<td>used to name the vertices</td>
</tr>
</tbody>
</table>
14.2.1. How to name the vertices

With `\tkzDefSpcTriangle[medial, name=M](A,B,C){M_A, M_B, M_C}` you get three vertices named $M_A$, $M_B$ and $M_C$.

With `\tkzDefSpcTriangle[medial](A,B,C){a,b,c}` you get three vertices named and labeled $a$, $b$ and $c$.

Possible `\tkzDefSpcTriangle[medial, name=M_](A,B,C){A,B,C}` you get three vertices named $M_A$, $M_B$ and $M_C$.

14.3. Option medial or centroid

The geometric centroid of the polygon vertices of a triangle is the point $G$ (sometimes also denoted $M$) which is also the intersection of the triangle's three triangle medians. The point is therefore sometimes called the median point. The centroid is always in the interior of the triangle.


In the following example, we obtain the Euler circle which passes through the previously defined points.

\begin{tikzpicture}[rotate=90, scale=.75]
\tkzDefPoints{0/0/A,6/0/B,0.8/4/C}
\tkzDefTriangleCenter[centroid](A,B,C)
\tkzGetPoint{M}
\tkzDefSpcTriangle[medial, name=M](A,B,C){M_A,M_B,M_C}
\tkzDrawPolygon(A,B,C)
\tkzDrawSegments[dashed,new](A,M_A B,M_B C,M_C)
\tkzDrawPolygon[new](M_A,M_B,M_C)
\tkzDrawPoints(A,B,C)
\tkzDrawPoints[new](M,M_A,M_B,M_C)
\tkzLabelPoints[center=M,font=\scriptsize](A,B,C,M_A,M_B,M_C)
\tkzLabelPoints[font=\scriptsize](M)
\end{tikzpicture}

14.3.1. Option in or incentral

The incentral triangle is the triangle whose vertices are determined by the intersections of the reference triangle's angle bisectors with the respective opposite sides.

Weisstein, Eric W. "Incentral triangle" From MathWorld–A Wolfram Web Resource.

\begin{tikzpicture}[scale=1]
\tkzDefPoints{0/0/A,5/0/B,1/3/C}
\tkzDefSpcTriangle[in, name=I](A,B,C){I_a,I_b,I_c}
\tkzInCenter(A,B,C)\tkzGetPoint{I}
\tkzDrawPolygon(A,B,C)
\tkzDrawPolygon[new](I_a,I_b,I_c)
\tkzDrawPoints(A,B,C,I,I_a,I_b,I_c)
\tkzDrawCircle[in](A,B,C)
\tkzDrawSegments[dashed,new](A,I_a B,I_b C,I_c)
\tkzAutoLabelPoints[center=I, font=\scriptsize](I_a,I_b,I_c)
\tkzAutoLabelPoints[center=I, font=\scriptsize](A,B,C)
\end{tikzpicture}
14.3.2. Option ex or excentral

The excentral triangle of a triangle ABC is the triangle $J_aJ_bJ_c$ with vertices corresponding to the excenters of ABC.

\begin{tikzpicture}[scale=.6]
\tkzDefPoints{0/0/A,6/0/B,0.8/4/C}
\tkzDefSpcTriangle[excentral,name=J](A,B,C){_a,_b,_c}
\tkzDrawPolygon(A,B,C)
\tkzDrawPolygon[new](J_a,J_b,J_c)
\tkzClipBB
\tkzDrawPoints(A,B,C)
\tkzDrawPoints[new](J_a,J_b,J_c)
\tkzLabelPoints(A,B,C)
\tkzLabelPoints[new](J_b,J_c)
\tkzLabelPoints[new,above](J_a)
\tkzDrawCircles[gray](J_a,T_a J_b,T_b J_c,T_c)
\end{tikzpicture}

14.3.3. Option intouch or contact

The contact triangle of a triangle ABC, also called the intouch triangle, is the triangle formed by the points of tangency of the incircle of ABC with ABC.

Weisstein, EricW. "Contact triangle" From MathWorld–A Wolfram Web Resource.

We obtain the intersections of the bisectors with the sides.

\begin{tikzpicture}[scale=.75]
\tkzDefPoints{0/0/A,6/0/B,0.8/4/C}
\tkzDefSpcTriangle[intouch,name=X](A,B,C){_a,_b,_c}
\tkzInCenter(A,B,C)\tkzGetPoint{I}
\tkzDrawPolygon(A,B,C)
\tkzDrawPolygon[new](X_a,X_b,X_c)
\tkzDrawPoints(A,B,C)
\tkzDrawPoints[new](X_a,X_b,X_c)
\tkzDrawCircle[in](A,B,C)
\tkzAutoLabelPoints[center=I,blue,font=\scriptsize\%(X_a,X_b,X_c)
\tkzAutoLabelPoints[center=I,red,font=\scriptsize\%(A,B,C)
\end{tikzpicture}

14.3.4. Option extouch

The extouch triangle $T_aT_bT_c$ is the triangle formed by the points of tangency of a triangle ABC with its excircles $I_a$, $I_b$, and $I_c$. The points $T_a$, $T_b$, and $T_c$ can also be constructed as the points which bisect the perimeter of $A_1A_2A_3$ starting at A, B, and C.


We obtain the points of contact of the exinscribed circles as well as the triangle formed by the centers of the exinscribed circles.
14. Triangles

14.3.5. Option orthic

Given a triangle ABC, the triangle $H_AH_BH_C$ whose vertices are endpoints of the altitudes from each of the vertices of ABC is called the orthic triangle, or sometimes the altitude triangle. The three lines $AH_A, BH_B,$ and $CH_C$ are concurrent at the orthocenter $H$ of ABC.
14.3.6. Option feuerbach

The Feuerbach triangle is the triangle formed by the three points of tangency of the nine-point circle with the excircles.

Weisstein, Eric W. "Feuerbach triangle" From MathWorld–A Wolfram Web Resource.

The points of tangency define the Feuerbach triangle.

\begin{tikzpicture}[scale=1.25]
  \tkzDefPoint(0,0){A}
  \tkzDefPoint(3,0){B}
  \tkzDefPoint(0.5,2.5){C}
  \tkzDefCircle[euler](A,B,C) \tkzGetPoint{N}
  \tkzDefSpcTriangle[feuerbach, name=F](A,B,C){_a,_b,_c}
  \tkzDefSpcTriangle[excentral, name=J](A,B,C){_a,_b,_c}
  \tkzDefSpcTriangle[extouch, name=T](A,B,C){_a,_b,_c}
  \tkzDrawPoints[blue](J_a,J_b,J_c, F_a,F_b,F_c,A,B,C)
  \tkzClipBB \tkzShowBB
  \tkzDrawCircle[purple](N,F_a)
  \tkzDrawPolygon(A,B,C)
  \tkzDrawPolygon[new](F_a,F_b,F_c)
  \tkzDrawCircles[gray](J_a,F_a J_b,F_b J_c,F_c)
  \tkzAutoLabelPoints[center=N,dist=.3, font=\scriptsize](A,B,C,F_a,F_b, F_c,J_a,J_b,J_c)
\end{tikzpicture}

14.3.7. Option tangential

The tangential triangle is the triangle $T_aT_bT_c$ formed by the lines tangent to the circumcircle of a given triangle $ABC$ at its vertices. It is therefore antipedal triangle of $ABC$ with respect to the circumcenter $O$.


\begin{tikzpicture}[scale=.5,rotate=80]
  \tkzDefPoints{0/0/A,6/0/B,1.8/4/C}
  \tkzDefSpcTriangle[tangential, name=T](A,B,C){_a,_b,_c}
  \tkzDrawPolygon(A,B,C)
  \tkzDrawPolygon[new](T_a,T_b,T_c)
  \tkzDrawPoints(A,B,C)
  \tkzDrawPoints[new](T_a,T_b,T_c)
  \tkzDrawCircle[gray](T_a,T_b,T_c)
  \tkzDrawCircle[gray](A,B,C)
  \tkzGetPoint{O}
  \tkzDrawCircle(O,A)
  \tkzLabelPoints(A,B,C)
  \tkzLabelPoints[fill=white](T_a,T_b,T_c)
\end{tikzpicture}

14.3.8. Option euler

The Euler triangle of a triangle $ABC$ is the triangle $E_aE_bE_c$ whose vertices are the midpoints of the segments joining the orthocenter $H$ with the respective vertices. The vertices of the triangle are known as the Euler points, and lie on the nine-point circle.

\begin{tikzpicture}[rotate=90,scale=1.25]
\tkzDefPoints{0/0/A,6/0/B,0.8/4/C}
\tkzDefSpcTriangle[medial, name=M](A,B,C){A,B,C}
\tkzDefTriangleCenter[euler](A,B,C)
\tkzGetPoint{N} % I= N nine points
\tkzDefTriangleCenter[ortho](A,B,C)
\tkzGetPoint{H}
\tkzDefMidPoint(A,H) \tkzGetPoint{E_A}
\tkzDefMidPoint(C,H) \tkzGetPoint{E_C}
\tkzDefMidPoint(B,H) \tkzGetPoint{E_B}
\tkzDefSpcTriangle[ortho,name=H](A,B,C){A,B,C}
\tkzDrawPolygon(A,B,C)
\tkzDrawCircle(N,E_A)
\tkzDrawSegments[\new](A,H_A B,H_B C,H_C)
\tkzDrawPoints(A,B,C,N,H)
\tkzDrawPoints[red](M_A,M_B,M_C)
\tkzDrawPoints[blue]({H_A,H_B,H_C})
\tkzDrawPoints[green]({E_A,E_B,E_C})
\tkzAutoLabelPoints*[center=N,font={\scriptsize}]{A,B,C,M_A,M_B,M_C,H_A,H_B,H_C,E_A,E_B,E_C}
\tkzLabelPoints*[font={\scriptsize}]{H,N}
\tkzMarkSegments[mark=s|,size=3pt, color=blue,line width=1pt]{B,E_B E_B,H}
\tkzDrawPolygon{color=cyan}(M_A,M_B,M_C)
\end{tikzpicture}
14.3.9. Option euler and Option orthic
14. Triangles

14.3.10. Option \textit{symmedial}

The symmedial triangle $K_A K_B K_C$ is the triangle whose vertices are the intersection points of the symmedians with the reference triangle $ABC$.

\begin{tikzpicture}
\tkzDefPoint(0,0){A}
\tkzDefPoint(5,0){B}
\tkzDefPoint(.75,4){C}
\tkzDefTriangleCenter[symmedian](A,B,C) \tkzGetPoint{K}
\tkzDefSpcTriangle[symmedial,name=K_](A,B,C){A,B,C}
\tkzDrawPolygon(A,B,C)
\tkzDrawSegments[new](A,K_A B,K_B C,K_C)
\tkzDrawPoints(A,B,C,K,K_A,K_B,K_C)
\tkzLabelPoints[font=\scriptsize](A,B,C,K,K_A,K_B,K_C)
\end{tikzpicture}

14.4. Permutation of two points of a triangle

\begin{verbatim}
\tkzPermute((pt1,pt2,pt3))
\end{verbatim}

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>(pt1,pt2,pt3) \tkzPermute(A,B,C)</td>
<td>A, B, C are unchanged, B, C exchange their position</td>
<td></td>
</tr>
</tbody>
</table>

The triangle is unchanged.

14.4.1. Modification of the school triangle

This triangle is constructed from the segment $[AB]$ on $[A, x)$
If we want the segment $[AC]$ to be on $[A, x)$, we just have to swap $B$ and $C$.

Remark: Only the first point is unchanged. The order of the last two parameters is not important.
15. Definition of polygons

15.1. Defining the points of a square

We have seen the definitions of some triangles. Let us look at the definitions of some quadrilaterals and regular polygons.

\texttt{\tkzDefSquare((pt1,pt2))}

The square is defined in the forward direction. From two points, two more points are obtained such that the four taken in order form a square. The square is defined in the forward direction. The results are in \texttt{tkzFirstPointResult} and \texttt{tkzSecondPointResult}. We can rename them with \texttt{\tkzGetPoints}.

<table>
<thead>
<tr>
<th>Arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>\texttt{(pt1,pt2)} \texttt{\tkzDefSquare((A,B))}</td>
<td>\texttt{tkzFirstPointResult} \texttt{tkzSecondPointResult}</td>
<td>The square is defined in the direct direction.</td>
</tr>
</tbody>
</table>

15.1.1. Using \texttt{\tkzDefSquare} with two points

Note the inversion of the first two points and the result.

\begin{tikzpicture}[scale=.5]
\tkzDefPoint(0,0){A} \tkzDefPoint(3,0){B}
\tkzDefSquare(A,B)
\tkzDrawPolygon(A,B,tkzFirstPointResult,\tkzSecondPointResult)
\tkzDefSquare(B,A)
\tkzDrawPolygon(B,A,tkzFirstPointResult,\tkzSecondPointResult)
\end{tikzpicture}

We may only need one point to draw an isosceles right-angled triangle so we use \texttt{\tkzGetFirstPoint} or \texttt{\tkzGetSecondPoint}.

15.1.2. Use of \texttt{\tkzDefSquare} to obtain an isosceles right-angled triangle

\begin{tikzpicture}[scale=1]
\tkzDefPoint(0,0){A}
\tkzDefPoint(3,0){B}
\tkzDefSquare(A,B) \tkzDefPoint((3,0)){A}
\tkzDrawPolygon(A,B,tkzFirstPointResult,\tkzSecondPointResult)
\tkzDefSquare(B,A)
\tkzDrawPolygon(B,A,tkzFirstPointResult,\tkzSecondPointResult)
\tkzDrawSegment(A,B)
\tkzMarkRightAngles(A,B,C)
\tkzDrawPoints(A,B)
\tkzLabelPoints(A,B)
\tkzLabelPoints(C)
\end{tikzpicture}
15. Definition of polygons

15.1.3. Pythagorean Theorem and \tkzDefSquare

\begin{tikzpicture}[scale=.5]
\tkzDefPoint(0,0){C}
\tkzDefPoint(4,0){A}
\tkzDefPoint(0,3){B}
\tkzDefSquare(B,A)\tkzGetPoints{E}{F}
\tkzDefSquare(A,C)\tkzGetPoints{G}{H}
\tkzDefSquare(C,B)\tkzGetPoints{I}{J}
\tkzDrawPolygon(A,B,C)
\tkzDrawPolygon(A,C,G,H)
\tkzDrawPolygon(C,B,I,J)
\tkzDrawPolygon(B,A,E,F)
\tkzLabelSegment(A,C){$a$}
\tkzLabelSegment(C,B){$b$}
\tkzLabelSegment[swap](A,B){$c$}
\end{tikzpicture}

15.2. Defining the points of a rectangle

\tkzDefRectangle((pt1,pt2))

The rectangle is defined in the forward direction. From two points, two more points are obtained such that the four taken in order form a rectangle. The two points passed in arguments are the ends of a diagonal of the rectangle. The sides are parallel to the axes.
The results are in \tkzFirstPointResult and \tkzSecondPointResult. We can rename them with \tkzGetPoints.

<table>
<thead>
<tr>
<th>Arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>((pt1,pt2))</td>
<td>\tkzDefRectangle((A,B))</td>
<td>The rectangle is defined in the direct direction.</td>
</tr>
</tbody>
</table>

15.2.1. Example of a rectangle definition

\begin{tikzpicture}
\tkzDefPoints{0/0/A,5/2/C}
\tkzDefRectangle(A,C) \tkzGetPoints{B}{D}
\tkzDrawPolygon[fill=teal!15](A,...,D)
\end{tikzpicture}

15.3. Definition of parallelogram

Defining the points of a parallelogram. It is a matter of completing three points in order to obtain a parallelogram.

\tkzDefParallelogram((pt1,pt2,pt3))

<table>
<thead>
<tr>
<th>arguments</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>((pt1,pt2,pt3))</td>
<td>no default</td>
<td>Three points are necessary</td>
</tr>
</tbody>
</table>
15. Definition of polygons

From three points, another point is obtained such that the four taken in order form a parallelogram. The result is in \texttt{tkzPointResult}.
We can rename it with the name \texttt{\tkzGetPoint}.

15.3.1. Example of a parallelogram definition

\begin{tikzpicture}[scale=1]
\tkzDefPoints{0/0/A, 3/0/B, 4/2/C}
\tkzDefParallelogram(A,B,C)
\tkzGetPoint{D}
\tkzDrawPolygon(A,B,C,D)
\tkzLabelPoints(A,B)
\tkzLabelPoints[above right](C,D)
\tkzDrawPoints(A,...,D)
\end{tikzpicture}

15.4. The golden rectangle

\texttt{\tkzDefGoldenRectangle(⟨point,point⟩)}

The macro determines a rectangle whose size ratio is the number $\Phi$.
The created points are in \texttt{tkzFirstPointResult} and \texttt{tkzSecondPointResult}.
They can be obtained with the macro \texttt{tkzGetPoints}. The following macro is used to draw the rectangle.

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>⟨pt1,pt2⟩</td>
<td>⟨(A,B)⟩</td>
<td>If C and D are created then $AB/BC = \Phi$.</td>
</tr>
<tr>
<td>\tkzDefGoldenRectangle</td>
<td>or \tkzDefGoldRectangle</td>
<td></td>
</tr>
</tbody>
</table>

15.4.1. Golden Rectangles

\begin{tikzpicture}[scale=.6]
\tkzDefPoint(0,0){A} \tkzDefPoint(8,0){B}
\tkzDefGoldRectangle(A,B) \tkzGetPoints{C}{D}
\tkzDefGoldRectangle(B,C) \tkzGetPoints{E}{F}
\tkzDefGoldRectangle(C,E) \tkzGetPoints{G}{H}
\tkzDrawPolygon(A,B,C,D)
\tkzDrawSegments(E,F G,H)
\end{tikzpicture}

15.4.2. Construction of the golden rectangle

Without the previous macro here is how to get the golden rectangle.
15. Definition of polygons

15.5. Regular polygon

\texttt{tkzDefRegPolygon[⟨local\_options⟩]((pt1,pt2))}

From the number of sides, depending on the options, this macro determines a regular polygon according to its center or one side.

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>((pt1,pt2))</td>
<td>((O,A))</td>
<td>with option &quot;center&quot;, O is the center of the polygon.</td>
</tr>
<tr>
<td>((pt1,pt2))</td>
<td>((A,B))</td>
<td>with option &quot;side&quot;, [AB] is a side.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>example</th>
</tr>
</thead>
<tbody>
<tr>
<td>name</td>
<td>P</td>
<td>The vertices are named P1,P2,…</td>
</tr>
<tr>
<td>sides</td>
<td>5</td>
<td>number of sides.</td>
</tr>
<tr>
<td>center</td>
<td>center</td>
<td>The first point is the center.</td>
</tr>
<tr>
<td>side</td>
<td>center</td>
<td>The two points are vertices.</td>
</tr>
<tr>
<td>Options</td>
<td>TikZ</td>
<td>…</td>
</tr>
</tbody>
</table>

15.5.1. Option center

\texttt{\begin{tikzpicture}\begin{tikzpicture}[scale=.5]
\tkzDefPoint(0,0){A}
\tkzDefPoint(8,0){B}
\tkzDefMidPoint(A,B)
\tkzGetPoint{I}
\tkzDefSquare(A,B)\tkzGetPoints{C}{D}
\tkzInterLC(A,B)(I,C)\tkzGetPoints{G}{E}
\tkzDefPointWith[colinear= at C](E,B)
\tkzGetPoint{F}
\tkzDefPointBy[projection=onto D--C](E)
\tkzGetPoint{H}
\tkzDrawArc[style=dashed](I,E)(D)
\tkzDrawSquare(A,B)
\tkzDrawPoints(C,D,E,F,H)
\tkzLabelPoints(A,B,C,D,E,F,H)
\tkzDrawSegments[style=dashed,color=gray](E,F,C,F,B,E,F,H,H,C,E,H)
\end{tikzpicture}\end{tikzpicture}}
15.5.2. Option *side*

\begin{tikzpicture}[scale=1]
  \tkzDefPoints{-4/0/A, -1/0/B}
  \tkzDefRegPolygon[side,sides=5,name=P](A,B)
  \tkzDrawPolygon[thick](P1,P...,P5)
\end{tikzpicture}
16. Circles

Among the following macros, one will allow you to draw a circle, which is not a real feat. To do this, you will need to know the center of the circle and either the radius of the circle or a point on the circumference. It seemed to me that the most frequent use was to draw a circle with a given center passing through a given point. This will be the default method, otherwise you will have to use the $R$ option. There are a large number of special circles, for example the circle circumscribed by a triangle.

- I have created a first macro $\texttt{tkzDefCircle}$ which allows, according to a particular circle, to retrieve its center and the measurement of the radius in cm. This recovery is done with the macros $\texttt{tkzGetPoint}$ and $\texttt{tkzGetLength}$;
- then a macro $\texttt{tkzDrawCircle}$;
- then a macro that allows you to color in a disc, but without drawing the circle $\texttt{tkzFillCircle}$;
- sometimes, it is necessary for a drawing to be contained in a disk, this is the role assigned to $\texttt{tkzClipCircle}$;
- it finally remains to be able to give a label to designate a circle and if several possibilities are offered, we will see here $\texttt{tkzLabelCircle}$.

16.1. Characteristics of a circle: $\texttt{tkzDefCircle}$

This macro allows you to retrieve the characteristics (center and radius) of certain circles.

\begin{verbatim}
\texttt{tkzDefCircle[(local options)]((A,B)) or ((A,B,C))}
\end{verbatim}

Attention the arguments are lists of two or three points. This macro is either used in partnership with $\texttt{tkzGetPoint}$ and/or $\texttt{tkzGetLength}$ to obtain the center and the radius of the circle, or by using $\texttt{tkzPointResult}$ and $\texttt{tkzLengthResult}$ if it is not necessary to keep the results.

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>$((pt1,pt2))$ or $((pt1,pt2,pt3))$</td>
<td>$(A,B)$</td>
<td>$[AB]$ is radius A is the center</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>through</td>
<td>through</td>
<td>circle characterized by two points defining a radius</td>
</tr>
<tr>
<td>diameter</td>
<td>through</td>
<td>circle characterized by two points defining a diameter</td>
</tr>
<tr>
<td>circum</td>
<td>through</td>
<td>circle circumscribed of a triangle</td>
</tr>
<tr>
<td>in</td>
<td>through</td>
<td>incircle a triangle</td>
</tr>
<tr>
<td>ex</td>
<td>through</td>
<td>excircle of a triangle</td>
</tr>
<tr>
<td>euler or nine</td>
<td>through</td>
<td>Euler's Circle</td>
</tr>
<tr>
<td>speicker</td>
<td>through</td>
<td>Spikey Circle</td>
</tr>
<tr>
<td>apollonius</td>
<td>through</td>
<td>circle of Apollonius</td>
</tr>
<tr>
<td>K</td>
<td>1</td>
<td>coefficient used for a circle of Apollonius</td>
</tr>
</tbody>
</table>

In the following examples, I draw the circles with a macro not yet presented, but this is not necessary. In some cases you may only need the center or the radius.
16.1.1. Example with a random point and option through

The radius measurement is: \(1.70425\text{cm} \text{ i.e. } 48.49069\text{pt}\)

\begin{tikzpicture}[scale=1]
  \tkzDefPoint(0,4){A}
  \tkzDefPoint(2,2){B}
  \tkzDefMidPoint(A,B) \tkzGetPoint{I}
  \tkzDefRandPointOn[segment = I--B] \tkzGetPoint{C}
  \tkzDefCircle[through](A,C)
  \tkzGetLength{rACcm}
  \tkzcmtopt(rACcm){rACpt}
  \tkzDrawCircle(A,C)
  \tkzDrawPoints(A,B,C)
  \tkzLabelPoints(A,B,C)
  \tkzLabelCircle[draw, text width=3cm,text centered, font=\scriptsize,below=1cm](A,C)(-90)
  \text{The radius measurement is: } \rACcm \text{ cm i.e. } \rACpt \text{ pt}
\end{tikzpicture}

16.1.2. Example with option diameter

It is simpler here to search directly for the middle of \([AB]\).

\begin{tikzpicture}[scale=1]
  \tkzDefPoint(0,0){A}
  \tkzDefPoint(2,2){B}
  \tkzDefCircle[diameter](A,B)
  \tkzGetPoint{O}
  \tkzDrawCircle(O,B)
  \tkzDrawSegment(A,B)
  \tkzDrawPoints(A,B,O)
  \tkzLabelPoints[below](A,B,O)
\end{tikzpicture}

16.1.3. Circles inscribed and circumscribed for a given triangle

\begin{tikzpicture}[scale=.75]
  \tkzDefPoint(2,2){A} \tkzDefPoint(5,-2){B}
  \tkzDefPoint(1,-2){C}
  \tkzDefCircle[in](A,B,C)
  \tkzGetPoint{I} \tkzGetLength{rIN}
  \tkzDefCircle[circum](A,B,C)
  \tkzGetPoint{K} \tkzGetLength{rCI}
  \tkzDrawCircles[R,new](I,{\rIN} K,{\rCI})
  \tkzLabelPoints[below](B,C)
  \tkzLabelPoints[above left](A,I,K)
  \tkzDrawPolygon(A,B,C)
\end{tikzpicture}

16.1.4. Example with option ex

We want to define an excircle of a triangle relatively to point C

\begin{tikzpicture}[scale=1]
  \tkzDefPoint(0,0){A}
  \tkzDefPoint(2,2){B}
  \tkzDefCircle[through](A,B,C)
  \tkzGetLength{rAc}
  \tkzcmtopt(rAc){rAcpt}
  \tkzDrawCircle(A,B,C)
  \tkzDrawPoints(A,B,C)
  \tkzLabelPoints(A,B,C)
  \tkzLabelCircle[draw, text width=3cm,text centered, font=\scriptsize,below=1cm](A,B,C)
  \text{The radius measurement is: } \rAc \text{ cm i.e. } \rAcpt \text{ pt}
\end{tikzpicture}
16.1.5. Euler’s circle for a given triangle with option euler

We verify that this circle passes through the middle of each side.

```latex
\begin{tikzpicture}[scale=.75]
  \tkzDefPoints{ 5/0/A, 0/0/B, 7/0/C}
  \tkzDefCircle[euler](A,B,C)
  \tkzGetPoint{E} \tkzGetLength{rEuler}
  \tkzDefSpcTriangle[medial](A,B,C){M_a,M_b,M_c}
  \tkzDrawPoints(A,B,C,E,M_a,M_b,M_c)
  \tkzDrawCircle[R](E,rEuler)
  \tkzDrawPolygon(A,B,C)
  \tkzDrawPoints[below](B,C)
  \tkzDrawPoints[below](A,E)
\end{tikzpicture}
```
16.1.6. Apollonius circles for a given segment option `apollonius`

\begin{tikzpicture}[scale=0.75]
  \tkzDefPoint(0,0){A}
  \tkzDefPoint(4,0){B}
  \tkzDefCircle[apollonius,K=2](A,B)
  \tkzGetPoint{K1}
  \tkzGetLength{rAp}
  \tkzDrawCircle[R,color = teal!50!black, fill=teal!20,opacity=.4](K1,rAp)
  \tkzDefCircle[apollonius,K=3](A,B)
  \tkzGetPoint{K2} \tkzGetLength{rAp}
  \tkzDrawCircle[R,color=orange!50, fill=orange!20,opacity=.4](K2,rAp)
  \tkzLabelPoints[below](A,B,K1,K2)
  \tkzDrawPoints(A,B,K1,K2)
  \tkzDrawLine[add=.2 and 1](A,B)
\end{tikzpicture}

16.1.7. Circles exinscribed to a given triangle option `ex`

You can also get the center and the projection of it on one side of the triangle. with `\tkzGetFirstPoint{Jb}` and `\tkzGetSecondPoint{Tb}`.

\begin{tikzpicture}[scale=.6]
  \tkzDefPoint(0,0){A}
  \tkzDefPoint(3,0){B}
  \tkzDefPoint(1,2.5){C}
  \tkzDefCircle[ex](A,B,C) \tkzGetPoint{I}
  \tkzGetLength{rI}
  \tkzDefCircle[ex](C,A,B) \tkzGetPoint{J}
  \tkzGetLength{rJ}
  \tkzDefCircle[ex](B,C,A) \tkzGetPoint{K}
  \tkzGetLength{rK}
  \tkzDefCircle[in](B,C,A) \tkzGetPoint{O}
  \tkzGetLength{rO}
  \tkzDrawLines[add=1.5 and 1.5](A,B A,C B,C)
  \tkzDrawPoints(I,J,K)
  \tkzDrawPolygon(A,B,C)
  \tkzDrawPolygon[dashed](I,J,K)
  \tkzDrawCircle[R,teal](O,rO)
  \tkzDrawSegments[dashed](A,K B,J C,I)
  \tkzDrawPoints(A,B,C)
  \tkzDrawCircles[R,new](J,{rJ} I,{rI} K,{rK})
  \tkzLabelPoints(A,B,C,I,J,K)
\end{tikzpicture}

16.1.8. Spiucker circle with option `spieker`

The incircle of the medial triangle $M_aM_bM_c$ is the Spieker circle:

\begin{tikzpicture}[scale=.6]
  \tkzDefPoint(0,0){A}
  \tkzDefPoint(3,0){B}
  \tkzDefPoint(1,2.5){C}
  \tkzDefCircle[ex](A,B,C) \tkzGetPoint{I}
  \tkzGetLength{rI}
  \tkzDefCircle[ex](C,A,B) \tkzGetPoint{J}
  \tkzGetLength{rJ}
  \tkzDefCircle[ex](B,C,A) \tkzGetPoint{K}
  \tkzGetLength{rK}
  \tkzDefCircle[in](B,C,A) \tkzGetPoint{O}
  \tkzGetLength{rO}
  \tkzDrawLines[add=1.5 and 1.5](A,B A,C B,C)
  \tkzDrawPoints(I,J,K)
  \tkzDrawPolygon(A,B,C)
  \tkzDrawPolygon[dashed](I,J,K)
  \tkzDrawCircle[R,teal](O,rO)
  \tkzDrawSegments[dashed](A,K B,J C,I)
  \tkzDrawPoints(A,B,C)
  \tkzDrawCircles[R,new](J,{rJ} I,{rI} K,{rK})
  \tkzLabelPoints(A,B,C,I,J,K)
\end{tikzpicture}
16. Circles

16.1.9. Examples from js bibra tex.stackexchange.com

\begin{tikzpicture}[scale=1]
\tkzDefPoints{ 0/0/A, 4/0/B, 0.8/4/C}
\tkzDefSpcTriangle[medial](A,B,C){M_a,M_b,M_c}
\tkzDefTriangleCenter[spieker](A,B,C)
\tkzGetPoint{S_p}
\tkzDrawPolygon(A,B,C)
\tkzDrawPolygon[cyan](M_a,M_b,M_c)
\tkzDrawPoints(B,C,A)
\tkzDrawPoints[new](M_a,M_b,M_c,S_p)
\tkzDrawCircle[in,new](M_a,M_b,M_c)
\tkzAutoLabelPoints[center=S_p, dist=.3](M_a,M_b,M_c)
\tkzLabelPoints[right](S_p)
\tkzAutoLabelPoints[center=S_p](A,B,C)
\end{tikzpicture}

\begin{tikzpicture}[scale=0.4]
\tkzDefPoint(6,4){A}
\tkzDefPoint(6,-4){B}
\tkzDefMidPoint(B,A) \tkzGetPoint{P}
\tkzDefLine[orthogonal=through P](A,B)
\tkzGetPoint{X}
\tkzDefCircle[through](X,P)
\tkzCalcLength(X,P) \tkzGetLength{rXP}
\tkzDefShiftPoint[X](180:rXP*2){Y}
\tkzDefPointWith[linear,K=0.3](Y,P)
\tkzGetPoint{x}
\tkzDrawPoints(X,x)
\tkzDrawCircles(x,P X,P)
\tkzLabelLine[pos=0.5, above](x,P){r1}
\tkzDefShiftPoint[X](90:rXP){X'}
\tkzDrawSegments[<->, >=triangle 45](X,X' P,x)
\tkzLabelLine[pos=0.5, above, sloped](X,X'){r}
\tkzLabelPoints[above](x)
\tkzLabelPoints[above](X)
\end{tikzpicture}
16.2. Projection of excenters

\begin{tikzpicture}
\tkzDefPoint(0,4){A}
\tkzDefPoint(2,2){B}
\tkzDefMidPoint(B,A)\tkzGetPoint{P}
\tkzDefLine[orthogonal =through P](B,A)
\tkzGetPoint(X)
\tkzDefCircle[through](X,P)
\tkzGetLength{xPpt}
\tkzDefPointWith[linear,K=0.3](X,P)
\tkzGetPoint{y}
\tkzDrawPoints(X,y)
\tkzDrawSegment[x=0.3](X,P)
\tkzDrawSegment(P,X)
\tkzLabelPoints(X,y)
\tkzCalcLength[cm](X,P)\tkzGetLength{xP}
\tkzDefShiftPoint[X](-90:0.5\xP){Y}
\tkzDrawSegments(Y,P){Y}{X}
\tkzLabelLine[pos=0.5,left](y,P){X}
\tkzCalcLength[cm](X,P)\tkzGetLength{xP}
\tkzDefShiftPoint[X](-90:0.5\xP){Y}
\tkzDrawSegments(Y,P){Y}{X}
\tkzLabelLine[pos=0.5,left](y,P){X}
\end{tikzpicture}

Each excenter has three projections on the sides of the triangle ABC. We can do this with one macro \texttt{\tkzDefProjExcenter}.

\begin{tabular}{ll}
<table>
<thead>
<tr>
<th>Option</th>
<th>Default</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>name</td>
<td>no default</td>
<td>used to name the vertices</td>
</tr>
<tr>
<td>arguments</td>
<td>default</td>
<td>definition</td>
</tr>
<tr>
<td>(pt1=\alpha_1, pt2=\alpha_2, ...)</td>
<td>no default</td>
<td>Each point has a assigned weight</td>
</tr>
</tbody>
</table>
\end{tabular}

\texttt{tkz-euclide} AlterMundus
16. Circles

16.2.1. Excircles

\begin{tikzpicture}[scale=.6]
\tikzset{line style/.append style={line width=.2pt}}
\tikzset{label style/.append style={color=teal,font=\footnotesize}}
\tkzDefPoints{0/0/A,5/0/B,0.8/4/C}
\tkzDefSpcTriangle[excentral,name=J](A,B,C){a,b,c}
\tkzDefSpcTriangle[intouch,name=I](A,B,C){a,b,c}
\tkzDefProjExcenter[name=J](A,B,C)(a,b,c){X,Y,Z}
\tkzDefCircle[in](A,B,C) \tkzGetPoint{I} \tkzGetSecondPoint{T}
\tkzDrawCircles[red](Ja,Xa Jb,Yb Jc,Zc)
\tkzDrawCircle(I,T)
\tkzDrawPolygon[dashed,color=blue](Ja,Jb,Jc)
\tkzDrawLines[add=1.5 and 1.5](A,C A,B B,C)
\tkzDrawSegments(Ja,Xa Ja,Ya Ja,Za
Jb,Xb Jb,Yb Jb,Zb
Jc,Xc Jc,Yc Jc,Zc
I,Ja I,Jb I,Jc)
\tkzMarkRightAngles[size=.2,fill=gray!15](%}
Ja,Za,B Ja,Xa,B
Ja,Ya,C Jb,Yb,C
Jb,Zb,B Jb,Xb,C
Jc,Yc,A Jc,Zc,B
Jc,Xc,C I,Ja,B
\end{tikzpicture}
\textit{I, Ib, C, Ic, A)}
\tkzDrawSegments[blue](Jc, C, Ja, A, Jb, B)
\tkzLabelPoints(A, Yc, Ya, Yb, Ja, I, Zc)
\tkzLabelPoints[left](Jb, Ib)
\tkzLabelPoints[below](Zb, Ic, Jc, B, Za)
\tkzLabelPoints[above right](C)
\tkzLabelPoints[right](Xb, Ia, Xa, Xc)
\end{tikzpicture}
16.3. Definition of circle by transformation; \texttt{tkzDefCircleBy}

These transformations are:

- translation;
- homothety;
- orthogonal reflection or symmetry;
- central symmetry;
- orthogonal projection;
- rotation (degrees);
- orthogonal from ;
- orthogonal through;
- inversion.

The choice of transformations is made through the options. The macro is \texttt{tkzDefCircleBy} and the other for the transformation of a list of points \texttt{tkzDefCirclesBy}. For example, we'll write:

\texttt{tkzDefCircleBy[\lbrace local options \rbrace][\langle pt1,pt2 \rangle](O,M)}

O is the center and M is a point on the circle. The image is a circle. The new center is \texttt{tkzFirstPointResult} and \texttt{tkzSecondPointResult} is a point on the new circle. You can get the results with the macro \texttt{tkzGetPoints}.

\begin{tabular}{lll}
\texttt{tkzDefCircleBy[\langle pt1,pt2 \rangle]} & \texttt{\langle pt1,pt2 \rangle} & \texttt{(O,M)} \\
\hline
\texttt{\langle local options \rangle} & \texttt{\langle pt1,pt2 \rangle} & \texttt{(O,M)} \\
\hline
\texttt{\langle local options \rangle} & \texttt{\langle pt1,pt2 \rangle} & \texttt{(O,M)} \\
\hline
\end{tabular}

The argument is a couple of points. The results is a couple of points. If you want to keep these points then the macro \texttt{tkzGetPoints\lbrace O' \rbrace\lbrace M' \rbrace} allows you to assign the name \texttt{O'} to the center and \texttt{M'} to the point on the circle.

Arguments definition examples

<table>
<thead>
<tr>
<th>\texttt{pt1,pt2}</th>
<th>\texttt{existing points}</th>
<th>\texttt{\langle pt1,pt2 \rangle}</th>
<th>\texttt{\langle pt1,pt2 \rangle}</th>
</tr>
</thead>
<tbody>
<tr>
<td>\texttt{\langle local options \rangle}</td>
<td>\texttt{\langle pt1,pt2 \rangle}</td>
<td>\texttt{\langle pt1,pt2 \rangle}</td>
<td>\texttt{\langle pt1,pt2 \rangle}</td>
</tr>
<tr>
<td>\texttt{\langle local options \rangle}</td>
<td>\texttt{\langle pt1,pt2 \rangle}</td>
<td>\texttt{\langle pt1,pt2 \rangle}</td>
<td>\texttt{\langle pt1,pt2 \rangle}</td>
</tr>
</tbody>
</table>

The image is only defined and not drawn.
16.3.1. Examples of transformations

16.3.2. Translation

\begin{tikzpicture}[>=latex]
\tkzDefPoint(0,0){A} \tkzDefPoint(3,1){B}
\tkzDefPoint(3,2){C} \tkzDefPoint(4,3){D}
\tkzDefCircleBy[translation= from B to A](C,D)
\tkzGetPoints{C'}{D'}
\tkzDrawPoints[teal](A,B,C,D,C',D')
\tkzDrawSegments[orange,->](A,B)
\tkzDrawCircles(C,D C',D')
\tkzLabelPoints[above,color=teal](A,B,C,C')
\tkzLabelPoints[above,color=teal](D,D')
\end{tikzpicture}

16.3.3. Reflection (orthogonal symmetry)

\begin{tikzpicture}[>=latex]
\tkzDefPoint(0,0){A} \tkzDefPoint(3,1){B}
\tkzDefPoint(3,2){C} \tkzDefPoint(4,3){D}
\tkzDefCircleBy[reflection = over A--B](C,D)
\tkzGetPoints{C'}{D'}
\tkzDrawPoints[teal](A,B,C,D,C',D')
\tkzDrawLine[add =0 and 1,orange](A,B)
\tkzDrawCircles(C,D C',D')
\tkzLabelPoints[below,color=teal](A,B,C,C')
\tkzLabelPoints[above,color=teal](D,D')
\end{tikzpicture}

16.3.4. Homothety

\begin{tikzpicture}[scale=1.2]
\tkzDefPoint(0,0){A} \tkzDefPoint(3,1){B}
\tkzDefPoint(3,2){C} \tkzDefPoint(4,3){D}
\tkzDefCircleBy[homothety=center A ratio .5](C,D)
\tkzGetPoints{C'}{D'}
\tkzDrawPoints[teal](A,C,D,C',D')
\tkzDrawCircles(C,D C',D')
\tkzLabelPoints[above,color=teal](A,C,C')
\tkzLabelPoints[above,color=teal](D,D')
\end{tikzpicture}
16.3.5. Symmetry

\begin{tikzpicture}[scale=1]
  \tkzDefPoint(0,0){A} \tkzDefPoint(3,1){B}
  \tkzDefPoint(3,2){C} \tkzDefPoint(4,3){D}
  \tkzDefCircleBy[symmetry=center B](C,D)
  \tkzGetPoints{C'}{D'}
  \tkzDrawPoints[teal](B,C,D,C',D')
  \tkzDrawLines[orange](C,C' D,D')
  \tkzDrawCircles(C,D C',D')
  \tkzLabelPoints[color=teal](A,C,C')
  \tkzLabelPoints[color=teal,above](D)
  \tkzLabelPoints[color=teal,below](D')
\end{tikzpicture}

16.3.6. Rotation

\begin{tikzpicture}[scale=0.5]
  \tkzDefPoint(3,-1){B}
  \tkzDefPoint(3,2){C} \tkzDefPoint(4,3){D}
  \tkzDefCircleBy[rotation=center B angle 90](C,D)
  \tkzGetPoints{C'}{D'}
  \tkzDrawPoints[teal](B,C,D,C',D')
  \tkzDrawCircles(C,D C',D')
\end{tikzpicture}

16.3.7. Orthogonal from

Orthogonal circle of given center. \texttt{\tkzGetPoints\{z1\}\{z2\}} gives two points of the circle.

\begin{tikzpicture}[scale=.75]
  \tkzDefPoints{0/0/O,1/0/A}
  \tkzDefPoints{1.5/1.25/B,-2/-3/C}
  \tkzDefCircleBy[orthogonal from=B](O,A)
  \tkzGetPoints\{z1\}\{z2\}
  \tkzDefCircleBy[orthogonal from=C](O,A)
  \tkzGetPoints\{t1\}\{t2\}
  \tkzDrawCircle(O,A)
  \tkzDrawCircles\{new\}(B,z1 C,t1)
  \tkzDrawPoints\{t1,t2,C\}
  \tkzDrawPoints\{z1,z2,0,A,B\}
  \tkzLabelPoints\{O,A,B,C\}
\end{tikzpicture}

16.3.8. Orthogonal from : Right angle between circles

We are looking for a circle orthogonal to the given circle.
16. Circles

16.3.9. Orthogonal through

Orthogonal circle passing through two given points.

\begin{tikzpicture}[scale=1]
\tkzDefPoint(0,0){O}
\tkzDefPoint(1,0){A}
\tkzDrawCircle(O,A)
\tkzDefPoint(-1.5,-1.5){z1}
\tkzDefPoint(1.5,-1.25){z2}
\tkzDefCircleBy[orthogonal through=z1 and z2](O,A)
\tkzGetPoint{c}
\tkzDrawCircle[new](tkzPointResult,z1)
\tkzDrawPoints[new](O,A,z1,z2,c)
\tkzLabelPoints(O,A,z1,z2,c)
\end{tikzpicture}

16.3.10. Inversion

\begin{tikzpicture}[scale=1.5]
\tkzSetUpPoint[size=4,color=red,fill=red!20]
\tkzSetUpStyle[color=purple,ultra thin]{st1}
\tkzSetUpStyle[color=cyan,ultra thin]{st2}
\tkzDefPoint(2,0){A} \tkzDefPoint(3,0){B}
\tkzDefPoint(3,2){C} \tkzDefPoint(4,2){D}
\tkzDefCircleBy[inversion = center B through A](C,D)
\tkzGetPoints(C',D')
\tkzDrawPoints(A,B,C,D,C',D')
\tkzLabelPoints(A,B,C,D,C',D')
\tkzDrawCircles(B,A)
\tkzDrawCircles[st1](C,D)
\tkzDrawCircles[st2](C',D')
\end{tikzpicture}
17. Intersections

It is possible to determine the coordinates of the points of intersection between two straight lines, a straight line and a circle, and two circles. The associated commands have no optional arguments and the user must determine the existence of the intersection points himself.

17.1. Intersection of two straight lines \texttt{\tkzInterLL}

\texttt{\tkzInterLL((A,B))((C,D))}

Defines the intersection point \texttt{\tkzPointResult} of the two lines (AB) and (CD). The known points are given in pairs (two per line) in brackets, and the resulting point can be retrieved with the macro \texttt{\tkzDefPoint}.

17.1.1. Example of intersection between two straight lines

\begin{tikzpicture}[rotate=-45,scale=.75]
\tkzDefPoint(2,1){A}
\tkzDefPoint(6,5){B}
\tkzDefPoint(3,6){C}
\tkzDefPoint(5,2){D}
\tkzDrawLines(A,B C,D)
\tkzInterLL(A,B)(C,D)
\tkzGetPoint{I}
\tkzDrawPoints[color=blue](A,B,C,D)
\tkzDrawPoint[color=red](I)
\end{tikzpicture}

17.2. Intersection of a straight line and a circle \texttt{\tkzInterLC}

As before, the line is defined by a couple of points. The circle is also defined by a couple:

- (O,C) which is a pair of points, the first is the center and the second is any point on the circle.
- (O,r) The r measure is the radius measure.

\texttt{\tkzInterLC[(\texttt{options})](\langle A,B\rangle)(\langle O,C\rangle) or (\langle O,r\rangle) or (\langle O,C,D\rangle)}

So the arguments are two couples.

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>N</td>
<td>N</td>
<td>(O,C) determines the circle</td>
</tr>
<tr>
<td>R</td>
<td>N</td>
<td>(O,1) unit 1 cm</td>
</tr>
<tr>
<td>with nodes</td>
<td>N</td>
<td>(O,C,D) CD is a radius</td>
</tr>
<tr>
<td>common=pt</td>
<td></td>
<td>pt is common point; \texttt{\tkzFirstPoint} gives the other point</td>
</tr>
<tr>
<td>near</td>
<td></td>
<td>\texttt{\tkzFirstPoint} is the closest point to the first point of the line</td>
</tr>
</tbody>
</table>

The macro defines the intersection points I and J of the line (AB) and the center circle O with radius r if they exist; otherwise, an error will be reported in the .log file. \texttt{with nodes} avoids you to calculate the radius which is the length of \texttt{CD}. If common and near are not used then \texttt{\tkzFirstPoint} is the smallest angle (angle with \texttt{\tkzSecondPoint} and the center of the circle).
\tkzTestInterLC((O,A))((O',B))

So the arguments are two couples which define a line and a circle with a center and a point on the circle. If there is a non empty intersection between these the line and the circle then the test \iftkzFlagLC gives true.

17.2.1. test line-circle intersection

\begin{tikzpicture}[scale=1]
\tkzDefPoints{
3 /4 /I,
3 /2 /P,
0 /2 /La,
8 /3 /Lb}
\tkzDrawCircle(I,P)
\foreach \i in {1,...,3}{
\coordinate (Lb) at (8,\i);
\tkzDrawLine(La,Lb)
\tkzTestInterLC(La,Lb)(I,P)
\iftkzFlagLC
\tkzInterLC(La,Lb)(I,P)
\tkzGetPoints{a}{b}
\tkzDrawPoints(a,b)
\fi}
\end{tikzpicture}

17.2.2. Line-circle intersection

In the following example, the drawing of the circle uses two points and the intersection of the straight line and the circle uses two pairs of points. We will compare the angles $\angle D, E, O$ and $\angle E, D, O$. These angles are in opposite directions. \tkzFirstPoint is assigned to the point that forms the angle with the smallest measure (counterclockwise direction). The counterclockwise angle $\angle D, E, O$ has a measure equal to $360^\circ$ minus the measure of $\angle O, E, D$.

\begin{tikzpicture}[scale=.75]
\tkzInit[xmax=5,ymax=4]
\tkzDefPoint(1,1){O}
\tkzDefPoint(-2,4){La}
\tkzDefPoint(5,0){Lb}
\tkzDefPoint(3,3){C}
\tkzInterLC(A,B)(O,C) \tkzGetPoints{D}{E}
\tkzMarkAngle[->,size=1.5](E,D,O)
\tkzDrawPolygons[new](O,D,E)
\tkzMarkAngle[->,size=1.5](D,E,O)
\tkzDrawCircle(O,C)
\tkzDrawPoints[teal](O,La,Lb,C)
\tkzDrawPoints[red](D,E)
\tkzDrawLine(La,Lb)
\tkzLabelPoints[above right](O,La,Lb,C,D,E)
\end{tikzpicture}

17.2.3. Line passing through the center option common

This case is special. You cannot compare the angles. In this case, the option \texttt{near} must be used. \tkzFirstPoint is assigned to the point closest to the first point given for the line. Here we want A to be closest to Lb.

\begin{tikzpicture}[scale=.75]
\tkzDefPoint(1,1){O}
\tkzDefPoint(-2,4){La}
\tkzDefPoint(5,0){Lb}
\tkzDefPoint(3,3){C}
\tkzInterLC(A,B)(O,C) \tkzGetPoints{D}{E}
\tkzMarkAngle[-,size=1.5](E,D,O)
\tkzDrawPolygons[teal](O,D,E)
\tkzDrawCircle(O,C)
\tkzDrawPoints[teal](O,La,Lb,C)
\tkzDrawPoints[red](D,E)
\tkzDrawLine(La,Lb)
\tkzLabelPoints[above right](O,La,Lb,C,D,E)
\end{tikzpicture}
17.2.4. Line-circle intersection with option common

A special case that we often meet, a point of the line is on the circle and we are looking for the other common point.

17.2.5. Line-circle intersection order of points

The idea is to compare the angles formed with the first defining point of the line, a resultant point and the center of the circle. The first point is the one that corresponds to the smallest angle. As you can see $\angle BCO < \angle BEO$. To tell the truth, $\angle BEO$ is counterclockwise.
17.2.6. Example with \foreach

\begin{tikzpicture}[scale=3,rotate=180]
\tkzDefPoint(0,1){J}
\tkzDefPoint(0,0){O}
\foreach \i in {0,-5,-10,...,-90}
{\tkzDefPoint({2.5*cos(\i*pi/180)},{1+2.5*sin(\i*pi/180)}){P}
\tkzInterLC[\R](P,J)(O,1){N}{M}
\tkzDrawSegment[color=orange](J,N)
\tkzDrawPoints[red](N)}
\foreach \i in {-90,-95,...,-175,-180}
{\tkzDefPoint({2.5*cos(\i*pi/180)},{1+2.5*sin(\i*pi/180)}){P}
\tkzInterLC[\R](P,J)(O,1){N}{M}
\tkzDrawSegment[color=orange](J,M)
\tkzDrawPoints[red](M)}
\end{tikzpicture}

17.2.7. Line-circle intersection with option near

D is the point closest to b.

\begin{tikzpicture}
\tkzDefPoints{6/6/0.5/1/A,2/2/0/O,3/1/D}
\tkzInterLC[common=A](B,D)(O,A) \tkzGetPoints{C}{E}
\tkzDrawPoints(O,A,B,D)
\tkzDrawCircle(O,A) \tkzDrawLine(E,O)
\tkzDrawSegments[dashed](B,O O,C)
\tkzMarkAngle[->,size=1.5](B,C,O)
\tkzDrawSegments[dashed](O,E)
\tkzMarkAngle[->,size=1.5](B,E,O)
\tkzDrawPoints(C,E)
\tkzLabelPoints[above](O,E)
\tkzLabelPoints[right](A,B,C,D)
\end{tikzpicture}
17. More complex example of a line-circle intersection

Figure from [http://gogeometry.com/problem/p190_tangent_circle](http://gogeometry.com/problem/p190_tangent_circle)

17.2.9. Circle defined by a center and a measure, and special cases

Let’s look at some special cases like straight lines tangent to the circle.
17.2.10. Calculation of radius

With \pgfmath and \pgfmathsetmacro

The radius measurement may be the result of a calculation that is not done within the intersection macro, but before. A length can be calculated in several ways. It is possible of course, to use the module \pgfmath and the macro \pgfmathsetmacro. In some cases, the results obtained are not precise enough, so the following calculation $0.0002 \div 0.0001$ gives 1.98 with \pgfmath while xfp will give 2.

With \texttt{xfp} and \texttt{\fpeval}:

```latex
\begin{tikzpicture}
\tkzDefPoint(2,2){A}
\tkzDefPoint(5,4){B}
\tkzDefPoint(4,4){O}
\pgfmathsetmacro\tkzLen{\fpeval{0.0002/0.0001}}% or \edef\tkzLen{\fpeval{0.0002/0.0001}}
\tkzInterLC[R](A,B)(O,\tkzLen)
\tkzGetPoints{I}{J}
\tkzDrawCircle[R](O,\tkzLen)
\tkzDrawPoints[color=blue](A,B)
\tkzDrawPoints[color=red](I,J)
\end{tikzpicture}
```
17.2.11. Option "with nodes"

\begin{tikzpicture}[scale=.75]
\tkzDefPoints{0/0/A,4/0/B,1/1/D,2/0/E}
\tkzDefTriangle[equilateral](A,B)
\tkzGetPoint{C}
\tkzInterLC[with nodes](D,E)(C,A,B)
\tkzGetPoints{F}{G}
\tkzDrawCircle(C,A)
\tkzDrawPolygon(A,B,C)
\tkzDrawPoints(A,...,G)
\tkzDrawLine(F,G)
\end{tikzpicture}

17.3. Intersection of two circles \texttt{\tkzInterCC}

The most frequent case is that of two circles defined by their center and a point, but as before the option \texttt{R} allows to use the radius measurements.

\texttt{\tkzInterCC[\texttt{options}]((O,A))((O',A')) or ((O,r))((O',r')) or ((O,A,B))((O',C,D))}

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>N</td>
<td>N</td>
<td>OA and O'A' are radii, O and O' are the centers.</td>
</tr>
<tr>
<td>R</td>
<td>N</td>
<td>r and r' are dimensions and measure the radii.</td>
</tr>
<tr>
<td>with nodes</td>
<td>N</td>
<td>in (A,A,C)(C,B,F) AC and BF give the radii.</td>
</tr>
<tr>
<td>common=pt</td>
<td>pt</td>
<td>pt is common point; \texttt{tkzFirstPoint} gives the other point.</td>
</tr>
</tbody>
</table>

This macro defines the intersection point(s) I and J of the two center circles O and O'. If the two circles do not have a common point then the macro ends with an error that is not handled. If the centers are O and O' and the intersections are A and B then the angles O,A,O' and O,B,O' are in opposite directions. \texttt{tkzFirstPoint} is assigned to the point that forms the "clockwise" angle.

\texttt{\tkzTestInterCC((O,A))((O',B))}

So the arguments are two couples which define two circles with a center and a point on the circle. If there is a non empty intersection between these two circles then the test \texttt{\iftkzFlagCC} gives true.
17.3.1. test circle-circle intersection

\begin{tikzpicture}[scale=1]
\tkzDefPoints{0 /0 /A, 2 /0 /B, 4 /0 /I, 1 /0 /P}
\tkzDrawCircle(A,B)
\foreach \i in {1,...,3}{%
\coordinate (P) at (\i,0);
\tkzDrawCircle[new](I,P)
\tkzTestInterCC(A,B)(I,P)
\iftkzFlagCC
\tkzInterCC(A,B)(I,P) \tkzGetPoints{a}{b}
\tkzDrawPoints(a,b)
\fi}
\end{tikzpicture}

17.3.2. circle-circle intersection with common point.

\begin{tikzpicture}[scale=.5]
\tkzDefPoints{0/0/O,5/-1/A,2/2/B}
\tkzDrawPoints(O,A,B)
\tkzDrawCircles(O,B A,B)
\tkzInterCC[common=B](O,B)(A,B) \tkzGetFirstPoint{C}
\tkzDrawPoint(C)
\tkzLabelPoints[above](O,A,B,C)
\end{tikzpicture}

17.3.3. circle-circle intersection order of points.
The idea is to compare the angles formed with the first center, a resultant point and the center of the second circle. The first point is the one that corresponds to the smallest angle.
As you can see $\widehat{ODB} < \widehat{OBE}$

\begin{tikzpicture}[scale=.5]
\pgfkeys{/pgf/number format/.cd, fixed relative, precision=4}
\tkzDefPoints{0/0/O,5/-1/A,2/2/B,2/-1/C}
\tkzDrawPoints(O,A,B)
\tkzDrawCircles(O,A B,C)
\tkzInterCC(O,A)(B,C) \tkzGetPoints{D}{E}
\tkzDrawPoints(C,D,E)
\tkzLabelPoints(O,A,B,C,D,E)
\tkzDrawSegments[cyan](D,O D,B)
\tkzMarkAngle[red,->,size=1.5](O,D,B) \tkzGetAngle{an}
\tkzLabelAngle(O,D,B){$\pgfmathprintnumber{\an}$}
\tkzDrawSegments[cyan](E,O E,B)
\tkzMarkAngle[red,->,size=1.5](O,E,B) \tkzGetAngle{an}
\tkzLabelAngle(O,E,B){$\pgfmathprintnumber{\an}$}
\end{tikzpicture}
17.3.4. Construction of an equilateral triangle.

\[\triangle A, B, C \text{ is a clockwise angle}\]

\begin{tikzpicture}[trim left=-1cm,scale=.5]
\tkzDefPoint(1,1){A}
\tkzDefPoint(5,1){B}
\tkzInterCC(A,B)(B,A)\tkzGetPoints{C}{D}
\tkzDrawPoint[C](C)
\tkzDrawCircles(A,B B,A)
\tkzCompass[color=red](A,C)
\tkzCompass[color=red](B,C)
\tkzDrawPolygon(A,B,C)
\tkzMarkSegments[mark=\][A,C B,C]
\tkzLabelPoints[]\tkzLabelPoint[above](C){$C$}
\tkzLabelPoints[]\tkzLabelPoint(A,B)
\tkzLabelPoints[]\tkzLabelPoint[above](C){$C$}
\end{tikzpicture}

17.3.5. Segment trisection

The idea here is to divide a segment with a ruler and a compass into three segments of equal length.

\begin{tikzpicture}[scale=.6]
\tkzDefPoint(0,0){A}
\tkzDefPoint(3,2){B}
\tkzInterCC(A,B)(B,A) \tkzGetSecondPoint{D}
\tkzInterCC(D,B)(B,A) \tkzGetPoints{A}{C}
\tkzInterCC(D,B)(A,B) \tkzGetPoints{E}{B}
\tkzInterLC[common=D](C,D)(E,D) \tkzGetFirstPoint{F}
\tkzInterLL(A,F)(B,C) \tkzGetPoint{O}
\tkzInterLL(O,D)(A,B) \tkzGetPoint{H}
\tkzInterLL(O,E)(A,B) \tkzGetPoint{G}
\tkzDrawCircles(D,E A,B B,A E,A)
\tkzDrawSegments[]\tkzDrawPoints(A,...,H)
\tkzDrawSegments(A,B B,D A,D A,E F C,F B,C)
\tkzMarkSegments[mark=\][A,G G,H H,B]
\end{tikzpicture}
17.3.6. With the option "with nodes"

\begin{tikzpicture}[scale=.5]
\tkzDefPoints{0/0/A,0/5/B,5/0/C}
\tkzDefPoint(54:5){F}
\tkzInterCC[with nodes](A,A,C)(C,B,F)
\tkzGetPoints{a}{e}
\tkzInterCC(A,C)(a,e) \tkzGetFirstPoint{b}
\tkzInterCC(A,C)(b,a) \tkzGetFirstPoint{c}
\tkzInterCC(A,C)(c,b) \tkzGetFirstPoint{d}
\tkzDrawCircle[new](A,C)
\tkzDrawPoints(a,b,c,d,e)
\tkzDrawPolygon(a,b,c,d,e)
\foreach \vertex/\num in {a/36,b/108,c/180,d/252,e/324}{{% 
\tkzDrawPoint(\vertex)
\tkzLabelPoint[label=\num:$\vertex$](\vertex){}
\tkzDrawSegment(A,\vertex)
}}\end{tikzpicture}

17.3.7. Mix of intersections

\begin{tikzpicture}[scale = .75]
\tkzDefPoint(2,2){A}
\tkzDefPoint(0,0){B}
\tkzDefPoint(-2,2){C}
\tkzDefPoint(0,4){D}
\tkzDefPoint(4,2){E}
\tkzCircumCenter(A,B,C)\tkzGetPoint{O}
\tkzInterCC[R](O,2)(D,2) \tkzGetPoints{M1}{M2}
\tkzInterCC(O,A)(D,O) \tkzGetPoints{1}{2}
\tkzInterLC(A,E)(B,M1) \tkzGetSecondPoint{M3}
\tkzInterLC(O,C)(M3,D) \tkzGetSecondPoint{L}
\tkzDrawSegments(C,L)
\tkzDrawPoints(A,B,C,D,E,M1,M2,M3,O,L)
\tkzDrawSegments[draw](O,E)
\tkzDrawSegments[new](C,A D,B)
\tkzDrawPoint(O)
\tkzDrawCircles[new](M3,D B,M2 D,O)
\tkzDrawCircle(O,A)
\tkzLabelPoints(A,B,C,D,E,M1,M2,M3,O,L)\end{tikzpicture}

17.3.8. Altshiller-Court's theorem

The two lines joining the points of intersection of two orthogonal circles to a point on one of the circles met the other circle in two diametricaly oposite points. Altshiller p 176
\begin{tikzpicture}
\tkzDefPoints{0/0/P,5/0/Q,3/2/I}
\tkzDefCircleBy[orthogonal from=P](Q,I)
\tkzGetFirstPoint{E}
\tkzDrawCircles(P,E Q,E)
\tkzInterCC[common=E](P,E)(Q,E) \tkzGetFirstPoint{F}
\tkzDefPointOnCircle[through = angle 80 center P point E]
\tkzGetPoint{A}
\tkzInterLC[common=E](A,E)(Q,E) \tkzGetFirstPoint{C}
\tkzInterLL(A,F)(C,Q) \tkzGetPoint{D}
\tkzDrawLines[add=0 and 1](P,Q)
\tkzDrawLines[add=0 and 2](A,E)
\tkzDrawSegments(P,E E,F,F,C A,F C,D)
\tkzDrawPoints(P,Q,E,F,A,C,D)
\tkzLabelPoints(P,Q,E,F,A,C,D)
\end{tikzpicture}
18. Angles

18.1. Definition and usage with \texttt{tkz-euclide}

In Euclidean geometry, an angle is the figure formed by two rays, called the sides of the angle, sharing a common endpoint, called the vertex of the angle. [Wikipedia]. A ray with \texttt{tkz-euclide} is defined by two points also each angle is defined with three points like $\angle \text{AOB}$. The vertex $O$ is the second point. Their order is important because it is assumed that the angle is specified in the direct order (counterclockwise). In trigonometry and mathematics in general, plane angles are conventionally measured counterclockwise, starting with $0^\circ$ pointing directly to the right (or east), and $90^\circ$ pointing straight up (or north)[Wikipedia]. Let us agree that an angle measured counterclockwise is positive.

\[ \text{Angles are involved in several macros like } \texttt{\tkzDefPoint, \tkzDefPointBy [rotation = \ldots], \tkzDrawArc} \text{ and the next one } \texttt{\tkzGetAngle}. \text{ With the exception of the last one, all these macros accept negative angles.} \]

\begin{center}
\begin{tabular}{|c|c|}
\hline
\textbf{\texttt{\tkzDefPointBy [rotation = \ldots]}} & \text{Rotation $80^\circ$ from (O, A) to (O, B)} \\
\hline
\texttt{\tkzDefPointBy [rotation = center O angle 80]} & \text{\tkzDefPointBy [rotation = center O angle -80]} \\
\hline
\texttt{\tkzDrawArc} & \text{Rotation $-80^\circ$ from (O, A) to (O, B)} \\
\hline
\texttt{\tkzFindAngle(A,O,B)} gives $80^\circ$ & \texttt{\tkzFindAngle(A,O,B)} gives $280^\circ$ \\
\hline
\end{tabular}
\end{center}

As we can see, the $-80^\circ$ rotation defines a clockwise angle but the macro \texttt{\tkzFindAngle} recovers a counterclockwise angle.

18.2. Recovering an angle \texttt{\tkzGetAngle}

\texttt{\tkzGetAngle(name of macro)}

Assigns the value in degree of an angle to a macro. The value is positive and between $0^\circ$ and $360^\circ$. This macro retrieves \texttt{\tkzAngleResult} and stores the result in a new macro.

\begin{center}
\begin{tabular}{|c|c|}
\hline
\textbf{\texttt{\tkzGetAngle(name of macro)}} & \text{example} & \text{explanation} \\
\hline
name of macro \texttt{\tkzGetAngle(ang)} & \texttt{\ang} contains the value of the angle. \\
\hline
\end{tabular}
\end{center}
This is an auxiliary macro that allows you to retrieve the result of the following macro $\texttt{tkzFindAngle}$.

### 18.3. Angle formed by three points

\begin{verbatim}
\tkzFindAngle({pt1,pt2,pt3})
\end{verbatim}

The result is stored in a macro $\texttt{tkzAngleResult}$.

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\langle pt1,pt2,pt3 \rangle$</td>
<td>$\tkzFindAngle(A,B,C)$</td>
<td>$\texttt{tkzAngleResult}$ gives the angle ($\overrightarrow{BA}, \overrightarrow{BC}$)</td>
</tr>
</tbody>
</table>

The measure is always positive and between $0^\circ$ and $360^\circ$. With the usual conventions, a counterclockwise angle smaller than a straight angle has always a measure between $0^\circ$ and $180^\circ$, while a clockwise angle smaller than a straight angle will have a measurement greater than $180^\circ$. $\texttt{tkzGetAngle}$ can retrieve the angle.

#### 18.3.1. Verification of angle measurement

\begin{tikzpicture}[scale=.75]
\tkzDefPoint(-1,1){A}
\tkzDefPoint(5,2){B}
\tkzDefEquilateral(A,B)
\tkzGetPoint{C}
\tkzDrawPolygon(A,B,C)
\tkzFindAngle(B,A,C) \tkzGetAngle{angleBAC}
\edef\angleBAC{\fpeval{round(\angleBAC)}}
\tkzDrawPoints(A,B,C)
\tkzLabelPoints(A,B)
\tkzLabelPoint[right](C){$C$}
\tkzLabelAngle(B,A,C){$\angleBAC^\circ$}
\tkzMarkAngle[size=1.5](B,A,C)
\end{tikzpicture}

#### 18.3.2. Determination of the three angles of a triangle

\begin{tikzpicture}
\tikzset{label angle style/.append style={pos=1.4}}
\tkzDefPoints{0/0/a,5/3/b,3/6/c}
\tkzDrawPolygon(a,b,c)
\tkzFindAngle(c,b,a) \tkzGetAngle{angleCBA}
\pgfmathparse{round(1+\angleCBA)}
\let\angleCBA\pgfmathresult
\tkzFindAngle(a,c,b) \tkzGetAngle{angleACB}
\pgfmathparse{round(\angleACB)}
\let\angleACB\pgfmathresult
\tkzFindAngle(b,a,c) \tkzGetAngle{angleBAC}
\pgfmathparse{round(\angleBAC)}
\let\angleBAC\pgfmathresult
\tkzMarkAngle(c,b,a)
\tkzLabelAngle(c,b,a){\tiny $\angleCBA^\circ$}
\tkzMarkAngle(a,c,b){\tiny $\angleACB^\circ$}
\tkzMarkAngle(b,a,c){\tiny $\angleBAC^\circ$}
\end{tikzpicture}
18.3.3. Angle between two circles

We are looking for the angle formed by the tangents at a point of intersection

\begin{tikzpicture}[scale=.4]
\pgfkeys{/pgf/number format/.cd, fixed, precision=1}
\tkzDefPoints{0/0/A,6/0/B,4/2/C}
\tkzDrawCircles(A,C B,C)
\tkzDefTangent[at=C](A) \tkzGetPoint{a}
\tkzDefPointsBy[symmetry = center C](a){d}
\tkzDefTangent[at=C](B) \tkzGetPoint{b}
\tkzDrawLines[add=1 and 4](a,C C,b)
\tkzFillAngle[fill=teal,opacity=.2, size=2](b,C,d)
\tkzFindAngle(b,C,d) \tkzGetAngle{bcd}
\tkzLabelAngle[pos=1.25](b,C,d){\tiny $\pgfmathprintnumber{cd}^\circ$}
\end{tikzpicture}

18.4. Angle formed by a straight line with the horizontal axis \texttt{\texttt{\tkzFindSlopeAngle}}

Much more interesting than the last one. The result is between -180 degrees and +180 degrees.

\begin{verbatim}
\tkzFindSlopeAngle((A,B))
\end{verbatim}

Determines the slope of the straight line (AB). The result is stored in a macro \texttt{\tkzAngleResult}.

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>(pt1,pt2)</td>
<td>\tkzFindSlopeAngle(A,B)</td>
<td></td>
</tr>
</tbody>
</table>

\texttt{\tkzGetAngle} can retrieve the result. If retrieval is not necessary, you can use \texttt{\tkzAngleResult}.

18.4.1. How to use \texttt{\tkzFindSlopeAngle}

The point here is that (AB) is the bisector of \overline{CAD}, such that the AD slope is zero. We recover the slope of (AB) and then rotate twice.

\begin{tikzpicture}
\tkzDefPoint(1,5){A} \tkzDefPoint(5,2){B}
\tkzFindSlopeAngle(A,B) \tkzGetAngle{tkzang}
\tkzDefPointBy[rotation= center A angle \tkzang](B)
\tkzGetPoint{C}
\tkzDefPointBy[rotation= center A angle -\tkzang](B)
\tkzGetPoint{D}
\tkzDrawSegment(A,B)
\tkzDrawSegments[new](A,C A,D)
\tkzDrawPoints(A,B,C,D)
\tkzCompass[length=1](A,C)
\tkzCompass[delta=10,brown](B,C)
\tkzLabelPoints(B,C,D)
\tkzLabelPoints[above left](A)
\end{tikzpicture}

18.4.2. Use of \texttt{\tkzFindSlopeAngle} and \texttt{\tkzGetAngle}

Here is another version of the construction of a mediator
18.4.3. Another use of \texttt{\texttt{\texttt{tkzFindSlopeAngle}}}

\begin{tikzpicture}[scale=1.5]
\tkzDefPoint(1,2){A} \tkzDefPoint(3,4){B}
\tkzDefPoint(3,2){C} \tkzDefPoint(3,1){D}
\tkzDrawSegments(A,B A,C A,D)
\tkzDrawPoints[color=red](A,B,C,D)
\tkzLabelPoints(A,B,C,D)
\tkzFindSlopeAngle(A,B) \tkzGetAngle{SAB}
\tkzFindSlopeAngle(A,C) \tkzGetAngle{SAC}
\tkzFindSlopeAngle(A,D) \tkzGetAngle{SAD}
\pgfkeys{/pgf/number format/.cd,fixed,precision=2}
\tkzText(1,5){The slope of (AB) is : $\pgfmathprintnumber{\SAB}^\circ$}
\tkzText(1,4.5){The slope of (AC) is : $\pgfmathprintnumber{\SAC}^\circ$}
\tkzText(1,4){The slope of (AD) is : $\pgfmathprintnumber{\SAD}^\circ$}
\end{tikzpicture}
19. Random point definition

At the moment there are four possibilities:

1. point in a rectangle;
2. on a segment;
3. on a straight line;
4. on a circle.

19.1. Obtaining random points

This is the new version that replaces \tkzGetRandPointOn.

\tkzDefRandPointOn\[\langle local options \rangle\]

The result is a point with a random position that can be named with the macro \tkzGetPoint. It is possible to use \tkzPointResult if it is not necessary to retain the results.

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>rectangle=pt1 and pt2</td>
<td></td>
<td>[rectangle=A and B]</td>
</tr>
<tr>
<td>segment= pt1--pt2</td>
<td></td>
<td>[segment=A--B]</td>
</tr>
<tr>
<td>line=pt1--pt2</td>
<td></td>
<td>[line=A--B]</td>
</tr>
<tr>
<td>circle =center pt1 radius dim</td>
<td></td>
<td>[circle = center A radius 2]</td>
</tr>
<tr>
<td>circle through=center pt1 through pt2</td>
<td></td>
<td>[circle through= center A through B]</td>
</tr>
<tr>
<td>disk through=center pt1 through pt2</td>
<td></td>
<td>[disk through= center A through B]</td>
</tr>
</tbody>
</table>

19.1.1. Random point in a rectangle

\begin{tikzpicture}
\tkzDefPoints{0/0/A,5/3/C}
\tkzDefRandPointOn\[rectangle = A and C\]
\tkzGetPoint{E}
\tkzDefRectangle(A,C)\tkzGetPoints{B}{D}
\tkzDrawPolygon[red](A,...,D)
\tkzDrawPoints(A,...,E)
\tkzLabelPoints(A,...,E)
\end{tikzpicture}

19.1.2. Random point on a segment or a line

\begin{tikzpicture}
\tkzDefPoints{0/0/A,5/2/C}
\tkzDefRandPointOn\[segment = A--C\]\tkzGetPoint{B}
\tkzDrawLine(A,C)
\tkzDrawPoints(A,C) \tkzDrawPoint[red](B)
\tkzLabelPoints(A,C) \tkzLabelPoints[red](B)
\end{tikzpicture}
19.1.3. Random point on a circle or a disk

\begin{tikzpicture}
\tkzDefPoints{3/2/A,1/1/B}
\tkzCalcLength(A,B) \tkzGetLength{rAB}
\tkzDefRandPointOn[circle = center A radius rAB]
\tkzGetPoint{C}
\tkzDefRandPointOn[circle through= center A through B]
\tkzGetPoint{D}
\tkzDefRandPointOn[disk through=center A through B]
\tkzGetPoint{E}
\tkzDrawCircle[R](A,rAB)
\tkzDrawPoints(A,B)
\tkzLabelPoints(A,B)
\tkzDrawPoints[red](C,D,E)
\tkzLabelPoints[red](C,D,E)
\end{tikzpicture}
Part IV.

Drawing and Filling
20. Drawing

\texttt{tkz-euclide} can draw 5 types of objects: point, line or line segment, circle, arc and sector.

\section*{20.1. Draw a point or some points}

There are two possibilities: \texttt{\tkzDrawPoint} for a single point or \texttt{\tkzDrawPoints} for one or more points.

\subsection*{20.1.1. Drawing points \texttt{\tkzDrawPoint}}

\begin{verbatim}
\tkzDrawPoint[⟨local options⟩](⟨name⟩)
\end{verbatim}

<table>
<thead>
<tr>
<th>arguments</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>name of point</td>
<td>no default</td>
<td>Only one point name is accepted</td>
</tr>
</tbody>
</table>

The argument is required. The disc takes the color of the circle, but lighter. It is possible to change everything. The point is a node and therefore it is invariant if the drawing is modified by scaling.

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>TikZ options</td>
<td>all TikZ options are valid.</td>
<td></td>
</tr>
<tr>
<td>shape</td>
<td>circle</td>
<td>Possible cross or cross out</td>
</tr>
<tr>
<td>size</td>
<td>6</td>
<td>\pgflinewidth</td>
</tr>
<tr>
<td>color</td>
<td>black</td>
<td>the default color can be changed</td>
</tr>
</tbody>
</table>

We can create other forms such as \texttt{cross}.

By default, \texttt{point style} is defined like this:

\begin{verbatim}
\tikzset{point style/.style = {
  draw = black,
  inner sep = 0pt,
  shape = circle,
  minimum size = 3 pt,
  fill = black
}}
\end{verbatim}

\subsection*{20.1.2. Example of point drawings}

Note that \texttt{scale} does not affect the shape of the dots. Which is normal. Most of the time, we are satisfied with a single point shape that we can define from the beginning, either with a macro or by modifying a configuration file.

\begin{tikzpicture}[scale=.5]
\tkzDefPoint(1,3){A}
\tkzDefPoint(4,1){B}
\tkzDefPoint(0,0){O}
\tkzDrawPoint[color=red](A)
\tkzDrawPoint[fill=blue!20,draw=blue](B)
\tkzDrawPoint[shape=cross,size=8pt,color=teal](O)
\end{tikzpicture}

It is possible to draw several points at once but this macro is a little slower than the previous one. Moreover, we have to make do with the same options for all the points.
21. Drawing the lines

The following macros are simply used to draw, name lines.

21.1. Draw a straight line

To draw a normal straight line, just give a couple of points. You can use the add option to extend the line (This option is due to Mark Wibrow, see the code below).

The style of a line is by default:

```
\tikzset{line style/.style = {
  line width = .6pt,
  color = black,
  style = solid,
  add = {.2} and {.2}
}}
```

with

```
\tikzset{%
  add/.style args={#1 and #2}{
    to path=\($!(\tikztostart)!-#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)!#1!(\tikztotarget)!-#2!(\tikztotarget)!-#1!(\tikztostart)!-#2!(\tikztostart)\to path=()\end{tikzpicture}}
```

You can modify this style with `\tkzSetUpLine` see 38.0.1
22. Drawing a segment

There is, of course, a macro to simply draw a segment.

22.1. Draw a segment \tkzDrawSegment
22. Drawing a segment

\tkzDrawSegment[⟨local options⟩](⟨pt1,pt2⟩)

The arguments are a list of two points. The styles of TiKZ are available for the drawings.

<table>
<thead>
<tr>
<th>Argument</th>
<th>Example</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>(pt1,pt2)</td>
<td>(A,B)</td>
<td>draw the segment [A,B]</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Options</th>
<th>Example</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>TikZ options</td>
<td>all TikZ options are valid.</td>
<td></td>
</tr>
<tr>
<td>dim</td>
<td>no default</td>
<td>dim = {label,dim,option}, …</td>
</tr>
<tr>
<td>…</td>
<td>…</td>
<td>allows you to add dimensions to a figure.</td>
</tr>
</tbody>
</table>

This is of course equivalent to \draw (A)--(B);. You can also use the option add.

22.1.1. Example with point references

\begin{tikzpicture}[scale=1.5]
\tkzDefPoint(0,0){A}
\tkzDefPoint(2,1){B}
\tkzDrawSegment[color=red,thin](A,B)
\tkzDrawPoints(A,B)
\tkzLabelPoints(A,B)
\end{tikzpicture}

22.1.2. Example of extending an segment with option add

\begin{tikzpicture}
\tkzDefPoints{0/0/A,6/0/B,0.8/4/C}
\tkzDefTriangleCenter[euler](A,B,C)
\tkzGetPoint{E}
\tkzDrawCircle[euler,red](A,B,C)
\tkzDrawLines[add=.5 and .5](A,B A,C B,C)
\tkzDrawPoints(A,B,C,E)
\tkzLabelPoints(A,B,C,E)
\end{tikzpicture}

22.1.3. Adding dimensions with option dim new code from Muzimuzhi Z

This code comes from an answer to this question on tex.stackexchange.com (change-color-and-style-of-dimension-lines-in-tkz-euclide). You can use now two styles: \texttt{dim style} and \texttt{dim fence style}. You have several ways to use them. I’ll let you look at the examples to see what you can do with these styles.

\tikzset{dim style/.append style={dashed}} % append if you want to keep precedent style.
22. Drawing a segment

22.1.4. Adding dimensions with option dim partI

\begin{tikzpicture}[scale=2]
  \pgfkeys{/pgf/number format/.cd, fixed, precision=2}
  \tkzDefPoint(0,0){A}
  \tkzDefPoint(3.07,0){B}
  \tkzInterCC[R]{A,2.37}(B,1.82)
  \tkzGetPoints{C}{C'}
  \tkzDrawCircle[in]{A,B,C} \tkzGetPoint{G}
  \tkzGetLength{rIn}
  \tkzDrawPolygon(A,B,C)
  \tkzDrawPoints(A,B,C)
  \tkzCalcLength(A,B) \tkzGetLength{ABl}
  \tkzCalcLength(B,C) \tkzGetLength{BCl}
  \tkzCalcLength(A,C) \tkzGetLength{ACl}
  \begin{scope}[dim style/.style={dashed,sloped,teal}]
    \tkzDrawSegment[dim={\pgfmathprintnumber\BCl,6pt,text=red}](C,B)
    \tkzDrawSegment[dim={\pgfmathprintnumber\ACl,6pt,}](A,C)
    \tkzDrawSegment[dim={\pgfmathprintnumber\ABl,-6pt,}](A,B)
  \end{scope}
  \tkzLabelPoints(A,B) \tkzLabelPoints[above](C)
\end{tikzpicture}
22. Drawing a segment

22.1.5. Adding dimensions with option dim part II

\begin{tikzpicture}[scale=.75]
  \tkzDefPoints{0/0/O,-2/0/A,2/0/B,-2/4/C,2/4/D,2/-4/E,-2/-4/F}
  \tkzDrawPolygon(C,...,F)
  \tkzDrawSegments(A,B)
  \tkzDrawPoints(A,...,F,O)
  \tkzLabelPoints(A,...,F,O)
  \tkzDrawSegment[dim={ \sqrt{5},2cm,}](C,E)
  \tkzDrawSegment[dim={ \frac{\sqrt{5}}{2},1cm,}](O,E)
  \tkzDrawSegment[dim={ 2,2cm,left=8pt}](F,C)
  \tkzDrawSegment[dim={ 1,1cm,left=8pt}](F,A)
\end{tikzpicture}

22.2. Drawing segments \texttt{\tkzDrawSegments}

If the options are the same we can plot several segments with the same macro.

\texttt{\tkzDrawSegments[(local options)]((pt1,pt2 pt3,pt4 ...))}

The arguments are a two-point couple list. The styles of TiKZ are available for the plots.

\begin{tikzpicture}
  \tkzInit[xmin=-1,xmax=3,ymin=-1,ymax=2]
  \tkzClip[space=1]
  \tkzDefPoint(0,0){A}
  \tkzDefPoint(2,1){B}
  \tkzDefPoint(3,0){C}
  \tkzDrawSegments(A,B B,C)
  \tkzDrawPoints(A,B,C)
  \tkzLabelPoints(A,C)
  \tkzLabelPoints[above](B)
\end{tikzpicture}

22.2.1. Place an arrow on segment

\begin{tikzpicture}
  \tkzSetUpStyle[postaction=decorate,
  decoration={markings, mark=at position .5 with {\arrow[thick]{#1}}}](myarrow)
  \tkzDefPoint(0,0){A}
  \tkzDefPoint(4,-4){B}
  \tkzDrawSegments[myarrow=stealth](A,B)
  \tkzDrawPoints(A,B)
\end{tikzpicture}
22.3. Drawing line segment of a triangle

22.3.1. How to draw Altitude

```
\begin{tikzpicture}[rotate=-90]
  \tkzDefPoint(0,1){A}
  \tkzDefPoint(2,4){C}
  \tkzDefPointWith[orthogonal normed,K=7](C,A)
  \tkzGetPoint{B}
  \tkzDefSpcTriangle[orthic,name=Hc](A,B,C){a,b,c}
  \tkzDrawLine[dashed,color=magenta](C,Hc)
  \tkzDrawSegment[green!60!black](A,C)
  \tkzDrawSegment[green!60!black](C,B)
  \tkzDrawSegment[green!60!black](B,A)
  \tkzLabelPoint[left](A){$A$}
  \tkzLabelPoint[right](B){$B$}
  \tkzLabelPoint[above](C){$C$}
  \tkzLabelPoint[left](Hc){$Hc$}
  \tkzLabelSegment[auto](B,A){$c$}
  \tkzLabelSegment[auto,swap](B,C){$a$}
  \tkzLabelSegment[auto,swap](C,A){$b$}
  \tkzMarkAngle[size=1,color=cyan,mark=\ ](C,B,A)
  \tkzMarkAngle[size=1,color=cyan,mark=\ ](A,C,Hc)
  \tkzMarkAngle[size=0.75, color=orange,mark=\ ||\ ||\ ||\ ](Hc,C,B)
  \tkzMarkAngle[size=0.75, color=orange,mark=\ ||\ ||\ ||\ ](B,A,C)
  \tkzMarkRightAngle(A,C,B)
  \tkzMarkRightAngle(B,Hc,C)
\end{tikzpicture}
```

22.4. Drawing a polygon

```
\tkzDrawPolygon[(local options)](points list)
```

Just give a list of points and the macro plots the polygon using the Ti\kZ options present. You can replace \((A, B, C, D, E)\) by \((A, ..., E)\) and \((P_1, P_2, P_3, P_4, P_5)\) by \((P_1, P_\ldots, P_5)\).

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>((pt1,pt2,pt3,...))</td>
<td>\tkzDrawPolygon<a href="A,B,C">gray,dashed</a></td>
<td>Drawing a triangle</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>example</th>
</tr>
</thead>
<tbody>
<tr>
<td>Options TikZ</td>
<td>...</td>
<td>\tkzDrawPolygon<a href="A,B,C">red,line width=2pt</a></td>
</tr>
</tbody>
</table>

22.4.1. \tkzDrawPolygon

```
\begin{tikzpicture} [rotate=18,scale=1]
  \tkzDefPoints{0/0/A,2.25/0.2/B,2.5/2.75/C,-0.75/2/D}
  \tkzDrawPolygon(A,B,C,D)
  \tkzDrawSegments[style=dashed](A,C B,D)
\end{tikzpicture}
```
22. Drawing a segment

22.4.2. Option two angles

\begin{tikzpicture}
\tkzDefPoint(0,0){A}
\tkzDefPoint(6,0){B}
\tkzDefTriangle[two angles = 50 and 70](A,B) \tkzGetPoint{C}
\tkzDrawPolygon(A,B,C)
\tkzLabelAngle[pos=1.4](B,A,C){$50^\circ$}
\tkzLabelAngle[pos=0.8](C,B,A){$70^\circ$}
\end{tikzpicture}

22.4.3. Style of line

\begin{tikzpicture}[scale=.6]
\tkzSetUpLine[line width=5mm,color=teal]
\tkzDefPoint(0,0){O}
\foreach \i in {0,...,5}\
{\tkzDefPoint({30+60*\i}:4){p\i}}
\tkzDefMidPoint(p1,p3) \tkzGetPoint{m1}
\tkzDefMidPoint(p3,p5) \tkzGetPoint{m3}
\tkzDefMidPoint(p5,p1) \tkzGetPoint{m5}
\tkzDrawPolygon[line join=round](p1,p3,p5)
\tkzDrawPolygon[teal!80,
line join=round](p0,p2,p4)
\tkzDrawSegments(m1,p3 m3,p5 m5,p1)
\tkzDrawCircle[teal,R](O,4.8)
\end{tikzpicture}

22.5. Drawing a polygonal chain

\verb+\tkzDrawPolySeg[(local options)]((points list))+

Just give a list of points and the macro plots the polygonal chain using the TikZ options present.

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>⟨pt1,pt2,pt3,...⟩</td>
<td>\tkzDrawPolySeg<a href="A,B,C">gray,dashed</a></td>
<td>Drawing a triangle</td>
</tr>
<tr>
<td>options</td>
<td>default</td>
<td>example</td>
</tr>
<tr>
<td>Options TikZ</td>
<td>\tkzDrawPolySeg<a href="A,B,C">red,line width=2pt</a></td>
<td></td>
</tr>
</tbody>
</table>
22.5.1. Polygonal chain

```
\begin{tikzpicture}
  \tkzDefPoints{0/0/A,6/0/B,3/4/C,2/2/D}
  \tkzDrawPolySeg(A,...,D)
  \tkzDrawPoints(A,...,D)
\end{tikzpicture}
```

22.5.2. The idea is to inscribe two squares in a semi-circle.

A Sangaku look! It is a question of proving that one can inscribe in a half-disc, two squares, and to determine the length of their respective sides according to the radius.

```
\begin{tikzpicture}[scale=.75]
  \tkzDefPoints{0/0/A,8/0/B,4/0/I}
  \tkzDefSquare(A,B) \tkzGetPoints{C}{D}
  \tkzInterLC(I,C)(I,B) \tkzGetPoints{E'}{E}
  \tkzInterLC(I,D)(I,B) \tkzGetPoints{F'}{F}
  \tkzDefPointsBy[projection=onto A--B](E,F){H,G}
  \tkzDefPointsBy[symmetry = center H](I){J}
  \tkzDefSquare(H,J) \tkzGetPoints{K}{L}
  \tkzDrawSector(I,B)(A)
  \tkzDrawPolySeg(H,E,F,G)
  \tkzDrawPolySeg(J,K,L)
  \tkzDrawPoints(E,G,H,F,J,K,L)
\end{tikzpicture}
```

22.5.3. Polygonal chain: index notation

```
\begin{tikzpicture}
  \foreach \pt in {1,2,...,8} {%
    \tkzDefPoint(\pt*20:3){P_\pt}}
  \tkzDrawPolySeg(P_1,P_...,P_8)
  \tkzDrawPoints(P_1,P_...,P_8)
\end{tikzpicture}
```

23. Draw a circle with \texttt{tkzDrawCircle}

23.1. Draw one circle

```
\tkzDrawCircle[(local options)]((A,B))
```

Tips:

- Attention you need only two points to define a radius or a diameter. An additional option \texttt{R} is available to give a measure directly.

<table>
<thead>
<tr>
<th>Arguments</th>
<th>Example</th>
<th>Explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>\texttt{(pt1,pt2)} \texttt{((A,B))}</td>
<td>two points to define a radius or a diameter</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Options</th>
<th>Default</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>\texttt{through}</td>
<td>through</td>
<td>circle with two points defining a radius</td>
</tr>
<tr>
<td>\texttt{diameter}</td>
<td>through</td>
<td>circle with two points defining a diameter</td>
</tr>
<tr>
<td>\texttt{R}</td>
<td>through</td>
<td>circle characterized by a point and the measurement of a radius</td>
</tr>
</tbody>
</table>

\texttt{tkz-euclide} \hspace{1cm} AlterMundus
23. Draw a circle with \tkzDrawCircle

Of course, you have to add all the styles of TikZ for the tracings...

23.1.1. Circles and styles, draw a circle and color the disc

We’ll see that it’s possible to colour in a disc while tracing the circle.

\begin{tikzpicture}
\tkzDefPoint(0,0){O}
\tkzDefPoint(3,0){A}
% circle with center O and passing through A
\tkzDrawCircle(O,A)
% diameter circle \([OA]\)
\tkzDrawCircle[diameter,new,%
  line width=.4pt,fill=orange!10,%,
  opacity=.5](O,A)
% circle with center O and radius = \(\exp(1)\) cm
\edef\rayon{\fpeval{0.25*\exp(1)}}
\tkzDrawCircle[R,color=orange](O,\rayon)
\end{tikzpicture}

23.2. Drawing circles

\tkzDrawCircles[\langle local options\rangle](\langle A,B,C,D \ldots\rangle)

Attention, the arguments are lists of two points. The circles that can be drawn are the same as in the previous macro. An additional option R is available to give a measure directly.

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>((pt1,pt2 pt3,pt4 \ldots)) ((A,B,C,D))</td>
<td>List of two points</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>through</td>
<td>through</td>
<td>circle with two points defining a radius</td>
</tr>
<tr>
<td>diameter</td>
<td>through</td>
<td>circle with two points defining a diameter</td>
</tr>
<tr>
<td>R</td>
<td>through</td>
<td>circle characterized by a point and the measurement of a radius</td>
</tr>
</tbody>
</table>

Of course, you have to add all the styles of TikZ for the tracings...
23. Draw a circle with \texttt{tkzDrawCircle}

23.2.1. Circles defined by a triangle.

\begin{tikzpicture}
\tkzDefPoints{0/0/A,2/0/B,3/2/C}
\tkzDrawPolygon(A,B,C)
\tkzDrawCircles(A,B,B,C,C,A)
\tkzDrawPoints(A,B,C)
\tkzLabelPoints(A,B,C)
\end{tikzpicture}

23.2.2. Concentric circles.

\begin{tikzpicture}
\tkzDefPoint(0,0){A}
\tkzDrawCircles[R](A,1 A,2 A,3)
\tkzDrawPoint(A)
\tkzLabelPoints(A)
\end{tikzpicture}
23.2.3. Exscribed circles.

\begin{tikzpicture}[scale=1]
\tkzDefPoints{0/0/A,4/0/B,1/2.5/C}
\tkzDrawPolygon(A,B,C)
\tkzDefCircle[ex](B,C,A)
\tkzGetPoint{J_c} \tkzGetSecondPoint{T_c}
\tkzGetLength{rJc}
\tkzDrawCircle[R](J_c,{rJc pt})
\tkzDrawLines[add=0 and 1](C,A C,B)
\tkzDrawSegment(J_c,T_c)
\tkzMarkRightAngle(J_c,T_c,B)
\tkzDrawPoints(A,B,C,J_c,T_c)
\end{tikzpicture}

23.2.4. Cardioid

Based on an idea by O. Reboux made with pst-eucl (PStricks module) by D. Rodriguez.
Its name comes from the Greek \textit{kardia} (heart), in reference to its shape, and was given to it by Johan Castillon (Wikipedia).

\begin{tikzpicture}[scale=.5]
\tkzDefPoint(0,0){O}
\tkzDefPoint(2,0){A}
\foreach \ang in {5,10,...,360}{{\tkzDefPoint(\ang:2){M}}
\tkzDrawCircle(M,A)}
\end{tikzpicture}
23.3. Drawing semicircle

\(\texttt{\textbackslash tkzDrawSemiCircle[\{local\ options\}](A,B)}\)

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>((pt1,pt2))</td>
<td>((O,A)) or ((A,B))</td>
<td>radius or diameter</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>through</td>
<td>through</td>
<td>circle characterized by two points defining a radius</td>
</tr>
<tr>
<td>diameter</td>
<td>through</td>
<td>circle characterized by two points defining a diameter</td>
</tr>
</tbody>
</table>

23.3.1. Use of \texttt{tkzDrawSemiCircle}

\begin{tikzpicture}
\tkzDefPoint(0,0){A} \tkzDefPoint(6,0){B}
\tkzDefSquare(A,B) \tkzGetPoints{C}{D}
\tkzDrawPolygon(B,C,D,A)
\tkzDefPoint(3,6){F}
\tkzDefTriangle[equilateral](C,D)
\tkzGetPoint{I}
\tkzDefPointBy[projection=onto B--C](I)
\tkzGetPoint{J}
\tkzInterLL(D,B)(I,J) \tkzGetPoint{K}
\tkzDefPointBy[symmetry=center K](B)
\tkzGetPoint{M}
\tkzDrawCircle(M,I)
\tkzCalcLength(M,I) \tkzGetLength{dMI}
\tkzDrawPolygon(A,B,C,D)
\tkzDrawCircle[M,dMI]
\tkzDrawSemiCircle(F,D)
\end{tikzpicture}

23.4. Drawing semicircles

\(\texttt{\textbackslash tkzDrawSemiCircles[\{local\ options\}](A,B,C,D \ldots)}\)

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>((pt1,pt2 pt3,pt4 \ldots))</td>
<td>((A,B,C,D))</td>
<td>List of two points</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>through</td>
<td>through</td>
<td>circle with two points defining a radius</td>
</tr>
<tr>
<td>diameter</td>
<td>through</td>
<td>circle with two points defining a diameter</td>
</tr>
</tbody>
</table>

24. Drawing arcs
24. Drawing arcs

\texttt{\texttt{\texttt{\texttt{tkzDrawArc}}}([\texttt{local options}])((O,...))((...))}

This macro traces the arc of center O. Depending on the options, the arguments differ. It is a question of determining a starting point and an end point. Either the starting point is given, which is the simplest, or the radius of the arc is given. In the latter case, it is necessary to have two angles. Either the angles can be given directly, or nodes associated with the center can be given to determine them. The angles are in degrees.

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>towards</td>
<td>towards</td>
<td>O is the center and the arc from A to (OB)</td>
</tr>
<tr>
<td>rotate</td>
<td>towards</td>
<td>the arc starts from A and the angle determines its length</td>
</tr>
<tr>
<td>R</td>
<td>towards</td>
<td>We give the radius and two angles</td>
</tr>
<tr>
<td>R with nodes</td>
<td>towards</td>
<td>We give the radius and two points</td>
</tr>
<tr>
<td>angles</td>
<td>towards</td>
<td>We give the radius and two points</td>
</tr>
<tr>
<td>delta</td>
<td>@</td>
<td>angle added on each side</td>
</tr>
</tbody>
</table>

Of course, you have to add all the styles of Ti\textit{k}Z for the tracings...

<table>
<thead>
<tr>
<th>options</th>
<th>arguments</th>
<th>example</th>
</tr>
</thead>
<tbody>
<tr>
<td>towards</td>
<td>(\texttt{pt,pt}) (\texttt{pt})</td>
<td>\texttt{\texttt{\texttt{\texttt{tkzDrawArc}}}<a href="(0,A)">\texttt{delta=18}</a>(B)}</td>
</tr>
<tr>
<td>rotate</td>
<td>(\texttt{pt,pt}) (\texttt{an})</td>
<td>\texttt{\texttt{\texttt{\texttt{tkzDrawArc}}}<a href="0,A">\texttt{rotate, color=red}</a>(90)}</td>
</tr>
<tr>
<td>R</td>
<td>(\texttt{pt,r}) (\texttt{an,an})</td>
<td>\texttt{\texttt{\texttt{\texttt{tkzDrawArc}}}([R])((0,2))((30,90))}</td>
</tr>
<tr>
<td>R with nodes</td>
<td>(\texttt{pt,r}) (\texttt{pt,pt})</td>
<td>\texttt{\texttt{\texttt{\texttt{tkzDrawArc}}}([R with nodes])((0,2))((A,B))}</td>
</tr>
<tr>
<td>angles</td>
<td>(\texttt{pt,pt}) (\texttt{an,an})</td>
<td>\texttt{\texttt{\texttt{\texttt{tkzDrawArc}}}([angles])((0,A))((@,90))}</td>
</tr>
</tbody>
</table>

Here are a few examples:

24.1. Option \texttt{towards}

It's useless to put \texttt{towards}. In this first example the arc starts from A and goes to B. The arc going from B to A is different. The salient is obtained by going in the direct direction of the trigonometric circle.

\begin{tikzpicture}[scale=.75]
\tkzDefPoint(0,0){O}
\tkzDefPoint(2,-1){A}
\tkzDefPointBy[rotation= center O angle 90](A)
\tkzGetPoint{B}
\tkzDrawArc[rotation, color=red](0,A)(90)
\tkzDrawArc(O,B)(A)
\tkzDrawLines(add = 0 and .5](O,A O,B)
\tkzDrawPoints(O,A,B)
\tkzLabelPoints[below](O,A,B)
\end{tikzpicture}

24.2. Option \texttt{towards}

In this one, the arc starts from A but stops on the right (OB).
24. Drawing arcs

24.3. Option \texttt{rotate}

24.4. Option \texttt{R}

24.5. Option \texttt{R with nodes}

24.6. Option \texttt{delta}

This option allows a bit like \texttt{tkzCompass} to place an arc and overflow on either side. \texttt{delta} is a measure in degrees.
24. Drawing arcs

\begin{tikzpicture}
\tkzDefPoint(0,0){A}
\tkzDefPoint(3,0){B}
\tkzDefPointBy[rotation= center A angle 60](B)
\tkzGetPoint{C}
\begin{scope}
% style only local
\tkzDefPointBy[symmetry= center C](A)
\tkzGetPoint{D}
\tkzDrawSegments(A,B A,D)
\tkzDrawLine(B,D)
\tkzSetUpCompass[color=orange]
\tkzDrawArc[orange,delta=10](A,B)(C)
\tkzDrawArc[orange,delta=10](B,C)(A)
\tkzDrawArc[orange,delta=10](C,D)(D)
\end{scope}
\tkzDrawPoints(A,B,C,D)
\tkzLabelPoints(A,B,C,D)
\tkzMarkRightAngle(D,B,A)
\end{tikzpicture}

24.7. Option angles: example 1

\begin{tikzpicture}[scale=.75]
\tkzDefPoint(0,0){A}
\tkzDefPoint(5,0){B}
\tkzDefPoint(2.5,0){O}
\tkzDefPointBy[rotation=center O angle 60](B)
\tkzGetPoint{D}
\tkzDefPointBy[symmetry=center D](O)
\tkzGetPoint{E}
\begin{scope}
\tkzDrawArc[angles](O,B)(0,180)
\tkzDrawArc[angles](B,O)(100,180)
\tkzCompass[delta=20](D,E)
\tkzDrawLines(A,B O,E B,E)
\tkzDrawPoints(A,B,O,D,E)
\end{scope}
\tkzLabelPoints(A,B,O,D,E)
\tkzMarkRightAngle(O,B,E)
\end{tikzpicture}
24.8. Option angles: example 2

\begin{tikzpicture}
\tkzDefPoint(0,0){O}
\tkzDefPoint(5,0){I}
\tkzDefPoint(0,5){J}
\tkzInterCC(O,I)(I,O)\tkzGetPoints{B}{C}
\tkzInterCC(O,I)(J,O)\tkzGetPoints(A){D}
\tkzInterCC(I,O)(J,O)\tkzGetPoints(L,K)
\tkzDrawArc[angles](O,I)(0,90)
\tkzDrawArc[angles,color=gray, style=dashed](I,O)(90,180)
\tkzDrawArc[angles,color=gray, style=dashed](J,O)(-90,0)
\tkzDrawPoints(A,B,K)
\foreach \point in {I,A,B,J,K}{\tkzDrawSegment(O,\point)}
\end{tikzpicture}

25. Drawing a sector or sectors

25.1. \texttt{tkzDrawSector}

Attention the arguments vary according to the options.

\begin{verbatim}
\tkzDrawSector[(local options)]((O,...)((...))
\end{verbatim}

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>towards</td>
<td>towards</td>
<td>O is the center and the arc from A to (OB)</td>
</tr>
<tr>
<td>rotate</td>
<td>towards</td>
<td>the arc starts from A and the angle determines its length</td>
</tr>
<tr>
<td>R</td>
<td>towards</td>
<td>We give the radius and two angles</td>
</tr>
<tr>
<td>R with nodes</td>
<td>towards</td>
<td>We give the radius and two points</td>
</tr>
</tbody>
</table>

You have to add, of course, all the styles of TikZ for tracings...

<table>
<thead>
<tr>
<th>options</th>
<th>arguments</th>
<th>example</th>
</tr>
</thead>
<tbody>
<tr>
<td>towards</td>
<td>(pt,pt)((pt))</td>
<td>\tkzDrawSector(O,A)(B)</td>
</tr>
<tr>
<td>rotate</td>
<td>(pt,pt)((an))</td>
<td>\tkzDrawSector<a href="O,A">rotate,color=red</a>(90)</td>
</tr>
<tr>
<td>R</td>
<td>(pt,r)((an,an))</td>
<td>\tkzDrawSector<a href="0,2">R,color=teal</a>(30,90)</td>
</tr>
<tr>
<td>R with nodes</td>
<td>(pt,r)((pt,pt))</td>
<td>\tkzDrawSector<a href="0,2">R with nodes</a>(A,B)</td>
</tr>
</tbody>
</table>

Here are a few examples:

25.1.1. \texttt{tkzDrawSector} and \texttt{towards}

There's no need to put \texttt{towards}. You can use \texttt{fill} as an option.
25. Drawing a sector or sectors

25.1.2. \texttt{\texttt{tkzDrawSector}} and \texttt{rotate}

\begin{tikzpicture}[scale=2]
  \tkzDefPoints{0/0/O,2/2/A,2/1/B}
  \tkzDrawSector[rotate,orange](O,A)(20)
  \tkzDrawSector[rotate,teal](O,B)(-20)
\end{tikzpicture}

25.1.3. \texttt{tkzDrawSector} and \texttt{R}

\begin{tikzpicture}[scale=1.25]
  \tkzDefPoint(0,0){O}
  \tkzDefPoint(2,-1){A}
  \tkzDrawSector[R](O,1)(30,90)
  \tkzDrawSector[R](O,1)(90,180)
  \tkzDrawSector[R](O,1)(180,270)
  \tkzDrawSector[R](O,1)(270,360)
\end{tikzpicture}

25.1.4. \texttt{tkzDrawSector} and \texttt{R} with nodes

In this example I use the option \texttt{fill} but \texttt{tkzFillSector} is possible.

\begin{tikzpicture}
  \tkzDefPoint(0,0){O}
  \tkzDefPoint(-30:1){A}
  \tkzDefPointBy[rotation = center O angle -60](A)
  \tkzDrawSector[teal](O,A)(tkzPointResult)
  \begin{scope}[shift={(-60:1)}]
    \tkzDefPoint(0,0){O}
    \tkzDefPoint(-30:1){A}
    \tkzDefPointBy[rotation = center O angle -60](A)
    \tkzDrawSector[red](O,tkzPointResult)(A)
  \end{scope}
\end{tikzpicture}
25. Drawing a sector or sectors

\begin{tikzpicture}[scale=1.25]
\tkzDefPoint(0,0){O}
\tkzDefPoint(4,-2){A}
\tkzDefPoint(4,1){B}
\tkzDefPoint(3,3){C}
\tkzDrawSector[R with nodes, fill=teal!20](O,1)(B,C)
\tkzDrawSector[R with nodes, fill=orange!20](O,1.25)(A,B)
\tkzDrawSegments(O,A O,B O,C)
\tkzDrawPoints(O,A,B,C)
\tkzLabelPoints(A,B,C)
\tkzLabelPoints[left](O)
\end{tikzpicture}

25.1.5. \tkzDrawSector and R with nodes

\begin{tikzpicture} [scale=.4]
\tkzDefPoints{-1/-2/A,1/3/B}
\tkzDefRegPolygon[side,sides=6](A,B)
\tkzGetPoint{O}
\tkzDrawPolygon[fill=black!10, draw=blue](P1,P...,P6)
\tkzLabelRegPolygon[sep=1.05](O){A,...,F}
\tkzDrawCircle[dashed](O,A)
\tkzLabelSegment[above,sloped, midway](A,B){\(A B = 16m\)}
\foreach \i [count=\xi from 1] in {2,...,6,1}
{\tkzDefMidPoint(P\xi,P\i) \path (O) to [pos=1.1] node {\xi} (tkzPointResult) ;}
\tkzDefRandPointOn[segment = P3--P5] \tkzGetPoint{S}
\tkzDrawSegments[thick,dashed,red](A,S S,B) \tkzDrawPoints(P1,P...,P6,S)
\tkzLabelPoint[above,right](S){A}
\tkzDrawSector[R with nodes,fill=red!20](S,2)(A,B)
\tkzLabelAngle[pos=1.5](A,S,B){\$\alpha\$}
\end{tikzpicture}
25. Coloring a disc
This was possible with the macro \texttt{tkzDrawCircle}, but disk tracing was mandatory, this is no longer the case.

\begin{tabular}{|c|c|}
\hline
\texttt{tkzFillCircle[(local options)]((A,B))} & options default definition \\
\hline
\texttt{radius radius two points define a radius} & \texttt{R radius a point and the measurement of a radius} \\
\hline
\end{tabular}

You don’t need to put \texttt{radius} because that’s the default option. Of course, you have to add all the styles of \textsc{TiKZ} for the plots.

25.2.1. Yin and Yang

\begin{tikzpicture} [scale=0.75]
\tkzDefPoint(0,0){O} \tkzDefPoint(-4,0){A} \tkzDefPoint(4,0){B} \tkzDefPoint(-2,0){I} \tkzDefPoint(2,0){J} \tkzDrawSector[fill=teal](O,A)(B) \tkzFillCircle[fill=white](J,B) \tkzFillCircle[fill=teal](I,A) \tkzDrawCircle(O,A)
\end{tikzpicture}

25.2.2. From a sangaku

\begin{tikzpicture}
\tkzDefPoint(0,0){B} \tkzDefPoint(6,0){C} \tkzDefSquare(B,C) \tkzGetPoints{D}{A} \tkzClipPolygon(B,C,D,A) \tkzDefMidPoint(A,D) \tkzGetPoint{F} \tkzDefMidPoint(B,C) \tkzGetPoint{E} \tkzDefMidPoint(B,D) \tkzGetPoint{Q} \tkzDefTangent[from = B](F,A) \tkzGetPoints{H}{G} \tkzInterLL(F,G)(C,D) \tkzGetPoint{J} \tkzInterLL(A,J)(F,E) \tkzGetPoint{K} \tkzDefPointBy[projection=onto B--A](K) \tkzGetPoint{M} \tkzDrawPolygon(A,B,C,D) \tkzFillCircle[red!20](E,B) \tkzFillCircle[blue!20](M,A) \tkzFillCircle[green!20](K,Q) \tkzDrawCircles(B,A M,A E,B K,Q)
\end{tikzpicture}
25.2.3. Clipping and filling part I

\begin{tikzpicture}
\tkzDefSquare(A,B) \tkzGetPoints{C}{D}
\tkzDefPointWith[colinear normed=at X,K=1](O,X) \tkzGetPoint{F}
\begin{scope}
\tkzFillCircle[fill=teal!20](O,F)
\tkzFillPolygon[white](A,...,D)
\tkzClipPolygon(A,...,D)
\foreach \c/	 in {S/C,R/B,U/A,T/D} \tkzFillCircle[teal!20](\c,\t)
\end{scope}
\foreach \c/	 in {X/C,Y/B,Z/A,W/D} \tkzFillCircle[white](\c,\t)
\foreach \c/	 in {S/C,R/B,U/A,T/D} \tkzFillCircle[teal!20](\c,\t)
\end{tikzpicture}

25.2.4. Clipping and filling part II

\begin{tikzpicture}[scale=.75]
\tkzDefPoints{0/0/A,8/0/B,8/8/C,0/8/D}
\tkzDefMidPoint(A,B) \tkzGetPoint{F}
\tkzDefMidPoint(B,C) \tkzGetPoint{E}
\tkzDefMidPoint(D,B) \tkzGetPoint{I}
\tkzDefMidPoint(I,B) \tkzGetPoint{a}
\tkzInterLC(B,I)(B,C) \tkzGetSecondPoint{K}
\tkzDefMidPoint(I,K) \tkzGetPoint{b}
\begin{scope}
\tkzFillSector[fill=blue!10](B,C)(A)
\tkzDrawSemiCircle[diameter,fill=white](A,B)
\tkzDrawSemiCircle[diameter,fill=white](B,C)
\tkzClipCircle(E,B)
\tkzClipCircle(F,B)
\tkzFillCircle[fill=blue!10](B,A)
\end{scope}
\tkzDrawSemiCircle[thick](F,B)
\tkzDrawSemiCircle[thick](E,C)
\tkzDrawArc[thick](B,C)(A)
\tkzDrawSegments[thick](A,B,C)
\tkzDrawPoints(A,B,C,E,F)
\tkzLabelPoints[centered](a,b)
\tkzLabelPoints(A,B,C,E,F)
\end{tikzpicture}
25.2.5. Clipping and filling part III

\begin{tikzpicture}
\tkzDefPoint(0,0){A} \tkzDefPoint(1,0){B}
\tkzDefPoint(2,0){C} \tkzDefPoint(-3,0){a}
\tkzDefPoint(3,0){b} \tkzDefPoint(0,3){c}
\tkzDefPoint(0,-3){d}
\begin{scope}
\tkzClipPolygon(a,b,c,d)
\tkzFillCircle[teal!20](A,C)
\end{scope}
\tkzFillCircle[white](A,B)
\tkzDrawCircle[color=red](A,C)
\tkzDrawCircle[color=red](A,B)
\end{tikzpicture}

25.3. Coloring a polygon

\tkzFillPolygon\[⟨local options⟩\](⟨points list⟩)

You can color by drawing the polygon, but in this case you color the inside of the polygon without drawing it.

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>⟨pt1,pt2,…⟩</td>
<td>⟨A,B,…⟩</td>
<td></td>
</tr>
</tbody>
</table>

25.3.1. \tkzFillPolygon

\begin{tikzpicture}[scale=.5]
\tkzDefPoint(0,0){C} \tkzDefPoint(4,0){A}
\tkzDefPoint(0,3){B}
\tkzDefSquare(B,A) \tkzGetPoints{E}{F}
\tkzDefSquare(A,C) \tkzGetPoints{G}{H}
\tkzDefSquare(C,B) \tkzGetPoints{I}{J}
\tkzFillPolygon[color = orange!30 ](A,C,G,H)
\tkzFillPolygon[color = teal!40 ](C,B,I,J)
\tkzFillPolygon[color = purple!20](B,A,E,F)
\tkzDrawPolygon[line width = 1pt](A,B,C)
\tkzDrawPolygon[line width = 1pt](A,C,G,H)
\tkzDrawPolygon[line width = 1pt](C,B,I,J)
\tkzDrawPolygon[line width = 1pt](B,A,E,F)
\tkzLabelSegment[above](C,A){$a$}
\tkzLabelSegment[right](B,C){$b$}
\tkzLabelSegment[below left](B,A){$c$}
\end{tikzpicture}

25.4. \tkzFillSector

Attention the arguments vary according to the options.
25. Drawing a sector or sectors

\begin{tabular}{|l|l|l|}
\hline
\textbf{options} & \textbf{default} & \textbf{definition} \\
\hline
towards & towards & O is the center and the arc from A to (OB) \\
rotate & towards & the arc starts from A and the angle determines its length \\
R & towards & We give the radius and two angles \\
R with nodes & towards & We give the radius and two points \\
\hline
\end{tabular}

Options default definition towards towards O is the center and the arc from A to (OB)
rotate towards the arc starts from A and the angle determines its length
R towards We give the radius and two angles
R with nodes towards We give the radius and two points

Of course, you have to add all the styles of TikZ for the tracings...

\begin{tabular}{|l|l|l|}
\hline
\textbf{options} & \textbf{arguments} & \textbf{example} \\
\hline
towards & (pt,pt)(pt) & \tkzFillSector(O,A)(B) \\
rotate & (pt,pt)(an) & \tkzFillSector[rotate, color=red](O, A)(90) \\
R & (pt,r)(an,an) & \tkzFillSector[R, color=blue](O, 2)(30, 90) \\
R with nodes & (pt,r)(pt,pt) & \tkzFillSector[R with nodes](O, 2)(A,B) \\
\hline
\end{tabular}

25.4.1. \tkzFillSector and towards

It is useless to put \texttt{towards} and you will notice that the contours are not drawn, only the surface is colored.

\begin{tikzpicture}[scale=.6]
\tkzDefPoint(0,0){O}
\tkzDefPoint(-30:3){A}
\tkzDefPointBy[rotation = center O angle -60](A)
\tkzFillSector[fill=purple!20](O,A)(tkzPointResult)
\begin{scope}[shift={(-60:1)}]
\tkzDefPoint(0,0){O}
\tkzDefPoint(-30:3){A}
\tkzDefPointBy[rotation = center O angle -60](A)
\tkzGetPoint{A'}
\tkzFillSector[color=teal!40](O,A')(A)
\end{scope}
\end{tikzpicture}

25.4.2. \tkzFillSector and rotate

\begin{tikzpicture}[scale=1.5]
\tkzDefPoint(0,0){O} \tkzDefPoint(2,2){A}
\tkzFillSector[rotate, color=purple!20](O,A)(30)
\tkzFillSector[rotate, color=teal!40](O,A)(-30)
\end{tikzpicture}

25.5. Colour an angle: \tkzFillAngle

The simplest operation

\begin{tikzpicture}[scale=.6]
\tkzDefPoint(0,0){O}
\tkzDefPoint(2,2){A}
\tkzFillAngle[fill=yellow!50](O,A)(90)
\end{tikzpicture}
25. Drawing a sector or sectors

\begin{tikzpicture}
\tkzInit
\tkzDefPoints{0/0/O,2.5/0/A,1.5/2/B}
\tkzFillAngle[size=2, fill=gray!10](A,O,B)
\tkzDrawLines(O,A O,B)
\tkzDrawPoints(O,A,B)
\end{tikzpicture}

25.5.1. Example with size

\begin{tikzpicture}
\tkzInit
\tkzDefPoints{0/0/O,2.5/0/A,1.5/2/B}
\tkzFillAngle[size=2,fill=gray!10](B,O,A)
\tkzDrawLines(O,A O,B)
\tkzDrawPoints(O,A,B)
\end{tikzpicture}

25.5.2. Changing the order of items

\begin{tikzpicture}
\tkzInit
\tkzDefPoints{0/0/O,5/0/A,3/4/B}
% Don’t forget {} to get, () to use
\tkzFillAngle[size=4,left color=white, right color=red!50](A,O,B)
\tkzDrawLines(O,A O,B)
\tkzDrawPoints(O,A,B)
\end{tikzpicture}

\tkzFillAngles[(local options)]((A',O',B'))etc.

With common options, there is a macro for multiple angles.
25.5.3. Multiples angles

\begin{tikzpicture}[scale=0.5]
\tkzDefPoints{0/0/B,8/0/C,0/8/A,8/8/D}
\tkzDrawPolygon(B,C,D,A)
\tkzDefTriangle[equilateral](B,C) \tkzGetPoint{M}
\tkzInterLL(D,M)(A,B) \tkzGetPoint{N}
\tkzDefPointBy[rotation=center N angle -60](D) \tkzGetPoint{L}
\tkzInterLL(N,L)(M,B) \tkzGetPoint{P}
\tkzInterLL(M,C)(D,L) \tkzGetPoint{Q}
\tkzDrawSegments(D,N N,L L,D B,M M,C)
\tkzDrawPoints(L,N,P,Q,M,A,D)
\tkzLabelPoints[left](N,P,Q)
\tkzLabelPoints[above](M,A,D)
\tkzLabelPoints[above](L,B,C)
\tkzMarkAngles(C,B,M B,M,C M,C,B D,L,N L,N,D N,D,L)
\tkzFillAngles[fill=red!20,opacity=.2](C,B,M% B,M,C B,D,L,N L,N,D N,D,L)
\end{tikzpicture}
26. Controlling Bounding Box

From the PgfManual: “When you add the clip option, the current path is used for clipping subsequent drawings. Clipping never enlarges the clipping area. Thus, when you clip against a certain path and then clip again against another path, you clip against the intersection of both. The only way to enlarge the clipping path is to end the pgfscope in which the clipping was done. At the end of a pgfscope the clipping path that was in force at the beginning of the scope is reinstalled.”

First of all, you don’t have to deal with TikZ the size of the bounding box. Early versions of tkz-euclide did not control the size of the bounding box, now with tkz-euclide 4 the size of the bounding box is limited.

The initial bounding box after using the macro \tkzInit is defined by the rectangle based on the points (0, 0) and (10, 10). The \tkzInit macro allows this initial bounding box to be modified using the arguments (xmin, xmax, ymin, and ymax). Of course any external trace modifies the bounding box. TikZ maintains that bounding box. It is possible to influence this behavior either directly with commands or options in TikZ such as a command like \useasboundingbox or the option use as bounding box. A possible consequence is to reserve a box for a figure but the figure may overflow the box and spread over the main text. The following command \pgfresetboundingbox clears a bounding box and establishes a new one.

26.1. Utility of \tkzInit

However, it is sometimes necessary to control the size of what will be displayed. To do this, you need to have prepared the bounding box you are going to work in, this is the role of the macro \tkzInit. For some drawings, it is interesting to fix the extreme values (xmin,xmax,ymin and ymax) and to “clip” the definition rectangle in order to control the size of the figure as well as possible.

The two macros that are useful for controlling the bounding box:

   - \tkzInit
   - \tkzClip

To this, I added macros directly linked to the bounding box. You can now view it, backup it, restore it (see the section Bounding Box).

26.2. \tkzInit

\tkzInit[⟨local options⟩]

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>xmin</td>
<td>0</td>
<td>minimum value of the abscissae in cm</td>
</tr>
<tr>
<td>xmax</td>
<td>10</td>
<td>maximum value of the abscissae in cm</td>
</tr>
<tr>
<td>xstep</td>
<td>1</td>
<td>difference between two graduations in X</td>
</tr>
<tr>
<td>ymin</td>
<td>0</td>
<td>minimum y-axis value in cm</td>
</tr>
<tr>
<td>ymax</td>
<td>10</td>
<td>maximum y-axis value in cm</td>
</tr>
<tr>
<td>ystep</td>
<td>1</td>
<td>difference between two graduations in Y</td>
</tr>
</tbody>
</table>

The role of \tkzInit is to define an orthogonal coordinates system and a rectangular part of the plane in which you will place your drawings using Cartesian coordinates. This macro allows you to define your working environment as with a calculator. With tkz-euclide 4 \xstep and \ystep are always 1. Logically it is no longer useful to use \tkzInit, except for an action like "Clipping Out".

26.3. \tkzClip
The role of this macro is to "clip" the initial rectangle so that only the paths contained in this rectangle are drawn.

\begin{tikzpicture}
\tkzInit[xmax=4, ymax=3]
\tkzDefPoints{-1/-1/A,5/2/B}
\tkzDrawX \tkzDrawY
\tkzGrid
\tkzClip
\tkzDrawSegment(A,B)
\end{tikzpicture}

It is possible to add a bit of space

\tkzClip[space=1]

26.4. \texttt{\tkzClip} and the option \texttt{space}

This option allows you to add some space around the "clipped" rectangle.

\begin{tikzpicture}
\tkzInit[xmax=4, ymax=3]
\tkzDefPoints{-1/-1/A,5/2/B}
\tkzDrawX \tkzDrawY
\tkzGrid
\tkzClip[space=1]
\tkzDrawSegment(A,B)
\end{tikzpicture}

The dimensions of the "clipped" rectangle are $x_{\text{min}} \text{-} 1$, $y_{\text{min}} \text{-} 1$, $x_{\text{max}} \text{+} 1$ and $y_{\text{max}} \text{+} 1$.

26.5. \texttt{\tkzShowBB}

The simplest macro.

\begin{tikzpicture}
\tkzInit[xmax=4, ymax=3]
\tkzDefPoints{-1/-1/A,5/2/B}
\tkzDrawX \tkzDrawY
\tkzGrid
\tkzClip[space=1]
\tkzDrawSegment(A,B)
\end{tikzpicture}

This macro displays the bounding box. A rectangular frame surrounds the bounding box. This macro accepts TikZ options.
26. Controlling Bounding Box

26.5.1. Example with \texttt{tkzShowBB}

\begin{tikzpicture}[scale=.5]
\tkzInit[ymax=5,xmax=8]
\tkzGrid
\tkzDefPoint(3,0){A}
\begin{scope}
\tkzClipBB
\tkzDrawCircle[R](A,5)
\tkzShowBB[line width = 4pt,fill=teal!10,opacity=.4]
\end{scope}
\tkzDrawCircle[R,red](A,4)
\end{tikzpicture}

26.6. \texttt{tkzClipBB}

The idea is to limit future constructions to the current bounding box.

26.6.1. Example with \texttt{tkzClipBB} and the bisectors

\begin{tikzpicture}
\tkzInit[xmin=-3,xmax=6, ymin=-1,ymax=6]
\tkzDefPoint(0,0){O}\tkzDefPoint(3,1){I}
\tkzDefPoint(1,4){J}
\tkzDefLine[bisector](I,O,J) \tkzGetPoint{i}
\tkzDefLine[bisector out](I,O,J) \tkzGetPoint{j}
\tkzDrawPoints(O,I,J,i,j)
\tkzClipBB
\tkzDrawLines[add = 1 and 2,color=orange](O,I O,J)
\tkzDrawLines[add = 1 and 2](O,i O,j)
\tkzShowBB
\end{tikzpicture}
27. Clipping different objects

27.1. Clipping a polygon

\texttt{\textbackslash tkzClipPolygon[\{local options\}](\{points list\})}

This macro makes it possible to contain the different plots in the designated polygon.

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>(pt1,pt2,pt3,...)</td>
<td>(A,B,C)</td>
<td></td>
</tr>
<tr>
<td>options</td>
<td>default</td>
<td>definition</td>
</tr>
<tr>
<td>out</td>
<td>allows to clip the outside of the object</td>
<td></td>
</tr>
</tbody>
</table>

27.1.1. \texttt{\textbackslash tkzClipPolygon}

\begin{tikzpicture}[scale=1.25]
\tkzDefPoint(0,0){A}
\tkzDefPoint(4,0){B}
\tkzDefPoint(1,3){C}
\tkzDrawPolygon(A,B,C)
\tkzDefPoint(0,2){D}
\tkzDefPoint(2,0){E}
\tkzDrawPoints(D,E)
\tkzLabelPoints(D,E)
\tkzClipPolygon(A,B,C)
\tkzDrawLine[new](D,E)
\end{tikzpicture}

27.1.2. \texttt{\textbackslash tkzClipPolygon[\textbackslash out]}

\begin{tikzpicture}[scale=1]
\tkzDefPoint(0,0){P1}
\tkzDefPoint(4,0){P2}
\tkzDefPoint(4,4){P3}
\tkzDefPoint(0,4){P4}
\tkzDefPoint(1,1){Q1}
\tkzDefPoint(3,1){Q2}
\tkzDefPoint(3,3){Q3}
\tkzDefPoint(1,3){Q4}
\tkzDrawPolygon(P1,P2,P3,P4)
\begin{scope}
\tkzClipPolygon[out](Q1,Q2,Q3,Q4)
\tkzFillPolygon[teal!20](P1,P2,P3,P4)
\end{scope}
\tkzDrawPolygon(Q1,Q2,Q3,Q4)
\end{tikzpicture}
27. Clipping different objects

27.1.3. Example: use of "Clip" for Sangaku in a square

\begin{tikzpicture}[scale=.75]
\tkzDefPoint(0,0){A} \tkzDefPoint(8,0){B}
\tkzDefSquare(A,B) \tkzGetPoints(C,D)
\tkzDefPoint(4,8){F}
\tkzDefTriangle[equilateral](C,D)
\tkzDefPointBy[projection=onto B--C](I)
\tkzDefPoint(J)
\tkzInterLL(D,B)(I,J) \tkzGetPoint{K}
\tkzDefPointBy[symmetry=center K](B)
\tkzGetPoint{M}
\tkzClipPolygon(B,C,D,A)
\tkzCalcLength(M,I) \tkzGetLength{dMI}
\tkzFillPolygon[color = orange](A,B,C,D)
\tkzFillCircle[R,color = yellow](M,dMI)
\tkzFillCircle[R,color = blue!50!black](F,4)
\end{tikzpicture}

27.2. Clipping a disc

\texttt{\tkzClipCircle[\texttt{\langle local options\rangle}](\langle A,B \rangle) \text{ or } (\langle A,r \rangle)}

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\langle A,B \rangle) or (\langle A,r \rangle)</td>
<td>(\langle A,B \rangle) or (\langle A,2cm \rangle)</td>
<td>AB radius or diameter</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>radius</td>
<td></td>
<td>circle characterized by two points defining a radius</td>
</tr>
<tr>
<td>R</td>
<td>radius</td>
<td>circle characterized by a point and the measurement of a radius</td>
</tr>
<tr>
<td>out</td>
<td></td>
<td>allows to clip the outside of the object</td>
</tr>
</tbody>
</table>

It is not necessary to put \texttt{radius} because that is the default option.

27.2.1. Simple clip

\begin{tikzpicture}[scale=.5]
\tkzDefPoint(0,0){A} \tkzDefPoint(2,2){O}
\tkzDefPoint(4,4){B} \tkzDefPoint(5,5){C}
\tkzDrawPoints(O,A,B,C)
\tkzLabelPoints(O,A,B,C)
\tkzDrawCircle(O,A)
\tkzClipCircle(O,A)
\tkzDrawCircle[fill=teal!10,opacity=.5](C,0)
\end{tikzpicture}
27. Clipping different objects

27.3. Clip out

\begin{tikzpicture}
\tkzInit[xmin=-3,ymin=-2,xmax=4,ymax=3]
\tkzDefPoint(0,0){O}
\tkzDefPoint(-4,-2){A}
\tkzDefPoint(3,1){B}
\tkzDrawCircle[R](O,2)
\tkzDrawPoints(A,B)
% to have a good bounding box
\begin{scope}
\tkzClipCircle[out,R](O,2)
\tkzDrawLines(A,B)
\end{scope}
\end{tikzpicture}

27.4. Intersection of disks

\begin{tikzpicture}
\tkzDefPoints{0/0/O,4/0/A,0/4/B}
\tkzDrawPolygon[fill=teal](O,A,B)
\tkzClipPolygon(O,A,B)
\tkzClipCircle(A,O)
\tkzClipCircle(B,O)
\tkzFillPolygon[white](O,A,B)
\end{tikzpicture}

see a more complex example about clipping here \pageref{45.6}

27.5. Clipping a sector

Attention the arguments vary according to the options.

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>towards</td>
<td>towards O is the center and the sector starts from A to (OB)</td>
<td></td>
</tr>
<tr>
<td>rotate</td>
<td>towards The sector starts from A and the angle determines its amplitude.</td>
<td></td>
</tr>
<tr>
<td>R</td>
<td>towards We give the radius and two angles</td>
<td></td>
</tr>
</tbody>
</table>

You have to add, of course, all the styles of TiKZ for tracings...

<table>
<thead>
<tr>
<th>options</th>
<th>arguments</th>
<th>example</th>
</tr>
</thead>
<tbody>
<tr>
<td>towards</td>
<td>((pt,pt))((pt))</td>
<td>\tkzClipSector(0,A)(B)</td>
</tr>
<tr>
<td>rotate</td>
<td>((pt,pt))((angle))</td>
<td>\tkzClipSector<a href="0,A">rotate</a>(90)</td>
</tr>
<tr>
<td>R</td>
<td>((pt,r))(angle 1,angle 2)</td>
<td>\tkzClipSector<a href="0,2">R</a>(38,98)</td>
</tr>
</tbody>
</table>
27. Clipping different objects

27.5.1. Example 1

\begin{tikzpicture}[scale=0.5]
\tkzDefPoint(0,0){a}
\tkzDefPoint(12,0){b}
\tkzDefPoint(4,10){c}
\tkzInterCC[R](a,6)(b,8)
\tkzGetFirstPoint{AB1} \tkzGetSecondPoint{AB2}
\tkzInterCC[R](a,6)(c,6)
\tkzGetFirstPoint{AC1} \tkzGetSecondPoint{AC2}
\tkzInterCC[R](b,8)(c,6)
\tkzGetFirstPoint{BC1} \tkzGetSecondPoint{BC2}
\tkzDrawArc(a,AB2)(AB1)
\tkzDrawArc(b,AB1)(AB2)
\tkzDrawArc(a,AC2)(AC1)
\tkzDrawArc(c,AC1)(AC2)
\tkzDrawArc(b,BC2)(BC1)
\tkzDrawArc(c,BC1)(BC2)
\begin{scope}
\tkzClipSector(b,BC2)(BC1)
\tkzFillSector[teal!40!white](c,BC1)(BC2)
\end{scope}
\begin{scope}
\tkzClipSector(a,AB2)(AB1)
\tkzFillSector[teal!40!white](b,AB1)(AB2)
\end{scope}
\begin{scope}
\tkzClipSector(a,AC2)(AC1)
\tkzFillSector[teal!40!white](c,AC1)(AC2)
\end{scope}
\end{tikzpicture}

27.5.2. Example 2

\begin{tikzpicture}[scale=1.5]
\tkzDefPoint(0,0){O}
\tkzDefPoint(2,-1){A}
\tkzDefPoint(1,1){B}
\tkzDrawSector[new,dashed](O,A)(B)
\tkzDrawSector[new](O,B)(A)
\begin{scope}
\tkzClipSector(O,B)(A)
\tkzDrawSquare[color=teal,fill=teal!20](O,B)
\end{scope}
\tkzDrawPoints(A,B,O)
\end{tikzpicture}

27.6. Options from TikZ: trim left or right

See the \texttt{pgfmanual}

27.7. TikZ Controls \texttt{pgfinterruptboundingbox} and \texttt{endpgfinterruptboundingbox}

This command temporarily interrupts the calculation of the box and configures a new box. See the \texttt{pgfmanual}
27.7.1. Example about controlling the bounding box

\begin{tikzpicture}
\tkzDefPoint(0,5){A}\tkzDefPoint(5,4){B}
\tkzDefPoint(0,0){C}\tkzDefPoint(5,1){D}
\tkzDrawSegments(A,B C,D A,C)
\pgfinterruptboundingbox
\tkzInterLL(A,B)(C,D)\tkzGetPoint{I}
\endpgfinterruptboundingbox
\tkzClipBB
\tkzDrawCircle(I,B)
\end{tikzpicture}

27.8. Reverse clip: \texttt{tkzreverseclip}

In order to use this option, a bounding box must be defined.

\begin{verbatim}
\tikzset{tkzreverseclip/.style={insert path={
    (current bounding box.south west) --(current bounding box.north west) 
    --(current bounding box.north east) -- (current bounding box.south east) 
    -- cycle}}}
\end{verbatim}

27.8.1. Example with \texttt{tkzClipPolygon[out]}

\texttt{tkzClipPolygon[out], tkzClipCircle[out]} use this option.
\fbox{\begin{tikzpicture}[scale=1]
\tkzInit[xmin=-5,xmax=5,ymin=-4,ymax=6]
\tkzClip
\tkzDefPoints{-.5/0/P1,.5/0/P2}
\foreach \i [count=\j from 3] in {2,\ldots,7}\{
  \tkzDefShiftPoint[P\i]({45*(\i-1)}:1){P\j}
\tkzClipPolygon[out](P1,P\ldots,P8)
\tkzCalcLength(P1,P5)\tkzGetLength{r}
\begin{scope}[blend group=screen]
  \foreach \i in {1,\ldots,8}\{
    \pgfmathparse{100-5*\i}
    \tkzFillCircle[R,color=teal!\pgfmathresult](P\i,\r)
  \end{scope}
\end{scope}
\end{tikzpicture}}
Part V.

Marking
27.9. Mark a segment \texttt{\textbackslash tkzMarkSegment}

\begin{verbatim}
\texttt{\textbackslash tkzMarkSegment[(local options)](pt1,pt2)}
\end{verbatim}

The macro allows you to place a mark on a segment.

\begin{center}
\begin{tabular}{ll}
\textbf{options} & \textbf{default} & \textbf{definition} \\
pos & .5 & position of the mark \\
color & black & color of the mark \\
mark & none & choice of the mark \\
size & 4pt & size of the mark \\
\end{tabular}
\end{center}

Possible marks are those provided by TikZ, but other marks have been created based on an idea by Yves Combe.

27.9.1. Several marks

\begin{verbatim}
\begin{tikzpicture}
\tkzDefPoint(2,1){A}
\tkzDefPoint(6,4){B}
\tkzDrawSegment(A,B)
\tkzMarkSegment[color=brown,size=2pt,pos=0.4, mark=z](A,B)
\tkzMarkSegment[color=blue,pos=0.2, mark=oo](A,B)
\tkzMarkSegment[pos=0.8,mark=s,color=red](A,B)
\end{tikzpicture}
\end{verbatim}

27.9.2. Use of mark

\begin{verbatim}
\begin{tikzpicture}
\tkzDefPoint(2,1){A}
\tkzDefPoint(6,4){B}
\tkzDrawSegment(A,B)
\tkzMarkSegment[color=gray,pos=0.2,mark=s|](A,B)
\tkzMarkSegment[color=gray,pos=0.4,mark=s||](A,B)
\tkzMarkSegment[color=brown,pos=0.6,mark=||](A,B)
\tkzMarkSegment[color=red,pos=0.8,mark=|||](A,B)
\end{tikzpicture}
\end{verbatim}

27.10. Marking segments \texttt{\textbackslash tkzMarkSegments}

\begin{verbatim}
\texttt{\textbackslash tkzMarkSegments[(local options)]((pt1,pt2 pt3,pt4 ...))}
\end{verbatim}

Arguments are a list of pairs of points separated by spaces. The styles of TikZ are available for plots.

27.10.1. Marks for an isosceles triangle

\begin{verbatim}
\begin{tikzpicture}[scale=1]
\tkzDefPoints{0/0/O,2/2/A,4/0/B,6/2/C}
\tkzDrawSegments(O,A,A,B)
\tkzDrawPoints(O,A,B)
\tkzMarkSegments[mark=||,size=6pt](O,A,A,B)
\end{tikzpicture}
\end{verbatim}
27.11. Another marking

\begin{tikzpicture}[scale=1]
\tkzDefPoint(0,0){A}\tkzDefPoint(3,2){B}
\tkzDefPoint(4,0){C}\tkzDefPoint(2.5,1){P}
\tkzDrawPolygon(A,B,C)
\tkzDefEquilateral(A,P) \tkzGetPoint{P'}
\tkzDefPointsBy[rotation=center A angle 60](P,B){P',C'}
\tkzDrawPolygon(A,P,P')
\tkzDrawPolySeg(P',C',A,P,B)
\tkzDrawSegment(C,P)
\tkzDrawPoints(A,B,C,C',P,P')
\tkzMarkSegments[mark=s|,size=6pt, color=blue](A,P P,P' P',A)
\tkzMarkSegments[mark=||,color=orange](B,P P',C')
\tkzLabelPoints(A,C) \tkzLabelPoints[below](P)
\tkzLabelPoints[above right](P',C',B)
\end{tikzpicture}

27.12. Mark an arc \texttt{\tkzMarkArc}

\begin{tikzpicture}
\tkzDefPoint(0,0){O}
\pgfmathsetmacro\r{2}
\tkzDefPoint(30:\r){A}
\tkzDefPoint(85:\r){B}
\tkzDrawCircle(O,A)
\tkzMarkArc[color=red,mark=||](O,A,B)
\tkzDrawPoints(B,A,O)
\end{tikzpicture}

27.13. Mark an angle mark : \texttt{\tkzMarkAngle}

More delicate operation because there are many options. The symbols used for marking in addition to those of {\LaTeX} are defined in the file {\LaTeX} and designated by the following characters:
O is the vertex. Attention the arguments vary according to the options. Several markings are possible. You can simply draw an arc or add a mark on this arc. The style of the arc is chosen with the option arc, the radius of the arc is given by mksize, the arc can, of course, be colored.

### Options

<table>
<thead>
<tr>
<th>Option</th>
<th>Default</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>arc</td>
<td>1</td>
<td>choice of l, ll and lll (single, double or triple).</td>
</tr>
<tr>
<td>size</td>
<td>1 (cm)</td>
<td>arc radius.</td>
</tr>
<tr>
<td>mark</td>
<td>none</td>
<td>choice of mark.</td>
</tr>
<tr>
<td>mksize</td>
<td>4pt</td>
<td>symbol size (mark).</td>
</tr>
<tr>
<td>mkcolor</td>
<td>black</td>
<td>symbol color (mark).</td>
</tr>
<tr>
<td>mkpos</td>
<td>.5</td>
<td>position of the symbol on the arc.</td>
</tr>
</tbody>
</table>

#### 27.13.1. Example with mark = x and with mark =||

```latex
\begin{tikzpicture}[scale=.75]
  \tkzDefPoints{0/0/O,5/0/A,3/4/B}
  \tkzMarkAngle[size = 4,mark = x,arc=ll,mkcolor = red,mkpos=.33](A,O,B)
  \tkzMarkAngle[size = 2,mark = ||,arc=ll,mkcolor = blue,mkpos=.66](A,O,B)
  \tkzDrawLines(O,A O,B)
  \tkzDrawPoints(O,A,B)
\end{tikzpicture}
```

With common options, there is a macro for multiple angles.

#### 27.14. Marking a right angle: \tkzMarkRightAngle

```latex
\tkzMarkRightAngle[(local options)]((A,O,B))((A',O',B'))etc.
```

The **german** option allows you to change the style of the drawing. The option **size** allows to change the size of the drawing.

### Options

<table>
<thead>
<tr>
<th>Option</th>
<th>Default</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>german</td>
<td>normal</td>
<td>german arc with inner point.</td>
</tr>
<tr>
<td>size</td>
<td>.2</td>
<td>side size.</td>
</tr>
</tbody>
</table>
27.14.1. Example of marking a right angle

\begin{tikzpicture}
\tkzDefPoints{0/0/A,3/1/B,0.9/-1.2/P}
\tkzDefPointBy[projection = onto B--A](P) \tkzGetPoint{H}
\tkzDrawLines[add=.5 and .5](P,H)
\tkzMarkRightAngle[fill=blue!20,size=.5,draw](A,H,P)
\tkzDrawLines[add=.5 and .5](A,B)
\tkzMarkRightAngle[fill=red!20,size=.8](B,H,P)
\tkzDrawPoints(A,B,P,H)
\end{tikzpicture}

27.14.2. Example of marking a right angle, german style

\begin{tikzpicture}
\tkzDefPoints{0/0/A,3/1/B,0.9/-1.2/P}
\tkzDefPointBy[projection = onto B--A](P) \tkzGetPoint{H}
\tkzDrawLines[add=.5 and .5](P,H)
\tkzMarkRightAngle[german,size=.5,draw](A,H,P)
\tkzDrawPoints(A,B,P,H)
\tkzDrawLines[add=.5 and .5](A,B)
\tkzMarkRightAngle[german,size=.8](P,H,B)
\end{tikzpicture}

27.14.3. Mix of styles

\begin{tikzpicture}[scale=.75]
\tkzDefPoint(0,0){A}
\tkzDefPoint(4,1){B}
\tkzDefPoint(2,5){C}
\tkzDefPointBy[projection=onto B--A](C)
\tkzGetPoint{H}
\tkzDrawLine(A,B)
\tkzDrawLine[add = .5 and .2,color=red](C,H)
\tkzMarkRightAngle[size=1,color=red](C,H,A)
\tkzMarkRightAngle[german,size=.8,color=blue](B,H,C)
\tkzFillAngle[opacity=.2,fill=blue!20,size=.8](B,H,C)
\tkzLabelPoints(A,B,C)
\tkzDrawPoints(A,B,C)
\end{tikzpicture}
27.14.4. Full example

\begin{tikzpicture}[rotate=-90]
  \tkzDefPoint(0,1){A}
  \tkzDefPoint(2,4){C}
  \tkzDefPointWith[orthogonal normed,K=7](C,A)
  \tkzGetPoint{B}
  \tkzDrawSegment[green!60!black](A,C)
  \tkzDrawSegment[green!60!black](C,B)
  \tkzDrawSegment[green!60!black](B,A)
  \tkzDefSpcTriangle[orthic](A,B,C){N,O,P}
  \tkzDrawLine[dashed,color=magenta](C,P)
  \tkzLabelPoint[left](A){$A$}
  \tkzLabelPoint[right](B){$B$}
  \tkzLabelPoint[above](C){$C$}
  \tkzLabelPoint[left](P){$P$}
  \tkzLabelSegment[auto](B,A){$c$}
  \tkzLabelSegment[auto,swap](B,C){$a$}
  \tkzLabelSegment[auto,swap](C,A){$b$}
  \tkzMarkAngle[size=1,color=cyan,mark=\|\](C,B,A)
  \tkzMarkAngle[size=1,color=cyan,mark=\|\](A,C,P)
  \tkzMarkAngle[size=0.75,color=orange,mark=\|\](P,C,B)
  \tkzMarkAngle[size=0.75,color=orange,mark=\|\](B,A,C)
  \tkzMarkRightAngle[german](A,C,B)
  \tkzMarkRightAngle[german](B,P,C)
\end{tikzpicture}

27.15. \texttt{\tkzMarkRightAngles}

\tkzMarkRightAngles[(local options)]((A,0,B))((A',0',B'))etc.

With common options, there is a macro for multiple angles.
Part VI.

Labelling
28. Labelling

28.1. Label for a point

It is possible to add several labels at the same point by using this macro several times.

\begin{tabular}{|l|l|l|}
\hline
arguments & example & \\hline
point & \texttt{\tkzLabelPoint}(A)\{\textit{$A_1$}\} & \\hline
options & default & definition \\hline
TikZ options & colour, position etc. & \\hline
\end{tabular}

Optionally, we can use any style of TikZ, especially placement with above, right, dots...

28.1.1. Example with \texttt{\tkzLabelPoint}

\begin{tikzpicture}
\tkzDefPoint(0,0){A}
\tkzDefPoint(4,0){B}
\tkzDefPoint(0,3){C}
\tkzDrawSegments(A,B B,C C,A)
\tkzDrawPoints(A,B,C)
\tkzLabelPoint[left,red](A)\{\textit{$A$}\}
\tkzLabelPoint[right,blue](B)\{\textit{$B$}\}
\tkzLabelPoint[above,purple](C)\{\textit{$C$}\}
\end{tikzpicture}

28.1.2. Label and reference

The reference of a point is the object that allows to use the point, the label is the name of the point that will be displayed.

\begin{tikzpicture}
\tkzDefPoint(2,0){A}
\tkzDrawPoint(A)
\tkzLabelPoint[above](A)\{\textit{$A_1$}\}
\end{tikzpicture}

28.2. Add labels to points \texttt{\tkzLabelPoints}

It is possible to place several labels quickly when the point references are identical to the labels and when the labels are placed in the same way in relation to the points. By default, below right is chosen.

\begin{tabular}{|l|l|l|}
\hline
arguments & example & result \\hline
list of points & \texttt{\tkzLabelPoints}(A,B,C) & Display of A, B and C \\hline
\end{tabular}

This macro reduces the number of lines of code, but it is not obvious that all points need the same label positioning.
28.2.1. Example with \tkzLabelPoints

\begin{tikzpicture}
\tkzDefPoint(2,3){A}
\tkzDefShiftPoint[A](30:2){B}
\tkzDefShiftPoint[A](30:5){C}
\tkzDrawPoints(A,B,C)
\tkzLabelPoints(A,B,C)
\end{tikzpicture}

28.3. Automatic position of labels \tkzAutoLabelPoints

The label of a point is placed in a direction defined by a center and a point \texttt{center}. The distance to the point is determined by a percentage of the distance between the center and the point. This percentage is given by \texttt{dist}.

\begin{Verbatim}
\tkzLabelPoints[\texttt{local options}](\texttt{\langle A_1, A_2, \ldots \rangle})
\end{Verbatim}

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>result</th>
</tr>
</thead>
<tbody>
<tr>
<td>list of points</td>
<td>\texttt{\tkzLabelPoint(A,B,C)}</td>
<td>Display of A, B and C</td>
</tr>
</tbody>
</table>

28.3.1. Label for points with \tkzAutoLabelPoints

Here the points are positioned relative to the center of gravity of A, B, C and O.

\begin{tikzpicture}[scale=1]
\tkzDefPoint(2,1){O}
\tkzDefRandPointOn[circle=center O radius 1.5](A)
\tkzDefPointBy[rotation=center O angle 100](A)
\tkzDefPointBy[rotation=center O angle 78](A)
\tkzDrawCircle(O,A)
\tkzDrawPoints(O,A,B,C)
\tkzDrawSegments(C,B A,B A,O)
\tkzDefCentroid(A,B,C,O)
\tkzDrawPoint(tkzPointResult)
\tkzAutoLabelPoints[center=tkzPointResult, dist=.3, red](O,A,B,C)
\end{tikzpicture}

29. Label for a segment

\begin{Verbatim}
\tkzLabelSegment[\texttt{local options}](\texttt{\langle pt1, pt2 \rangle})(\texttt{label})
\end{Verbatim}

This macro allows you to place a label along a segment or a line. The options are those of \texttt{TikZ} for example \texttt{pos}.

\begin{Verbatim}
<table>
<thead>
<tr>
<th>argument</th>
<th>example</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>label</td>
<td>\texttt{\tkzLabelSegment(A,B)}(\texttt{5})</td>
<td>label text</td>
</tr>
<tr>
<td>(pt1,pt2)</td>
<td>(A,B)</td>
<td>label along \texttt{[AB]}</td>
</tr>
<tr>
<td>options</td>
<td>default</td>
<td>definition</td>
</tr>
<tr>
<td>pos</td>
<td>.5</td>
<td>label's position</td>
</tr>
</tbody>
</table>

\texttt{tkz-euclide} AlterMundus
29.0.1. First example

\begin{tikzpicture}
\tkzDefPoint(0,0){A}
\tkzDefPoint(6,0){B}
\tkzDrawSegment(A,B)
\tkzLabelSegment[above, pos=.8](A,B){$a$}
\tkzLabelSegment[below, pos=.2](A,B){$4$}
\end{tikzpicture}

29.0.2. Example : blackboard

\begin{tikzpicture}
\tikzstyle{background rectangle}=[fill=black]
\begin{scope}[rotate=-60]
\tkzSetUpStyle[red,auto]{label seg style}
\tkzDefPoint(0,1){A}
\tkzDefPoint(2,4){C}
\tkzDefPointWith[orthogonal normed,K=7](C,A)
\tkzGetPoint{B}
\tkzDefSpcTriangle[orthic](A,B,C){N,O,P}
\tkzDefTriangleCenter[circum](A,B,C)
\tkzGetPoint{O}
\tkzDrawPolygon[green!60!black](A,B,C)
\tkzDrawLine[dashed,color=magenta](C,P)
\tkzLabelSegment(B,A){$c$}
\tkzLabelSegment[swap](B,C){$a$}
\tkzLabelSegment[swap](C,A){$b$}
\tkzMarkAngles[size=1, color=cyan, mark=||](C,B,A A,C,P)
\tkzMarkAngles[size=0.75, color=orange, mark=||](P,C,B)
\tkzMarkAngles[size=0.75, color=orange, mark=||](B,A,C)
\tkzMarkRightAngles[german](A,C,B B,P,C)
\tkzAutoLabelPoints[center = 0, dist = .1](A,B,C)
\tkzLabelPoint[below left](P){$P$}
\end{tikzpicture}
30. Add labels on a straight line \tkzLabelLine

\tkzLabelLine[\textit{local options}]{(pt1,pt2)}{(label)}

The arguments are a two-point couple list. The styles of TikZ are available for plotting.

29.0.4. Labels for an isosceles triangle

\begin{tikzpicture}[scale=1]
\tkzDefPoints{0/0/O,2/2/A,4/0/B,6/2/C}
\tkzDrawSegments(O,A A,B)
\tkzDrawPoints(O,A,B)
\tkzDrawLine(O,B)
\tkzLabelSegments[color=red,above=4pt](O,A A,B){$a$}
\end{tikzpicture}

30. Add labels on a straight line \tkzLabelLine

\tkzLabelLine[\textit{local options}]{(pt1,pt2)}{(label)}

arguments default definition

label \texttt{\tkzLabelLine(A,B)}{$\Delta$}

options default definition

\texttt{pos} .5 \texttt{pos} is an option for TikZ, but essential in this case...
As an option, and in addition to the \texttt{pos}, you can use all styles of TikZ, especially the placement with \texttt{above}, \texttt{right}, ...

30.0.1. Example with \tkzLabelLine

An important option is \texttt{pos}, it's the one that allows you to place the label along the right. The value of \texttt{pos} can be greater than 1 or negative.

\begin{tikzpicture}
\tkzDefPoints{0/0/A,3/0/B,1/1/C}
\tkzDefLine[perpendicular=through C,K=-1](A,B)
\tkzGetPoint{c}
\tkzDrawLines(A,B C,c)
\tkzLabelLine[pos=1.25,blue,right](C,c)\{again $(\delta)$
\tkzLabelLine[pos=-0.25,red,left](C,c)\{again $(\delta)$
\end{tikzpicture}

30.1. Label at an angle : \tkzLabelAngle

\tkzLabelAngle[\textit{local options}]{(A,O,B)}

There is only one option, \texttt{dist} (with or without unit), which can be replaced by the TikZ's \texttt{pos} option (without unit for the latter). By default, the value is in centimeters.
30. Add labels on a straight line \texttt{tkzLabelLine}

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>pos</td>
<td>1</td>
<td>or dist, controls the distance from the top to the label.</td>
</tr>
</tbody>
</table>

It is possible to move the label with all TikZ options: rotate, shift, below, etc.

30.1.1. Example author js bibra stackexchange

\begin{tikzpicture}[scale=.75]
\tkzDefPoint(0,0){C}
\tkzDefPoint(20:9){B}
\tkzDefPoint(80:5){A}
\tkzDefPointsBy[projection=onto B--C](A){a}
\tkzDrawPolygon[thick,fill=yellow!15](A,B,C)
\tkzDrawSegment[dashed, red](A,a)
\tkzDrawSegment[style=red, dashed, dim={$10\text{,}15pt$,midway,font=\scriptsize, rotate=90}](A,a)
\tkzMarkAngle(B,C,A)
\tkzMarkRightAngle(A,a,C)
\tkzMarkRightAngle(C,A,B)
\tkzFillAngle[fill=blue!20, opacity=0.5](B,C,A)
\tkzFillAngle[fill=red!20, opacity=0.5](A,B,C)
\tkzLabelAngle[pos=1.25](A,B,C){$\beta$}
\tkzLabelAngle[pos=1.25](B,C,A){$\alpha$}
\tkzMarkAngle(A,B,C)
\tkzDrawPoints(A,B,C)
\tkzLabelPoints(B,C)
\tkzLabelPoints[above](A)
\end{tikzpicture}

30.1.2. Example with \texttt{pos}

\begin{tikzpicture}[scale=.75]
\tkzDefPoints{0/0/O,5/0/A,3/4/B}
\tkzMarkAngle[size = 4,mark = ||, arc=ll,color = red](A,O,B)%
\tkzDrawLines(O,A O,B)
\tkzDrawPoints(O,A,B)
\tkzLabelAngle[pos=2,draw,circle, fill=blue!15](A,O,B){$\alpha$}
\end{tikzpicture}
39. Add labels on a straight line \texttt{\textbackslash{}tkzLabelLine}

\begin{tikzpicture}[rotate=30]
\tkzDefPoint(2,1){S}
\tkzDefPoint(7,3){T}
\tkzDefPointBy[rotation=center S angle 60](T)
\tkzGetPoint{P}
\tkzDefLine[bisector,normed](T,S,P)
\tkzGetPoint{s}
\tkzDrawPoints(S,T,P)
\tkzDrawPolygone[color=blue](S,T,P)
\tkzDrawLine[dashed,color=blue,add=0 and 3](S,s)
\tkzLabelPoint[above right](P){$P$}
\tkzLabelPoints(S,T)
\tkzMarkAngle[size = 1.8,mark = |,arc=ll,color = blue](T,S,P)
\tkzMarkAngle[size = 2.1,mark = |,arc=1,color = blue](T,S,s)
\tkzMarkAngle[size = 2.3,mark = |,arc=1,color = blue](s,S,P)
\tkzLabelAngles[pos = 1.5](P){$60^\circ$}
\tkzLabelAngles[pos = 2.7](P){$30^\circ$}
\end{tikzpicture}

With common options, there is a macro for multiple angles.

It finally remains to be able to give a label to designate a circle and if several possibilities are offered, we will see here \texttt{\textbackslash{}tkzLabelCircle}.

39.2. Giving a label to a circle

\begin{quote}
\begin{verbatim}
\tkzLabelAngles[(local options)]((A,O,B))((A',O',B'))etc.
\end{verbatim}
\end{quote}

With common options, there is a macro for multiple angles.

It finally remains to be able to give a label to designate a circle and if several possibilities are offered, we will see here \texttt{\textbackslash{}tkzLabelCircle}.

39.2. Giving a label to a circle

\begin{quote}
\begin{verbatim}
\tkzLabelCircle[(local options)]((A,B))((angle))((label))
\end{verbatim}
\end{quote}

You don’t need to put \texttt{radius} because that’s the default option. We can use the styles from {Ti\textit{k}Z}. The label is created and therefore “passed” between braces.
31. Label for an arc

31.0.1. Label on arc

\begin{tikzpicture}
  \tkzDefPoint(0,0){O}
  \pgfmathsetmacro{\r}{2}
  \tkzDefPoint(30:2\r){A}
  \tkzDefPoint(85:2\r){B}
  \tkzDrawCircle(O,A)
  \tkzDrawPoints(B,A,O)
  \tkzLabelArc[right=2pt](O,A,B){\widearc{AB}}
  \tkzLabelPoints(A,B,O)
\end{tikzpicture}

This macro allows you to place a label along an arc. The options are those of TikZ for example pos.

\begin{tabular}{|c|c|c|}
\hline
\textbf{argument} & \textbf{example} & \textbf{definition} \\
\hline
\textbf{label} & \tkzLabelSegment(A,B){5} & label text \\
\hdashline
\textbf{(pt1,pt2,pt3)} & \tkzDefPoint(2,0){A} & label along the arc \widearc{AB} \\
\hline
\end{tabular}

\begin{tabular}{|c|c|c|}
\hline
\textbf{options} & \textbf{default} & \textbf{definition} \\
\hline
\textbf{pos} & .5 & label's position \\
\hline
\end{tabular}

31. Label for an arc

\begin{tikzpicture}
  \tkzDefPoint(0,0){O}
  \tkzDefPoint(2,0){N}
  \tkzDefPointBy[rotation=center O angle 50](N)
  \tkzGetPoint{M}
  \tkzDefPointBy[rotation=center O angle -20](N)
  \tkzGetPoint{P}
  \tkzDefPointBy[rotation=center O angle 125](N)
  \tkzGetPoint{P'}
  \tkzLabelCircle[above=4pt](O,N)(120){\mathcal{C}}
  \tkzDrawCircle(O,M)
  \tkzFillCircle[color=blue!10,opacity=.4](O,M)
  \tkzDefPointBy[rotation=center O angle 125](N)
  \tkzGetPoint{P'}
  \tkzLabelCircle[above=4pt](O,N)(120){\mathcal{C}}
  \tkzDrawCircle(O,M)
  \tkzFillCircle[color=blue!10,opacity=.4](O,M)
  \tkzDrawPoints(M,P)
  \tkzLabelPoints[right](M,P)
\end{tikzpicture}

\tkzLabelArc[(local options)]((pt1,pt2,pt3))\{(label)\}

This macro allows you to place a label along an arc. The options are those of TikZ for example pos.

\begin{tabular}{|c|c|c|}
\hline
\textbf{argument} & \textbf{example} & \textbf{definition} \\
\hline
\textbf{label} & \tkzLabelSegment(A,B){5} & label text \\
\hdashline
\textbf{(pt1,pt2,pt3)} & \tkzDefPoint(2,0){A} & label along the arc \widearc{AB} \\
\hline
\end{tabular}

\begin{tabular}{|c|c|c|}
\hline
\textbf{options} & \textbf{default} & \textbf{definition} \\
\hline
\textbf{pos} & .5 & label's position \\
\hline
\end{tabular}

\begin{tabular}{|c|c|c|}
\hline
\textbf{label} & \tkzDefPoint(0,0){O} \tkzDefPoint(2,0){N} \pgfmathsetmacro{\r}{2} \tkzDefPoint(30:2\r){A} \tkzDefPoint(85:2\r){B} \tkzDrawCircle(O,A) \tkzDrawPoints(B,A,O) \tkzLabelArc[right=2pt](O,A,B){\widearc{AB}} \tkzLabelPoints(A,B,O) \end{tikzpicture}

\tkzLabelArc[(local options)]((pt1,pt2,pt3))\{(label)\}
Part VII.

Complements
32. Using the compass

32.1. Main macro \tkzCompass

\tkzCompass[(local options)]((A,B))

This macro allows you to leave a compass trace, i.e. an arc at a designated point. The center must be indicated. Several specific options will modify the appearance of the arc as well as TikZ options such as style, color, line thickness etc.

You can define the length of the arc with the option length or the option delta.

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>delta</td>
<td>0 (deg)</td>
<td>Increases the angle of the arc symmetrically</td>
</tr>
<tr>
<td>length</td>
<td>1 (cm)</td>
<td>Changes the length (in cm)</td>
</tr>
</tbody>
</table>

32.1.1. Option length

\begin{tikzpicture}
\tkzDefPoint(1,1){A}
\tkzDefPoint(6,1){B}
\tkzInterCC[R](A,4)(B,3)
\tkzGetPoints{C}{D}
\tkzDrawPoint(C)
\tkzCompass[length=1.5](A,C)
\tkzCompass(B,C)
\tkzDrawSegments(A,B A,C B,C)
\end{tikzpicture}

32.1.2. Option delta

\begin{tikzpicture}
\tkzDefPoint(0,0){A}
\tkzDefPoint(5,0){B}
\tkzInterCC[R](A,4)(B,3)
\tkzGetPoints{C}{D}
\tkzDrawPoints(A,B,C)
\tkzCompass[delta=20](A,C)
\tkzCompass[delta=20](B,C)
\tkzDrawPolygon(A,B,C)
\tkzMarkAngle(A,C,B)
\end{tikzpicture}

32.2. Multiple constructions \tkzCompasss

\tkzCompasss[(local options)]((pt1,pt2 pt3,pt4,...))

\begin{tikzpicture}
\tkzDefPoint(1,1){A}
\tkzDefPoint(6,1){B}
\tkzInterCC[R](A,4)(B,3)
\tkzGetPoints{C}{D}
\tkzDrawPoints(A,B,C)
\tkzCompass(A,B A,C B,C)
\end{tikzpicture}

Attention the arguments are lists of two points. This saves a few lines of code.

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>delta</td>
<td>0</td>
<td>Modifies the angle of the arc by increasing it symmetrically</td>
</tr>
<tr>
<td>length</td>
<td>1</td>
<td>Changes the length</td>
</tr>
</tbody>
</table>
32. Using the compass

\begin{tikzpicture}[scale=.75]
\tkzDefPoint(2,2){A} \tkzDefPoint(5,-2){B}
\tkzDefPoint(3,4){C} \tkzDrawPoints(A,B)
\tkzDrawPoint[shape=cross out](C)
\tkzCompasss[new](A,B A,C B,C C,B)
\tkzShowLine[mediator,new,dashed,length = 2](A,B)
\tkzShowLine[parallel = through C,
        color=purple,length=2](A,B)
\tkzDefLine[mediator](A,B)
\tkzGetPoints{i}{j}
\tkzDefLine[parallel=through C](A,B)
\tkzGetPoint{D}
\tkzDrawLines[add=.6 and .6](C,D A,C B,D)
\tkzDrawLines(i,j) \tkzDrawPoints(A,B,C,i,j,D)
\tkzLabelPoints(A,B,C,i,j,D)
\end{tikzpicture}
33. The Show

33.1. Show the constructions of some lines \texttt{\textbackslash tkzShowLine}

\begin{verbatim}
\tkzShowLine[(local options)]((pt1,pt2)) or ((pt1,pt2,pt3))
\end{verbatim}

These constructions concern mediatrices, perpendicular or parallel lines passing through a given point and bisectors. The arguments are therefore lists of two or three points. Several options allow the adjustment of the constructions. The idea of this macro comes from \textit{Yves Combe}.

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>mediator</td>
<td>mediator</td>
<td>displays the constructions of a mediator</td>
</tr>
<tr>
<td>perpendicular mediator</td>
<td>constructions for a perpendicular</td>
<td></td>
</tr>
<tr>
<td>orthogonal</td>
<td>mediator</td>
<td>idem</td>
</tr>
<tr>
<td>bisector</td>
<td>mediator</td>
<td>constructions for a bisector</td>
</tr>
<tr>
<td>K</td>
<td>1</td>
<td>circle within a triangle</td>
</tr>
<tr>
<td>length</td>
<td>1</td>
<td>in cm, length of a arc</td>
</tr>
<tr>
<td>ratio</td>
<td>.5</td>
<td>arc length ratio</td>
</tr>
<tr>
<td>gap</td>
<td>2</td>
<td>placing the point of construction</td>
</tr>
<tr>
<td>size</td>
<td>1</td>
<td>radius of an arc (see bisector)</td>
</tr>
</tbody>
</table>

You have to add, of course, all the styles of \texttt{TikZ} for tracings...

33.1.1. Example of \texttt{\textbackslash tkzLine} and parallel

\begin{tikzpicture}
\tkzDefPoints{-1.5/-0.25/A,1/-0.75/B,-1.5/2/C}
\tkzDrawLine(A,B)
\tkzDefLine[parallel=through C](A,B) \tkzGetPoint{c}
\tkzShowLine[parallel=through C](A,B)
\tkzDrawLine(C,c) \tkzDrawPoints(A,B,C,c)
\end{tikzpicture}

33.1.2. Example of \texttt{\textbackslash tkzShowLine} and perpendicular

\begin{tikzpicture}
\tkzDefPoints{0/0/A, 3/2/B, 2/2/C}
\tkzDefLine[perpendicular=through C,K=-.5](A,B) \tkzGetPoint{c}
\tkzShowLine[perpendicular=through C,K=-.5,gap=3](A,B)
\tkzDefPointBy[projection=onto A--B](c)\tkzGetPoint{h}
\tkzMarkRightAngle[fill=lightgray](A,h,C)
\tkzDrawLines[add=.5 and .5](A,B C,c)
\tkzDrawPoints(A,B,C,c)
\end{tikzpicture}
33. The Show

33.1.3. Example of \texttt{\textbackslash{}tkzShowLine} and bisector

\begin{tikzpicture}[scale=1.25]
\tkzDefPoints{0/0/A, 4/2/B, 1/4/C}
\tkzDrawPolygon(A,B,C)
\tkzSetUpCompass[color=brown,line width=.1 pt]
\tkzDefLine[bisector](B,A,C) \tkzGetPoint{a}
\tkzDefLine[bisector](C,B,A) \tkzGetPoint{b}
\tkzInterLL(A,a)(B,b) \tkzGetPoint{I}
\tkzDefPointBy[projection = onto A--B](I) \tkzGetPoint{H}
\tkzShowLine[bisector,size=2,gap=3,blue](B,A,C)
\tkzShowLine[bisector,size=2,gap=3,blue](C,B,A)
\tkzDrawCircle[radius,color=blue,line width=.2pt](I,H)
\tkzDrawSegments[color=red!50](I,tkzPointResult)
\tkzDrawLines[add=0 and -0.3,color=red!50](A,a B,b)
\tkzDrawLines[add=-0.1 and -0.1](i,j)
\tkzDrawLines(A,B)
\tkzLabelPoints[below =3pt](A,B)
\end{tikzpicture}

33.1.4. Example of \texttt{\textbackslash{}tkzShowLine} and mediator

\begin{tikzpicture}
\tkzDefPoint(2,2){A}
\tkzDefPoint(5,4){B}
\tkzDrawPoints(A,B)
\tkzShowLine[mediator,color=orange,length=1](A,B)
\tkzGetPoints{i}{j}
\tkzDrawLines[i,j]
\tkzDrawLines(A,B)
\tkzLabelPoints[below =3pt](A,B)
\end{tikzpicture}

33.2. Constructions of certain transformations \texttt{\textbackslash{}tkzShowTransformation}

\begin{verbatim}
\tkzShowTransformation[⟨local options⟩](⟨pt1,pt2⟩) or (⟨pt1,pt2,pt3⟩)
\end{verbatim}

These constructions concern orthogonal symmetries, central symmetries, orthogonal projections and translations. Several options allow the adjustment of the constructions. The idea of this macro comes from Yves Combe.

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>reflection= over pt1--pt2</td>
<td>reflection</td>
<td>constructions of orthogonal symmetry</td>
</tr>
<tr>
<td>symmetry=center pt</td>
<td>reflection</td>
<td>constructions of central symmetry</td>
</tr>
<tr>
<td>projection=onto pt1--pt2</td>
<td>reflection</td>
<td>constructions of a projection</td>
</tr>
<tr>
<td>translation=from pt1 to pt2</td>
<td>reflection</td>
<td>constructions of a translation</td>
</tr>
<tr>
<td>length</td>
<td>1</td>
<td>arc length</td>
</tr>
<tr>
<td>ratio</td>
<td>.5</td>
<td>arc length ratio</td>
</tr>
<tr>
<td>gap</td>
<td>2</td>
<td>placing the point of construction</td>
</tr>
<tr>
<td>size</td>
<td>1</td>
<td>radius of an arc (see bisector)</td>
</tr>
</tbody>
</table>

\textit{tkz-euclide} AlterMundus
\begin{tikzpicture}[scale=.6]
\tkzDefPoint(0,0){O} \tkzDefPoint(2,-2){A}
\tkzDefPoint(70:4){B} \tkzDrawPoints(A,O,B)
\tkzDrawLine[add= 2 and 2](O,A)
\tkzDefPointBy[translation=from O to A](B)
\tkzGetPoint{C}
\tkzDrawPoint[orange](C) \tkzLabelPoints(C)
\tkzShowTransformation[translation=from O to A,length=2](B)
\tkzDrawSegments[-,orange](O,A B,C)
\tkzDefPointBy[reflection=over O--A](B)
\tkzGetPoint{E}
\tkzDrawSegment[blue](B,E)
\tkzDrawPoint[blue](E)
\tkzShowTransformation[reflection=over O--A,size=2](B)
\tkzDefPointBy[symmetry=center O](B)
\tkzGetPoint{F}
\tkzDrawSegment[green](B,F)
\tkzDrawPoint[green](F)
\tkzShowTransformation[symmetry=center O,length=2](B)
\tkzDefPointBy[projection=onto O--A](C)
\tkzGetPoint{H}
\tkzDrawSegments[-,magenta](O,A H)
\tkzShowTransformation[projection=onto O--A,size=3,gap=-2](C)
\tkzDrawPoints[orange](M,N)
\tkzDrawPoints[blue](O,A,B,I)
\tkzLabelPoints(O)
\tkzLabelPoints[above right](N,I)
\tkzLabelPoints[below left](M,A)
\end{tikzpicture}
34. Protractor

Based on an idea by Yves Combe, the following macro allows you to draw a protractor. The operating principle is even simpler. Just name a half-line (a ray). The protractor will be placed on the origin $O$, the direction of the half-line is given by $A$. The angle is measured in the direct direction of the trigonometric circle.

\begin{tikzpicture}
\tkzDefPoint(2,0){A}\tkzDefPoint(0,0){O}
\tkzDefShiftPoint[A](31:5){B}
\tkzDefShiftPoint[A](158:5){C}
\tkzDrawPoints(A,B,C)
\tkzDrawSegments[color = red,\n  line width = 1pt](A,B A,C)
\tkzProtractor[scale = 1](A,B)
\end{tikzpicture}

34.1. The circular protractor

Measuring in the forward direction

\begin{tikzpicture}[scale=.5]
\tkzDefPoint(2,3){A}
\tkzDefShiftPoint[A](31:5){B}
\tkzDefShiftPoint[A](158:5){C}
\tkzDrawSegments[color = red, line width = 1pt](A,B A,C)
\tkzProtractor[return](A,C)
\end{tikzpicture}

34.2. The circular protractor, transparent and returned

\begin{tikzpicture}[scale=.5]
\tkzDefPoint(2,0){A}\tkzDefPoint(0,0){O}
\tkzDefShiftPoint[A](31:5){B}
\tkzDefShiftPoint[A](158:5){C}
\tkzDrawPoints(A,B,C)
\tkzDrawSegments[color = red, line width = 1pt](A,B A,C)
\tkzProtractor[return](A,C)
\end{tikzpicture}

\begin{tabular}{|l|l|l|}
\hline
\textbf{options} & \textbf{default} & \textbf{definition} \\
\hline
lw & 0.4 pt & line thickness \\
\hline
scale & 1 & ratio: adjusts the size of the protractor \\
\hline
return & false & trigonometric circle indirect \\
\hline
\end{tabular}
35. Miscellaneous tools

35.1. Duplicate a segment

This involves constructing a segment on a given half-line of the same length as a given segment.

\tkzDuplicateSegment\((pt1,pt2)(pt3,pt4){pt5}\)

This involves creating a segment on a given half-line of the same length as a given segment. It is in fact the definition of a point. \tkzDuplicateSegment is the new name of \tkzDuplicateLen.

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>(pt1,pt2)(pt3,pt4){pt5}</td>
<td>\tkzDuplicateSegment((A,B)(E,F){C})</td>
<td>AC=EF and C ∈ [AB)</td>
</tr>
</tbody>
</table>

The macro \tkzDuplicateLength is identical to this one.

\begin{tikzpicture}[scale=.5]
\tkzDefPoints{0/0/A,2/-3/B,2/5/C}
\tkzDuplicateSegment(A,B)(A,C)
\tkzGetPoint{D}
\tkzDrawSegments[new](A,B A,C)
\tkzDrawSegment[teal](A,D)
\tkzDrawPoints[new](A,B,C,D)
\tkzLabelPoints[above right=3pt](A,B,C,D)
\end{tikzpicture}

35.1.1. Proportion of gold with \tkzDuplicateSegment

\begin{tikzpicture}[rotate=-90,scale=.4]
\tkzDefPoints{0/0/A,10/0/B}
\tkzDefMidPoint(A,B)
\tkzGetPoint{I}
\tkzDefPointWith[orthogonal,K=-.75](B,A)
\tkzGetPoint{C}
\tkzInterLC(B,C)(B,I) \tkzGetSecondPoint{D}
\tkzDuplicateSegment(B,D)(D,A) \tkzGetPoint{E}
\tkzInterLC(A,B)(A,E) \tkzGetPoint{M}
\tkzDrawArc[orange,delta=10](D,E)(B)
\tkzDrawArc[orange,delta=10](A,M)(E)
\tkzDrawLines(A,B B,C A,D)
\tkzDrawArc[orange,delta=10](B,D)(I)
\tkzDrawPoints(A,B,D,C,M,I)
\tkzLabelPoints(A,B,D,C,M,I)
\end{tikzpicture}
35.1.2. Golden triangle or sublime triangle

\begin{tikzpicture}[scale=.75]
\tkzDefPoints{0/0/A,5/0/C,0/5/B}
\tkzDefMidPoint(A,C)\tkzGetPoint{H}
\tkzDuplicateSegment(H,B)(H,A)\tkzGetPoint{D}
\tkzDuplicateSegment(A,D)(A,B)\tkzGetPoint{E}
\tkzDuplicateSegment(A,D)(B,A)\tkzGetPoint{G}
\tkzInterCC(A,C)(B,G)\tkzGetSecondPoint{F}
\tkzDrawLine(A,C)
\tkzDrawArc(A,C)(B)
\begin{scope}[arc style/.style={color=gray,%
style=dashed}]
\tkzDrawArc(H,B)(D)
\tkzDrawArc(A,D)(B)
\tkzDrawArc(B,G)(F)
\end{scope}
\tkzDrawSegment[dashed](H,B)
\tkzCompass(B,F)
\tkzDrawPolygon[new](A,B,F)
\tkzDrawPoints(A,...,H)
\tkzLabelPoints(A,...,H)
\end{tikzpicture}

35.2. Segment length \texttt{tkzCalcLength}

There’s an option in Ti\&Z named \texttt{veclen}. This option is used to calculate \(AB\) if \(A\) and \(B\) are two points. The only problem for me is that the version of Ti\&Z is not accurate enough in some cases. My version uses the \texttt{xfp} package and is slower, but more accurate.

\texttt{\tkzCalcLength[(local options)]((pt1,pt2))}

You can store the result with the macro \texttt{tkzGetLength} for example \texttt{tkzGetLength\{dAB\}} defines the macro \texttt{\dAB}.

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\langle pt1,pt2\rangle{name of macro} \texttt{\tkzCalcLength[pt]}{A,B} \dAB)</td>
<td>\texttt{\tkzCalcLength(A,B)} After \texttt{\tkzGetLength{dAB}} \dAB\ gives AB in pt</td>
<td></td>
</tr>
</tbody>
</table>

Only one option

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>example</th>
</tr>
</thead>
<tbody>
<tr>
<td>\texttt{cm}</td>
<td>true</td>
<td>\texttt{\tkzCalcLength(A,B)} After \texttt{\tkzGetLength{dAB}} \dAB\ gives AB in cm</td>
</tr>
</tbody>
</table>
35.2.1. Compass square construction

\begin{tikzpicture}[scale=1]
\tkzDefPoint(0,0){A} \tkzDefPoint(4,0){B}
\tkzCalcLength(A,B)\tkzGetLength{dAB}
\tkzDefLine[perpendicular=through A](A,B)
\tkzGetPoint{D}
\tkzDefPointWith[orthogonal,K=-1](B,A)
\tkzGetPoint{F}
\tkzGetPoint{C}
\tkzDrawLine[add=.6 and .2](A,B)
\tkzDrawLine(A,D)
\tkzShowLine[orthogonal=through A,gap=2](A,B)
\tkzMarkRightAngle(B,A,D)
\tkzCompasss(A,D)\tkzCompasss(C)
\tkzDrawArc[R](B,dAB)(80,110)
\tkzDrawPoints(A,B,C,D)
\tkzDrawSegments[color=gray,style=dashed](B,C,C,D)
\tkzLabelPoints(A,B,C,D)
\end{tikzpicture}

35.2.2. Example

The macro \texttt{\tkzDefCircle[radius](A,B)} defines the radius that we retrieve with \texttt{\tkzGetLength}, this result is in cm.

\begin{tikzpicture}[scale=.5]
\tkzDefPoint(0,0){A}
\tkzDefPoint(3,-4){B}
\tkzDefCircle[through](A,B)
\tkzGetLength{rABcm}
\tkzDrawCircle(A,B)
\tkzDrawPoints(A,B)
\tkzLabelPoints(A,B)
\tkzDrawSegment[dashed](A,B)\pgfmathprintnumber{\rABcm}$\end{tikzpicture}$

35.3. Transformation from pt to cm or cm to pt

Not sure if this is necessary and it is only a division by 28.45274 and a multiplication by the same number. The macros are:

\texttt{\tkzpttocm((number))\{name of macro\}}

The result is stored in a macro.

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>(number){name of macro}</td>
<td>\tkzpttocm(120){len}</td>
<td>\len gives a number of \tkznamecm</td>
</tr>
</tbody>
</table>

You’ll have to use \len along with cm.
35. Miscellaneous tools

35.4. Change of unit

\tkzcmtopt{⟨number⟩}{⟨name of macro⟩}

The result is stored in a macro.

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>⟨number⟩{⟨name of macro⟩}</td>
<td>\tkzcmtopt{5}{len}</td>
<td>\len length in pts</td>
</tr>
</tbody>
</table>

The result can be used with \lenpt

35.5. Get point coordinates

\tkzGetPointCoord{⟨A⟩}{⟨name of macro⟩}

<table>
<thead>
<tr>
<th>arguments</th>
<th>example</th>
<th>explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>⟨point⟩{⟨name of macro⟩}</td>
<td>\tkzGetPointCoord{A}{A}</td>
<td>\Ax and \Ay give coordinates for A</td>
</tr>
</tbody>
</table>

Stores in two macros the coordinates of a point. If the name of the macro is p, then \px and \py give the coordinates of the chosen point with the cm as unit.

35.5.1. Coordinate transfer with \tkzGetPointCoord

\begin{tikzpicture}
\tkzInit[xmax=5,ymax=3]
\tkzGrid[sub,orange]
\tkzDrawX \tkzDrawY
\tkzDefPoint(1,0){A}
\tkzDefPoint(4,2){B}
\tkzGetPointCoord(A){a}
\tkzGetPointCoord(B){b}
\tkzDefPoint(\ax,\ay){C}
\tkzDefPoint(\bx,\by){D}
\tkzDrawPoints[color=red](C,D)
\end{tikzpicture}

35.5.2. Sum of vectors with \tkzGetPointCoord

\begin{tikzpicture}[>=latex]
\tkzDefPoint(1,4){a}
\tkzDefPoint(3,2){b}
\tkzDefPoint(1,1){c}
\tkzDrawSegment[->,red](a,b)
\tkzGetPointCoord(c){c}
\draw[color=blue,->](a) -- ([shift=(b)]cx,\cy) ;
\draw[color=purple,->](b) -- ([shift=(b)]\cx,\cy) ;
\tkzDrawSegment[->,blue](a,c)
\tkzDrawSegment[->,purple](b,c)
\end{tikzpicture}
35.6. Swap labels of points

\begin{verbatim}
\tkzDefPoints{0/0/O,5/-1/A,2/2/B}
\tkzSwapPoints(A,B)
\tkzDrawPoints(O,A,B)
\end{verbatim}

The points have exchanged their coordinates.

35.6.1. Example

```
\begin{tikzpicture}
\tkzDefPoints{0/0/O,5/-1/A,2/2/B}
\tkzSwapPoints(A,B)
\tkzDrawPoints(O,A,B)
\tkzLabelPoints(O,A,B)
\end{tikzpicture}
```
Part VIII.

Working with style
36. Predefined styles

The way to proceed will depend on your use of the package. A method that seems to me to be correct is to use as much as possible predefined styles in order to separate the content from the form. This method will be the right one if you plan to create a document (like this documentation) with many figures. We will see how to define a global style for a document. We will see how to use a style locally.

The file \texttt{tkz-euclide.cfg} contains the predefined styles of the main objects. Among these the most important are points, lines, segments, circles, arcs and compass traces. If you always use the same styles and if you create many figures then it is interesting to create your own styles. To do this you need to know what features you can modify. It will be necessary to know some notions of \textsc{TiKZ}.

The predefined styles are global styles. They exist before the creation of the figures. It is better to avoid changing them between two figures. On the other hand these styles can be modified in a figure temporarily. There the styles are defined locally and do not influence the other figures.

For the document you are reading here is how I defined the different styles.

\begin{verbatim}
\tkzSetUpColors[background=white,text=black]
\tkzSetUpPoint[size=2,color=teal]
\tkzSetUpLine[line width=.4pt,color=teal]
\tkzSetUpCompass[color=orange, line width=.4pt,delta=10]
\tkzSetUpArc[color=gray,line width=.4pt]
\tkzSetUpStyle[orange]{new}
\end{verbatim}

The macro \texttt{\tkzSetUpColors} allows you to set the background color as well as the text color. If you don't use it, the colors of your document will be used as well as the fonts. Let's see how to define the styles of the main objects.

37. Points style

This is how the points are defined:

\begin{verbatim}
\tikzset{point style/.style = {
    draw = \tkz@euc@pointcolor,
    inner sep = 0pt,
    shape = \tkz@euc@pointshape,
    minimum size = \tkz@euc@pointsize,
    fill = \tkz@euc@pointcolor}
\end{verbatim}

It is of course possible to use \texttt{\tikzset} but you can use a macro provided by the package. You can use the macro \texttt{\tkzSetUpPoint} globally or locally.

Let's look at this possibility.

37.0.1. Use of \texttt{\tkzSetUpPoint}

\begin{verbatim}
\tkzSetUpPoint[(local options)]
\end{verbatim}

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>color</td>
<td>black</td>
<td>point color</td>
</tr>
<tr>
<td>size</td>
<td>3</td>
<td>point size</td>
</tr>
<tr>
<td>fill</td>
<td>black150</td>
<td>inside point color</td>
</tr>
<tr>
<td>shape</td>
<td>circle</td>
<td>point shape circle, cross or cross out</td>
</tr>
</tbody>
</table>

\textsc{tkz-euclide}
37.8.2. Global style or local style

First of all here is a figure created with the styles of my documentation, then the style of the points is modified within the environment `tikzpicture`.

You can use the macro `\tkzSetUpPoint` globally or locally. If you place this macro in your preamble or before your first figure then the point style will be valid for all figures in your document. It will be possible to use another style locally by using this command within an environment `tikzpicture`.

Let's look at this possibility.

\begin{tikzpicture}
\tkzDefPoints{0/0/A,5/0/B,3/2/C,3/1/D}
\tkzDrawPolygon(A,B,C)
\tkzDrawPoints(A,B,C)
\tkzLabelPoints(A,B)
\tkzLabelPoints[above right](C)
\end{tikzpicture}

The style of the points is modified locally in the second figure.

\begin{tikzpicture}
\begin{scope}
\tkzSetUpPoint[size=4,color=red,fill=red!20]
\tkzDefPoints{0/0/A,5/0/B,3/2/C,3/1/D}
\tkzDrawPolygon(A,B,C)
\tkzDrawPoints(A,B,C)
\tkzDrawPoint[shape=cross out,thick](D)
\tkzLabelPoints(A,B)
\tkzLabelPoints[above right](C)
\end{scope}
\end{tikzpicture}

The points get back the initial style. Point D has a new style limited by the environment `scope`. It is also possible to use `{...}` or `begin group ... end group`.

\begin{tikzpicture}
\tkzDefPoints{0/0/A,5/0/B,3/2/C,3/1/D}
\tkzDrawPolygon(A,B,C)
\tkzDrawPoints(A,B,C)
\begin{scope}
\tkzSetUpPoint[size=4,color=red,fill=red!20]
\tkzDrawPoint(D)
\end{scope}
\tkzLabelPoints(A,B)
\tkzLabelPoints[above right](C)
\end{tikzpicture}

37.8.3. Simple example with `\tkzSetUpPoint`

\begin{tikzpicture}
\tkzSetUpPoint[shape = cross out,color=blue]
\tkzDefPoint(2,1){A}
\tkzDefPoint(4,9){B}
\tkzDrawLine(A,B)
\tkzDrawPoints(A,B)
\end{tikzpicture}
37.0.4. Use of $\texttt{tkzSetUpPoint}$ inside a group

```latex
\begin{tikzpicture}
\tkzDefPoints{0/0/A,2/4/B,4/0/C,3/2/D}
\tkzDrawSegments(A,B A,C A,D)
\tkzSetUpPoint[shape=cross out,
fill=teal!50,
size=4,color=teal]
\tkzDrawPoints(A,B)
\tkzSetUpPoint[fill=teal!50,size=4,
color=teal]
\tkzDrawPoints(C,D)
\tkzLabelPoints(A,B,C,D)
\end{tikzpicture}
```

38. Lines style

38.0.1. Use of $\texttt{tkzSetUpLine}$

It is a macro that allows you to define the style of all the lines.

<table>
<thead>
<tr>
<th>options</th>
<th>default</th>
<th>definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>color</td>
<td>black</td>
<td>colour of the construction lines</td>
</tr>
<tr>
<td>line width</td>
<td>0.4pt</td>
<td>thickness of the construction lines</td>
</tr>
<tr>
<td>style</td>
<td>solid</td>
<td>style of construction lines</td>
</tr>
<tr>
<td>add</td>
<td>.2 and .2</td>
<td>changing the length of a line segment</td>
</tr>
</tbody>
</table>

38.0.2. Change line width

```latex
\begin{tikzpicture}[scale=.75]
\tkzSetUpLine[line width=1pt]
\begin{scope}[rotate=-90]
\tkzDefPoints{0/6/A,10/0/B,10/6/C}
\tkzDefPointBy[projection = onto B--A](C)
\tkzGetPoint{H}
\tkzMarkRightAngle[size=.4,
fill=teal!20](B,C,A)
\tkzMarkRightAngle[size=.4,
fill=orange!20](B,H,C)
\tkzDrawPolygon(A,B,C)
\tkzDrawSegment[new](C,H)
\end{scope}
\tkzLabelSegment[below](C,B){$a$}
\tkzLabelSegment[right](A,C){$b$}
\tkzLabelSegment[left](A,B){$c$}
\tkzLabelSegment[color=red](C,H){$h$}
\tkzDrawPoints(A,B,C)
\tkzLabelPoints[above left](H)
\end{tikzpicture}
```
38.0.3. Change style of line

\begin{tikzpicture}[scale=.5]
\tikzset{line style/.style = {color = gray, style=dashed}}
\tkzDefPoints{1/0/A,4/0/B,1/1/C,5/1/D}
\tkzDefPoints{1/2/E,6/2/F,8/4/A',3/4/B'}
\tkzCalcLength(C,D)
\tkzCalcLength(E,F)
\tkzGetLength(rCD)
\tkzGetLength(rEF)
\tkzInterCC[R](A',rCD)(B',rEF)
\tkzGetPoints{I}{J}
\tkzDrawLine(A',B')
\tkzCompass(A',B')
\tkzDrawSegments(A,B C,D E,F)
\tkzDrawCircles[R](A',rCD) B',rEF)
\begin{scope}
\tkzSetUpLine[color=red]
\tkzDrawSegments(A',I B',I)
\end{scope}
\tkzDrawPoints(A,B,C,D,E,F,A',B',I,J)
\tkzLabelPoints(A,B,C,D,E,F,A',B',I,J)
\end{tikzpicture}

38.0.4. Example 3: extend lines

\begin{tikzpicture}[scale=.75]
\tkzSetUpLine[add=.5 and .5]
\tkzDefPoints{0/0/A,4/0/B,1/3/C}
\tkzDrawLines(A,B,B,C A,C)
\tkzDrawPolygon[red,thick](A,B,C)
\tkzSetUpPoint[size=4,circle,color=red,fill=red!20]
\tkzDrawPoints(A,B,C)
\tkzSetUpPoint[size=4,circle,color=red,fill=red!20]
\tkzDrawPoints(A,B,C)
\end{tikzpicture}

39. Arc style

\begin{tabular}{|l|l|l|}
\hline
options & default & definition \\
\hline
\textbf{color} & black & colour of the lines \\
\textbf{line width} & 0.4pt & thickness of the lines \\
\textbf{style} & solid & style of construction lines \\
\hline
\end{tabular}
40. Compass style, configuration macro \tkzSetUpCompass

The following macro will help to understand the construction of a figure by showing the compass traces necessary to obtain certain points.

\begin{tikzpicture}
\def\r{3} \def\angle{200}
\tkzSetUpArc[delta=5,color=purple,style=dashed]
\tkzSetUpLabel[font=\scriptsize,red]
\tkzDefPoint(0,0){O}
\tkzDefPoint(\angle:\r){A}
\tkzInterCC(O,A)(A,O) \tkzGetPoints{C'}{C}
\tkzInterCC(O,A)(C,O) \tkzGetPoints{D'}{D}
\tkzInterCC(O,A)(D,O) \tkzGetPoints{X'}{X}
\tkzDrawCircle(O,A)
\tkzDrawArc(A,C')(C)
\tkzDrawArc(C,O)(D)
\tkzDrawArc(D,O)(X)
\tkzDrawLine[add=.1 and .1](A,X)
\tkzDrawPoints(O,A)
\tkzDrawPoints[\new](C,C',D,X)
\tkzLabelPoints[\below left](O,A)
\tkzLabelPoints[\below right](X)
\tkzLabelPoints[\above](D)
\end{tikzpicture}

\begin{tabular}{|l|l|}
\hline
\textbf{options} & \textbf{default} & \textbf{definition} \\
\hline
color & black & colour of the construction lines \\
line width & 0.4pt & thickness of the construction lines \\
style & solid & style of lines : solid, dashed,dotted,... \\
delta & 0 & changes the length of the arc \\
\hline
\end{tabular}

40.0.1. Use of \tkzSetUpCompass

\begin{tikzpicture}
\tkzSetUpCompass[color=red,delta=15]
\tkzDefPoint(1,1){A}
\tkzDefPoint(6,1){B}
\tkzInterCC[R](A,4)(B,4) \tkzGetPoints{C}{D}
\tkzCompass(A,C)
\tkzCompass(B,C)
\tkzDrawPolygon(A,B,C)
\tkzDrawPoints(A,B,C)
\end{tikzpicture}
40.9.2. Use of \tkzSetUpCompass with \tkzShowLine

\begin{tikzpicture}[scale=.75]
\tkzSetUpStyle[bisector,size=2,gap=3]{showbi}
\tkzSetUpCompass[color=teal,line width=.3 pt]
\tkzDefPoints{0/1/A, 8/3/B, 3/6/C}
\tkzDrawPolygon(A,B,C)
\tkzDefLine[bisector](B,A,C) \tkzGetPoint{a}
\tkzDefLine[bisector](C,B,A) \tkzGetPoint{b}
\tkzShowLine[showbi](B,A,C)
\tkzShowLine[showbi](C,B,A)
\tkzInterLL(A,a)(B,b) \tkzGetPoint{I}
\tkzDefPointBy[projection= onto A--B](I)
\tkzGetPoint{H}
\tkzDrawCircle[radius,new](I,H)
\tkzDrawSegments[new](I,H)
\tkzDrawLines[add=0 and .2,new](A,I B,I)
\end{tikzpicture}

41. Label style

The macro \tkzSetUpLabel is used to define the style of the point labels.

```
\tkzSetUpLabel[\{local options\}]
```

The options are the same as those of Ti\textsc{k}Z

\begin{tikzpicture}[scale=.75]
\tkzSetUpLabel[font=\scriptsize,red]
\tkzSetUpStyle[line width=1pt,teal,<->]{XY}
\tkzInit[xmin=-3,xmax=3,ymin=-3,ymax=3]
\tkzDrawX[XY]
\tkzDrawY[XY]
\tkzDefPoints{1/0/A,0/1/B,-1/0/C,0/-1/D}
\tkzDrawPoints[teal,fill=teal!30,size=6](A,...,D)
\tkzLabelPoint[above right](A){$(1,0)$}
\tkzLabelPoint[above right](B){$(0,1)$}
\tkzLabelPoint[above left](C){$(-1,0)$}
\tkzLabelPoint[above left](D){$(0,-1)$}
\end{tikzpicture}

42. Own style

You can set your own style with \tkzSetUpStyle

```
\tkzSetUpStyle[\{local options\}]
```

The options are the same as those of Ti\textsc{k}Z
43. How to use arrows

In some countries, arrows are used to indicate the parallelism of lines, to represent half-lines or the sides of an angle (rays).
Here are some examples of how to place these arrows. \texttt{tkz-euclide} loads a library called \texttt{arrows.meta}. \usetikzlibrary{arrows.meta}
This library is used to produce different styles of arrow heads. The next examples use some of them.

43.1. Arrows at endpoints on segment, ray or line

\textbf{Stealth, Triangle, To, Latex} and …which can be combined with \texttt{reversed}. That's easy to place an arrow at one or two endpoints.

1. \texttt{Triangle} and \texttt{Ray}

\begin{tikzpicture}
\tkzDefPoints{0/0/A,4/0/B}
\tkzDrawSegment[-Triangle](A,B)
\end{tikzpicture}

2. \texttt{Stealth} and \texttt{Segment}

\begin{tikzpicture}
\tkzDefPoints{0/0/A,4/0/B}
\tkzDrawSegment[Stealth-Stealth](A,B)
\end{tikzpicture}

3. \texttt{Latex} and \texttt{Line}

\begin{tikzpicture}
\tkzDefPoints{0/0/A,4/0/B}
\tkzDrawLine[red,Latex-Latex](A,B)
\tkzDrawPoints(A,B)
\end{tikzpicture}

4. \texttt{To} and \texttt{Segment}

\begin{tikzpicture}
\tkzDefPoints{0/0/A,4/0/B}
\tkzDrawSegment[To-To](A,B)
\end{tikzpicture}

5. \texttt{Latex} and \texttt{Segment}
43. How to use arrows

6. **Latex** and **Ray**

\begin{tikzpicture}
\tkzDefPoints{0/0/A,4/0/B}
\tkzDrawSegment[Latex-Latex](A,B)
\end{tikzpicture}

7. **Latex** and **Several rays**

\begin{tikzpicture}
\tkzDefPoints{0/0/A,4/0/B,5/-2/C}
\tkzDrawSegments[-Latex](A,B A,C)
\end{tikzpicture}

43.1.1. **Scaling an arrow head**

\begin{tikzpicture}
\tkzDefPoints{0/0/A,4/0/B}
\tkzDrawSegment[Latex[scale=2]-{Latex[scale=2]}](A,B)
\end{tikzpicture}

43.1.2. **Using vector style**

\tikzset{vector style/.style={>=Latex,->}}
You can redefine this style.

\begin{tikzpicture}
\tkzDefPoints{0/0/A,4/0/B}
\tkzDrawSegment[vector style](A,B)
\end{tikzpicture}

43.2. **Arrows on middle point of a line segment**

Arrows on lines are used to indicate that those lines are parallel. It depends on the country, in France we prefer to indicate outside the figure that \((A, B) \parallel (D, C)\). The code is an adaptation of an answer by muzimuzhi Z on the site tex.stackexchange.com.

Syntax:

- \texttt{tkz arrow (Latex by default)}
- \texttt{tkz arrow=<arrow end tip>}
- \texttt{tkz arrow=<arrow end tip> at <pos> (\texttt{<pos> = .5 by default})}
- \texttt{tkz arrow=<arrow end tip>[<arrow options>] at <pos>} option possible \texttt{scale}

Example usages:
43. How to use arrows

\tkzDrawSegment[tkz arrow=Stealth] (A,B)
\tkzDrawSegment[tkz arrow={To[scale=3] at .4}] (A,B)
\tkzDrawSegment[tkz arrow={Latex[scale=5,blue] at .6}] (A,B)

43.2.1. In a parallelogram

\begin{tikzpicture}
\tkzDefPoints{0/0/A,3/0/B,4/2/C}
\tkzDefParallelogram(A,B,C)
\tkzGetPoint{D}
\tkzDrawSegments[tkz arrow](A,B,D,C)
\tkzDrawSegments(B,C,D,A)
\tkzLabelPoints(A,B)
\tkzLabelPoints[above right](C,D)
\tkzDrawPoints(A,...,D)
\end{tikzpicture}

43.2.2. A line parallel to another one

\begin{tikzpicture}
\tkzDefPoints{0/0/A,3/0/B,1/2/C}
\tkzDefPointWith[colinear= at C](A,B)
\tkzGetPoint{D}
\tkzDrawSegments[tkz arrow=Triangle](A,B,C,D)
\tkzLabelPoints(A,B,C)
\tkzDrawPoints(A,...,C)
\end{tikzpicture}

43.2.3. Arrow on a circle

It is possible to place an arrow on the first quarter of a circle. A rotation allows you to move the arrow.

\begin{tikzpicture}
\tkzDefPoints{0/0/A,3/0/B}
\begin{scope}[rotate=150]
\tkzDrawCircle[tkz arrow={Latex[scale=2,red]}](A,B)
\end{scope}
\end{tikzpicture}

43.3. Arrows on all segments of a polygon

Some users of my package have asked me to be able to place an arrow on each side of a polygon. I used a style proposed by Paul Gaborit on the site tex.stackexchange.com.

\tikzset{tkz arrows/.style=
{postaction={on each path={tkz arrow={Latex[scale=2,color=black]}}}}}

You can change this style. With \texttt{tkz arrows} you can an arrow on each segment of a polygon
43. How to use arrows

43.3.1. Arrow on each segment with \texttt{tkz arrows}

\begin{tikzpicture}
\tkzDefPoints{0/0/A,3/0/B}
\tkzDefSquare(A,B) \tkzGetPoints{C}{D}
\tkzDrawPolygon[tkz arrows](A,...,D)
\end{tikzpicture}

43.3.2. Using \texttt{tkz arrows} with a circle

\begin{tikzpicture}
\tkzDefPoints{0/0/A,3/0/B}
\tkzDrawCircle[tkz arrows](A,B)
\end{tikzpicture}
Part IX.

Examples
44. Different authors

44.1. Code from Andrew Swan

\begin{tikzpicture}[scale=1.25]
\def\radius{4}
\def\angle{40}
\pgfmathsetmacro{\htan}{tan(\angle)}
\tkzDefPoint(0,0){A} \tkzDefPoint(0,\radius){F}
\tkzDefPoint(\radius,0){B}
\tkzDefPointBy[rotation= center A angle \angle](B)
\tkzGetPoint(C)
\tkzDefLine[perpendicular=through B,k=1](A,B)
\tkzGetPoint(b)
\tkzInterLL(A,C)(B,b) \tkzGetPoint(D)
\tkzDefLine[perpendicular=through C,k=-1](A,B)
\tkzGetPoint(c)
\tkzInterLL(C,c)(A,B) \tkzGetPoint(E)
\tkzDrawSector[fill=blue,opacity=.1](A,B)(C)
\tkzDrawArc[thin](A,B)(F)
\tkzMarkAngle(B,A,C)
\tkzLabelAngle[pos=0.8](B,A,C){$x$}
\tkzDrawPolygon(A,B,D)
\tkzDrawSegments(C,B)
\tkzDrawSegments[dashed,thin](C,E)
\tkzLabelPoints[below left](A)
\tkzLabelPoints[below right](B)
\tkzLabelPoints[above](C)
\tkzLabelPoints[above right](D)
\begin{scope}[/pgf/decoration/raise=5pt]
\draw [decorate,decoration={brace,mirror, amplitude=10pt},xshift=6pt,yshift=-1pt]
(A) -- (B) node [black,midway,yshift=-20pt]
{\footnotesize $1$};
\draw [decorate,decoration={brace,amplitude=10pt},
xshift=4pt,yshift=8pt]
(D) -- (B) node [black,midway,xshift=27pt]
{\footnotesize $\tan x$};
\draw [decorate,decoration={brace,amplitude=10pt},
xshift=4pt,yshift=8pt]
(E) -- (C) node [black,midway,xshift=-27pt]
{\footnotesize $\sin x$};
\end{scope}
\end{tikzpicture}

44.2. Example: Dimitris Kapeta

You need in this example to use \texttt{mkpos=.2} with \texttt{tkzMarkAngle} because the measure of $\widehat{CAB}$ is too small. Another possibility is to use \texttt{tkzFillAngle}.
44. Different authors

\begin{tikzpicture}[scale=1]
\tkzDefPoint(0,0){O}
\tkzDefPoint(2.5,0){N}
\tkzDefPoint(-4.2,0.5){M}
\tkzDefPointBy[rotation=center O angle 30](N)
\tkzGetPoint{B}
\tkzDefPointBy[rotation=center O angle -50](N)
\tkzGetPoint{A}
\tkzInterLC(M,B)(O,N) \tkzGetFirstPoint{C}
\tkzInterLC(M,A)(O,N) \tkzGetSecondPoint{A'}
\tkzMarkAngle[mkpos=.2, size=0.5](A,C,B)
\tkzMarkAngle[mkpos=.2, size=0.5](A,M,C)
\tkzDrawSegments(A,C M,A M,B)
\tkzDrawCircle(O,N)
\tkzLabelCircle[above left](O,N)(120){\mathcal{C}}
\begin{scope}[xfp]
\tkzMarkAngle[mkpos=.2, size=1.2](C,A,M)
\end{scope}
\tkzDrawPoints(O, A, B, M, B, C)
\tkzLabelPoints[right](O,A,B)
\tkzLabelPoints[above left](M,C)
\tkzLabelPoint[below left](A'){$A'$}
\end{tikzpicture}

44.3. Example: John Kitzmiller

Prove that \(\frac{AC}{CE} = \frac{BD}{DF}\).

Another interesting example from John, you can see how to use some extra options like \texttt{decoration} and \texttt{postaction} from Ti\kern-0.05em\kern-0.05emkZ with \texttt{tkz-euclide}.

\begin{tikzpicture}[scale=1]
\tkzDefPoints{0/0/O, 2/0/N, -4/0.5/M, 0/2/C, 0/0.5/A, 2.5/0/B, -4.2/0.5/M, 0/2/C}
\tkzDrawPoints(O, A, B, M, B, C)
\tkzLabelPoints[right](O,A,B)
\tkzLabelPoints[above left](M,C)
\tkzLabelPoint[below left](A'){$A'$}
\end{tikzpicture}
44. Different authors

44.4. Example 1: from Indonesia

\begin{tikzpicture}[scale=1.5, decoration={markings, mark=at position 3cm with {\arrow[scale=2]{>}}},]
\tkzDefPoints{0/0/E, 6/0/F, 0/1.8/P, 6/1.8/Q, 0/3/R, 6/3/S}
\tkzDrawLines[postaction={decorate}](E,F P,Q R,S)
\tkzDefPoints{3.5/3/A, 5/3/B}
\tkzDrawSegments(E,A F,B)
\tkzInterLL(E,A)(P,Q) \tkzGetPoint{C}
\tkzInterLL(B,F)(P,Q) \tkzGetPoint{D}
\tkzLabelPoints[above right](A,B)
\tkzLabelPoints[below](E,F)
\tkzLabelPoints[above left](C)
\tkzDrawSegments[style=dashed](A,F)
\tkzInterLL(A,F)(P,Q) \tkzGetPoint{G}
\tkzLabelPoints[above right](D,G)
\tkzDrawSegments[color=teal, line width=3pt, opacity=0.4](A,C A,G)
\tkzDrawSegments[color=magenta, line width=3pt, opacity=0.4](C,E G,F)
\tkzDrawSegments[color=teal, line width=3pt, opacity=0.4](B,D)
\tkzDrawSegments[color=magenta, line width=3pt, opacity=0.4](D,F)
\end{tikzpicture}
44. Different authors

\begin{tikzpicture}[scale=3]
  \tkzDefPoints{0/0/A,2/0/B}
  \tkzDefSquare(A,B) \tkzGetPoints{C}{D}
  \tkzDefPointBy[rotation=center D angle 45](C)\tkzGetPoint{G}
  \tkzDefSquare(G,D)\tkzGetPoints{E}{F}
  \tkzInterLL(B,C)(E,F)\tkzGetPoint{H}
  \tkzFillPolygon[gray!10](D,E,H,C,D)
  \tkzDrawPolygon(A,...,D)\tkzDrawPolygon(D,...,G)
  \tkzDrawSegment(B,E)
  \tkzMarkSegments[mark=|,size=3pt,color=gray](A,B B,C C,D D,A E,F F,G G,D D,E)
  \tkzMarkSegments[mark=||,size=3pt,color=gray](B,E E,H)
  \tkzLabelPoints[left](A,D)
  \tkzLabelPoints[right](B,C,F,H)
  \tkzLabelPoints[above](G)\tkzLabelPoints[below](E)
  \tkzMarkRightAngles(D,A,B D,G,F)
\end{tikzpicture}

44.5. Example 2: from Indonesia
44. Different authors

\begin{tikzpicture}
\pol/.style={fill=brown!40,opacity=.5},
\seg/.style={tkzdotted, color=gray}, hidden pt/.style={fill=gray!40},
mra/.style={color=gray!70, tkzdotted, /tkzrightangle/size=.2, scale=1.5}
\tkzDefPoints{0/0/A, 2.5/0/B, 1.33/0.75/D, 0/2.5/E, 2.5/2.5/F}
\tkzDefLine[parallel=through D](A,B) \tkzGetPoint{I1}
\tkzDefLine[parallel=through B](A,D) \tkzGetPoint{I2}
\tkzDefLine[parallel=through E](A,D) \tkzGetPoint{I3}
\tkzDefLine[parallel=through D](A,E) \tkzGetPoint{I4}
\tkzDefLine[parallel=through F](E,H) \tkzGetPoint{I5}
\tkzDefLine[parallel=through H](E,F) \tkzGetPoint{I6}
\tkzDefLine[parallel=through I3](A,D) \tkzGetPoint{I7}
\tkzDefLine[parallel=through I4](A,E) \tkzGetPoint{I8}
\tkzDefMidPoint(G,H) \tkzGetPoint{P}
\tkzDefMidPoint(B,C) \tkzGetPoint{R}
\tkzDefMidPoint(A,B) \tkzGetPoint{S}
\tkzDefMidPoint(A,D) \tkzGetPoint{M}
\tkzDefMidPoint(D,C) \tkzGetPoint{N}
\tkzDefMidPoint(E,H) \tkzGetPoint{U}
\tkzDefMidPoint(E,F) \tkzGetPoint{V}
\tkzDefMidPoint(E,H) \tkzGetPoint{U}
\tkzDefMidPoint(E,F) \tkzGetPoint{V}
\tkzDefMidPoint(G,H) \tkzGetPoint{Q}
\tkzDefLine[parallel=through K](D,H) \tkzGetPoint{I9}
\tkzDefLine[parallel=through I7](B,D) \tkzGetPoint{O}
\tkzDefMidPoint(G,H) \tkzGetPoint{Q}
\tkzFillPolygon[pol](P,Q,R,S,T,U)
\tkzDrawSegments[seg](K,O,L,P,Q,R,S,T,U,C,D,H,D,A,D,M,N,B,D)
\tkzDrawPolygon(A,B,F,E)
\tkzDrawPoints[hidden pt](M,N,O,D)
\tkzDrawPoints[hidden pt](M,N,O,D)
\tkzMarkRightAngle[mra](L,O,K)
\tkzMarkSegments[mark=|,size=1pt, thick, color=gray](A,S,B,S,B,R,C,R)
\tkzLabelAngle[pos=.3](K,L,O){\$\alpha\$}
\tkzLabelPoints{above left}(U,D,M) \tkzLabelPoints{above right}(L,N)
\end{tikzpicture}
44.6. Illustration of the Morley theorem by Nicolas François

\begin{tikzpicture}
\tkzInit[ymin=-3,ymax=5,xmin=-5,xmax=7]
\tkzClip
\tkzDefPoints{-2.5/-2/A,2/4/B,5/-1/C}
\tkzFindAngle(C,A,B) \tkzGetAngle{anglea}
\tkzDefPointBy[rotation=center A angle 1*anglea/3](C) \tkzGetPoint{TA1}
\tkzDefPointBy[rotation=center A angle 2*anglea/3](C) \tkzGetPoint{TA2}
\tkzDefPointBy[rotation=center B angle 1*angleb/3](A) \tkzGetPoint{TB1}
\tkzDefPointBy[rotation=center B angle 2*angleb/3](A) \tkzGetPoint{TB2}
\tkzDefPointBy[rotation=center C angle 1*anglec/3](B) \tkzGetPoint{TC1}
\tkzDefPointBy[rotation=center C angle 2*anglec/3](B) \tkzGetPoint{TC2}
\tkzInterLL(A,TA1)(B,TB2) \tkzGetPoint{U1}
\tkzInterLL(A,TA2)(B,TB1) \tkzGetPoint{V1}
\tkzInterLL(B,TA2)(C,TC1) \tkzGetPoint{U2}
\tkzInterLL(B,TA1)(C,TC2) \tkzGetPoint{V2}
\tkzInterLL(C,TC1)(A,TA2) \tkzGetPoint{U3}
\tkzInterLL(C,TC2)(A,TA1) \tkzGetPoint{V3}
\tkzDrawPolygons(A,B,C U1,U2,U3 V1,V2,V3)
\tkzDrawLines[add=2 and 2,very thin,dashed](A,TA1 B,TB1 C,TC1 A,TA2 B,TB2 C,TC2)
\tkzDrawPoints(U1,U2,U3,V1,V2,V3)
\tkzLabelPoint[left](V1){$s_a$} \tkzLabelPoint[right](V2){$s_b$}
\tkzLabelPoint[below](V3){$s_c$} \tkzLabelPoint[above left](A){$a$}
\tkzLabelPoints[above right](B,C) \tkzLabelPoint(U1){$t_a$}
\tkzLabelPoint[below left](U2){$t_b$} \tkzLabelPoint[above](U3){$t_c$}
\end{tikzpicture}
Pythagoras was not the first person who discovered this theorem around the world. Ancient China discovered this theorem much earlier than him. So there is another name for the Pythagorean theorem in China, the Gou-Gu theorem. Zhao Shuang was an ancient Chinese mathematician. He rediscovered the “Gou gu theorem”, which is actually the Chinese version of the “Pythagorean theorem”. Zhao Shuang used a method called the “cutting and compensation principle”, he created a picture of “Pythagorean Round Square” Below the figure used to illustrate the proof of the “Gou gu theorem.” (code from Nan Geng)
44.8. Reuleaux-Triangle

A well-known classic field of mathematics is geometry. You may know Euclidean geometry from school, with constructions by compass and ruler. Math teachers may be very interested in drawing geometry constructions and explanations. Underlying constructions can help us with general drawings where we would need intersections and tangents of lines and circles, even if it does not look like geometry. So, here, we will remember school geometry drawings. We will use the tkz-euclide package, which works on top of TikZ. We will construct an equilateral triangle. Then we extend it to get a Reuleaux triangle, and add annotations. The code is fully explained in the LaTeX Cookbook, Chapter 10, Advanced Mathematics, Drawing geometry pictures. Stefan Kottwitz

\begin{tikzpicture}
\tkzDefPoint(0,0){A} \tkzDefPoint(4,1){B}
\tkzInterCC(A,B)(B,A) \tkzGetPoints{C}{D}
\tkzInterLC(A,B)(B,A) \tkzGetPoints{E}{F}
\tkzDrawCircles[dashed](A,B B,A)
\tkzDrawPolygons(A,B,C A,E,D)
\tkzCompass[color=red, very thick](A,C B,C A,D B,D)
\begin{scope}
\tkzSetUpArc[thick,delta=0]
\tkzDrawArc[fill=blue!10](A,B)(C)
\tkzDrawArc[fill=blue!10](B,C)(A)
\tkzDrawArc[fill=blue!10](C,A)(B)
\end{scope}
\tkzMarkAngles(D,A,E A,E,D)
\tkzMarkRightAngle[size=0.65,fill=red!20,opacity=0.2](A,D,E)
\tkzLabelAngle[draw pos=0.65,pos=0.7](D,A,E){\$\alpha\$}
\tkzLabelAngle[draw pos=0.65,pos=0.8](A,E,D){\$\beta\$}
\end{tikzpicture}
45. Some interesting examples

45.1. Square root of the integers

How to get 1, \sqrt{2}, \sqrt{3} with a rule and a compass.

\begin{tikzpicture}
\tkzDefPoint(0,0){O}
\tkzDefPoint(1,0){a0}
\tkzDrawSegment(O,a0)
\foreach \i in {0,...,16}{
\tkzDefPointWith[orthogonal normed](a\i,O)
\tkzGetPoint{a\j}
\pgfmathsetmacro{\c}{5*\i}
\tkzDrawPolySeg[fill=teal!\c](a\i,a\j,O)}
\end{tikzpicture}

45.2. About right triangle

We have a segment [AB] and we want to determine a point C such that AC = 8 cm and ABC is a right triangle in B.

\begin{tikzpicture}[scale=.5]
\tkzDefPoint["A" left](2,1){A}
\tkzDefPoint["B" right](6,4){B}
\tkzDefPointWith[orthogonal,K=-1](B,A)
\tkzDrawLine[add = .5 and .5](B,tkzPointResult)
\tkzInterLC[R](B,tkzPointResult)(A,8)
\tkzGetPoints{J}{C}
\tkzDrawSegment(A,B)
\tkzDrawPoints(A,B,C)
\tkzCompass(A,C)
\tkzMarkRightAngle(A,B,C)
\tkzDrawLine[color=gray,style=dashed](A,C)
\tkzLabelPoint[above](C){$C$}
\end{tikzpicture}
45.3. Archimedes

This is an ancient problem proved by the great Greek mathematician Archimedes. The figure below shows a semicircle, with diameter $AB$. A tangent line is drawn and touches the semicircle at $B$. An other tangent line at a point, $C$, on the semicircle is drawn. We project the point $C$ on the line segment $[AB]$ on a point $D$. The two tangent lines intersect at the point $T$. Prove that the line $(AT)$ bisects $(CD)$.

\begin{tikzpicture}[scale=1]
\tkzDefPoint(0,0){A}\tkzDefPoint(6,0){D}
\tkzDefPoint(8,0){B}\tkzDefPoint(4,0){I}
\tkzDefLine[orthogonal=through D](A,D)
\tkzInterLC[R](D,tkzPointResult)(I,4) \tkzGetSecondPoint{C}
\tkzDefLine[orthogonal=through C](I,C) \tkzGetPoint{c}
\tkzDefLine[orthogonal=through B](A,B) \tkzGetPoint{b}
\tkzInterLL(C,c)(B,b) \tkzGetPoint{T}
\tkzInterLL(A,T)(C,D) \tkzGetPoint{P}
\tkzDrawArc(I,B)(A)
\tkzDrawSegments(A,B,A,T,C,D,I,C) \tkzDrawSegment[new](I,C)
\tkzDrawLine[add = 1 and 0](C,T) \tkzDrawLine[add = 0 and 1](B,T)
\tkzMarkRightAngle(I,C,T)
\tkzDrawPoints(A,B,I,D,C,T)
\tkzLabelPoints(A,B,I,D) \tkzLabelPoints[above right](C,T)
\tkzMarkSegment[mark=s|](C,D) \tkzMarkSegment[mark=s|](C,D)
\end{tikzpicture}
45.3.1. Square and rectangle of same area; Golden section

To construct Square and rectangle of same area.

\begin{tikzpicture}[scale=.75]
\tkzDefPoint(0,0){D} \tkzDefPoint(8,0){A} \\
\tkzDefSquare(D,A) \tkzGetPoints{B}{C} \\
\tkzDefMidPoint(D,A) \tkzGetPoint{E} \\
\tkzInterLC(D,A)(E,B)\tkzGetSecondPoint{F} \\
\tkzInterLC(A,B)(A,F)\tkzGetSecondPoint{G} \\
\tkzDefSquare(A,F)\tkzGetFirstPoint{H} \\
\tkzInterLL(C,D)(H,G)\tkzGetPoint{I} \\
\tkzFillPolygon[teal!10](I,G,B,C) \\
\tkzFillPolygon[teal!10](A,F,H,G) \\
\tkzDrawArc[angles](E,B)(0,120) \\
\tkzDrawSemiCircle(A,F) \\
\tkzDrawSegments(A,F E,B H,I F,H) \\
\tkzDrawPolygons(A,B,C,D) \\
\tkzDrawPoints(A,...,I) \\
\tkzLabelPoints(A,...,I) \\
\end{tikzpicture}
45.3.2. Steiner Line and Simson Line

Consider the triangle ABC and a point M on its circumcircle. The projections of M on the sides of the triangle are on a line (Steiner Line). The three closest points to M on lines AB, AC, and BC are collinear. It's the Simson Line.

\begin{tikzpicture}[scale=.75,rotate=-20]
\tkzDefPoint(0,0){B} \tkzDefPoint(2,4){A} \tkzDefPoint(7,0){C}
\tkzDefCircle[circum](A,B,C) \tkzGetPoint{O}
\tkzDrawCircle(O,A) \tkzCalcLength(O,A) \tkzGetLength{rOA}
\tkzDefShiftPoint[O](40:40:O){M}
\tkzDefShiftPoint[O](60:60:O){N}
\tkzDefTriangleCenter[orthic](A,B,C) \tkzGetPoint{H}
\tkzDefSpcTriangle[orthic,name=H](A,B,C){a,b,c}
\tkzDefPointsBy[reflection=over A--B](M,N){P,P'}
\tkzDefPointsBy[reflection=over A--C](M,N){Q,Q'}
\tkzDefPointsBy[reflection=over C--B](M,N){R,R'}
\tkzDefMidPoint(M,P) \tkzGetPoint{I}
\tkzDefMidPoint(M,Q) \tkzGetPoint{J}
\tkzDefMidPoint(M,R) \tkzGetPoint{K}
\tkzDrawSegments(P,R M,P M,Q M,R N,P' P' R' R' I,K)
\tkzDrawPolygons(A,B,C)
\end{tikzpicture}
45. Some interesting examples

45.4. Lune of Hippocrates

From wikipedia: In geometry, the lune of Hippocrates, named after Hippocrates of Chios, is a lune bounded by arcs of two circles, the smaller of which has as its diameter a chord spanning a right angle on the larger circle. In the first figure, the area of the lune is equal to the area of the triangle ABC. Hippocrates of Chios (ancient Greek mathematician,)

\begin{tikzpicture}
\tkzInit[xmin=-2,xmax=5,ymin=-1,ymax=6]
\tkzClip
\tkzDefPoint(0,0){A}\tkzDefPoint(4,0){B}
\tkzDefSquare(A,B)
\tkzGetFirstPoint{C}
\tkzDrawPolygon[fill=green!5](A,B,C)
\begin{scope}
\tkzClipCircle[out](B,A)
\tkzDrawSemiCircle[diameter,fill=teal!5](A,C)
\end{scope}
\tkzDrawArc[delta=0](B,C)(A)
\end{tikzpicture}

45.5. Lunes of Hasan Ibn al-Haytham

From wikipedia: the Arab mathematician Hasan Ibn al-Haytham (Latinized name Alhazen) showed that two lunes, formed on the two sides of a right triangle, whose outer boundaries are semicircles and whose inner boundaries are formed by the circumcircle of the triangle, then the areas of these two lunes added together are equal to the area of the triangle. The lunes formed in this way from a right triangle are known as the lunes of Alhazen.

\begin{tikzpicture}[scale=.5,rotate=180]
\tkzInit[xmin=-1,xmax=11,ymin=-4,ymax=7]
\tkzClip
\tkzDefPoints{0/0/A,8/0/B}
\tkzDefTriangle[pythagore,swap](A,B)
\tkzGetPoint{C}
\tkzDrawPolygon[fill=green!5](A,B,C)
\tkzDefMidPoint(C,A) \tkzGetPoint{I}
\begin{scope}
\tkzClipCircle[out](I,A)
\tkzDrawSemiCircle[diameter,fill=teal!5](B,A)
\tkzDrawSemiCircle[diameter,fill=teal!5](C,B)
\end{scope}
\tkzSetUpCompass[/tkzcompass/delta=0]
\tkzDrawSemiCircle[diameter](C,A)
\end{tikzpicture}
45.6. About clipping circles

The problem is the management of the bounding box. First you have to define a rectangle in which the figure will be inserted. This is done with the first two lines.

```latex
\begin{tikzpicture}
  \tkzInit[xmin=0,xmax=6,ymin=0,ymax=6]
  \tkzClip
  \tkzDefPoints{0/0/A, 6/0/B}
  \tkzDefSquare(A,B) \tkzGetPoints{C}{D}
  \tkzDefMidPoint(A,B) \tkzGetPoint{M}
  \tkzDefMidPoint(A,D) \tkzGetPoint{N}
  \tkzDefMidPoint(B,C) \tkzGetPoint{O}
  \tkzDefMidPoint(C,D) \tkzGetPoint{P}

  \begin{scope}
    \tkzClipCircle[\text{out}](M,B) \tkzClipCircle[\text{out}](P,D)
    \tkzFillPolygon[teal!20](M,N,P,O)
  \end{scope}

  \begin{scope}
    \tkzClipCircle[\text{out}](N,A) \tkzClipCircle[\text{out}](O,C)
    \tkzFillPolygon[teal!20](M,N,P,O)
  \end{scope}

  \begin{scope}
    \tkzClipCircle(P,C) \tkzClipCircle(N,A)
    \tkzFillPolygon[teal!20](N,P,D)
  \end{scope}

  \begin{scope}
    \tkzClipCircle(O,C) \tkzClipCircle(P,C)
    \tkzFillPolygon[teal!20](P,C,O)
  \end{scope}

  \begin{scope}
    \tkzClipCircle(M,B) \tkzClipCircle(O,B)
    \tkzFillPolygon[teal!20](O,B,M)
  \end{scope}

  \begin{scope}
    \tkzClipCircle(N,A) \tkzClipCircle(M,A)
    \tkzFillPolygon[teal!20](A,M,N)
  \end{scope}

  \tkzDrawSemiCircles(M,B N,A O,C P,D)
  \tkzDrawPolygons(A,B,C,D M,N,P,O)
\end{tikzpicture}
```
45. Some interesting examples

45.7. Similar isosceles triangles

The following is from the excellent site Descartes et les Mathématiques. I did not modify the text and I am only the author of the programming of the figures. http://debart.pagesperso-orange.fr/seconde/triangle.html

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Bibliography:

– Géométrie au Bac - Tangente, special issue no. 8 - Exercise 11, page 11
– Elisabeth Busser and Gilles Cohen: 200 nouveaux problèmes du "Monde" - POLE 2007 (200 new problems of "Le Monde")
– Affaire de logique n° 364 - Le Monde February 17, 2004

Two statements were proposed, one by the magazine Tangente and the other by Le Monde.

Editor of the magazine "Tangente": Two similar isosceles triangles AXB and BYC are constructed with main vertices X and Y, such that A, B and C are aligned and that these triangles are "indirect". Let α be the angle at vertex AXB = BYC. We then construct a third isosceles triangle XZY similar to the first two, with main vertex Z and "indirect". We ask to demonstrate that point Z belongs to the straight line (AC).

Editor of "Le Monde": We construct two similar isosceles triangles AXB and BYC with principal vertices X and Y, such that A, B and C are aligned and that these triangles are "indirect". Let α be the angle at vertex AXB = BYC. The point Z of the line segment [AC] is equidistant from the two vertices X and Y.
At what angle does he see these two vertices?

The constructions and their associated codes are on the next two pages, but you can search before looking. The programming respects (it seems to me ...) my reasoning in both cases.
45. Some interesting examples

45.8. Revised version of "Tangente"

\begin{tikzpicture}[scale=.8,rotate=60]
  \tkzDefPoint(6,0){X} \tkzDefPoint(3,3){Y}
  \tkzDefShiftPoint[X](-110:6){A} \tkzDefShiftPoint[X](-70:6){B}
  \tkzDefShiftPoint[Y](-110:4.2){A'} \tkzDefShiftPoint[Y](-70:4.2){B'}
  \tkzDefPointBy[translation= from A' to B ](Y) \tkzGetPoint{Y}
  \tkzDefPointBy[translation= from A' to B ](B') \tkzGetPoint{C}
  \tkzInterLL(A,B)(X,Y) \tkzGetPoint{O}
  \tkzDefMidPoint(X,Y) \tkzGetPoint{I}
  \tkzDefPointWith[orthogonal](I,Y)
  \tkzInterLL(I,tkzPointResult)(A,B) \tkzGetPoint{Z}
  \tkzDefCircle[circum](X,Y,B) \tkzGetPoint{O}
  \tkzDrawCircle(O,X)
  \tkzDrawLines[add = 0 and 1.5](A,C) \tkzDrawLines[add = 0 and 3](X,Y)
  \tkzDrawSegments(A,X B,X B,Y C,Y) \tkzDrawSegments[color=red](X,Z Y,Z)
  \tkzDrawPoints(A,B,C,X,Y,O,Z)
  \tkzLabelPoints(A,B,C,Z) \tkzLabelPoints[above right](X,Y,O)
\end{tikzpicture}
45. Some interesting examples

45.9. "Le Monde" version

\begin{tikzpicture}[scale=1.25]
  \tkzDefPoint(0,0){A}
  \tkzDefPoint(3,0){B}
  \tkzDefPoint(9,0){C}
  \tkzDefPoint(1.5,2){X}
  \tkzDefPoint(6,4){Y}
  \tkzDefCircle[circum](X,Y,B) \tkzGetPoint{O}
  \tkzDefMidPoint(X,Y) \tkzGetPoint{I}
  \tkzDefPointWith[orthogonal](I,Y) \tkzGetPoint{i}
  \tkzDrawLines[add = 2 and 1,color=orange](I,i)
  \tkzInterLL(I,i)(A,B) \tkzGetPoint{Z}
  \tkzInterLC(I,i)(O,B) \tkzGetFirstPoint{M}
  \tkzDefPointWith[orthogonal](B,Z) \tkzGetPoint{b}
  \tkzDrawCircle(O,B)
  \tkzDrawLines[add = 0 and 2,color=orange](B,b)
  \tkzDrawSegments(A,X B,X B,Y C,Y A,C X,Y)
  \tkzDrawSegments[color=red](X,Z Y,Z)
  \tkzDrawPoints(A,B,C,X,Y,Z,M,I)
  \tkzDrawPoints[above right](X,Y,M,I)
\end{tikzpicture}
45.10. Triangle altitudes

45. Some interesting examples

45.11. Altitudes – other construction

\begin{tikzpicture}
\tkzDefPoint(0,0){A} \tkzDefPoint(8,0){B}
\tkzDefPoint(5,6){C}
\tkzDefMidPoint(A,B)\tkzGetPoint{O}
\tkzDefPointBy[projection=onto A--B](C) \tkzGetPoint{P}
\tkzInterLC[common=A](C,A)(O,A)
\tkzGetFirstPoint{M}
\tkzInterLC(C,B)(O,A)
\tkzGetSecondPoint{N}
\tkzInterLL(B,M)(A,N)\tkzGetPoint{I}
\tkzDrawCircles[diameter](A,B I,C)
\tkzDrawSegments(C,A C,B A,B B,M A,N)
\tkzMarkRightAngles[fill=brown!20](A,M,B A,N,B A,P,C)
\tkzDrawSegment[style=dashed,color=orange](C,P)
\tkzLabelPoints(O,A,B,P)
\tkzLabelPoint[left](M){\$M\$}
\tkzLabelPoint[right](N){\$N\$}
\tkzLabelPoint[above](C){\$C\$}
\tkzLabelPoint[above right](I){\$I\$}
\tkzDrawPoints[color=red](M,N,P,I)
\tkzDrawPoints[color=brown](O,A,B,C)
\end{tikzpicture}
45. Some interesting examples

45.12. Three circles in an Equilateral Triangle

From Wikipedia: In geometry, the Malfatti circles are three circles inside a given triangle such that each circle is tangent to the other two and to two sides of the triangle. They are named after Gian Francesco Malfatti, who made early studies of the problem of constructing these circles in the mistaken belief that they would have the largest possible total area of any three disjoint circles within the triangle. Below is a study of a particular case with an equilateral triangle and three identical circles.

\begin{tikzpicture}[scale=.8]
\tkzDefPoints{0/0/A,8/0/B,0/4/a,8/4/b,8/8/c}
\tkzDefTriangle[equilateral](A,B) \tkzGetPoint{C}
\tkzDefMidPoint(A,B) \tkzGetPoint{M}
\tkzDefMidPoint(B,C) \tkzGetPoint{N}
\tkzDefMidPoint(A,C) \tkzGetPoint{P}
\tkzInterLL(A,N)(M,a) \tkzGetPoint{Ia}
\tkzDefPointBy[projection = onto A--B](Ia) \tkzGetPoint{ha}
\tkzInterLL(B,P)(M,b) \tkzGetPoint{Ib}
\tkzDefPointBy[projection = onto A--B](Ib) \tkzGetPoint{hb}
\tkzInterLL(A,C)(M,C) \tkzGetPoint{Ic}
\tkzDefPointBy[projection = onto A--C](Ic) \tkzGetPoint{hc}
\tkzInterLL(A,Ia)(B,Ib) \tkzGetPoint{G}
\tkzDefSquare(A,B) \tkzGetPoints{D}{E}
\tkzDrawPolygon(A,B,C)
\tkzClipBB
\tkzDrawSemiCircles[gray,dashed](M,B A,M A,B A,B A,G Ia)
\tkzDrawCircles[gray](Ia,ha Ib,hb Ic,hc)
\tkzDrawPolySeg(A,E,D,B)
\tkzDrawPoints(A,B,C,G)
\tkzDrawPoints(A,B,C,G,Ia,ib)
\tkzDrawSegments[gray,dashed](C,M A,N B,P M,a M,b A,a b b A,D Ia,ha)
\end{tikzpicture}
45.13. Law of sines

From Wikipedia: In trigonometry, the law of sines, sine law, sine formula, or sine rule is an equation relating the lengths of the sides of a triangle (any shape) to the sines of its angles.

\begin{equation}
\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}
\end{equation}

\(\hat{C} = \hat{D}\)

\(\frac{c}{2R} = \sin D = \sin C\)

Then

\(\frac{c}{\sin C} = 2R\)
45.14. Flower of Life

Sacred geometry can be described as a belief system attributing a religious or cultural value to many of the fundamental forms of space and time. According to this belief system, the basic patterns of existence are perceived as sacred because in contemplating them one is contemplating the origin of all things. By studying the nature of these forms and their relationship to each other, one may seek to gain insight into the scientific, philosophical, psychological, aesthetic and mystical laws of the universe. The Flower of Life is considered to be a symbol of sacred geometry, said to contain ancient, religious value depicting the fundamental forms of space and time. In this sense, it is a visual expression of the connections life weaves through all mankind, believed by some to contain a type of Akashic Record of basic information of all living things.

One of the beautiful arrangements of circles found at the Temple of Osiris at Abydos, Egypt (Rawles 1997). Weisstein, Eric W. "Flower of Life." From MathWorld–A Wolfram Web Resource. 
http://mathworld.wolfram.com/FlowerofLife.html
\begin{tikzpicture}[scale=.75]
\tkzSetUpLine[line width=2pt,color=teal!80!black]
\tkzSetUpCompass[line width=2pt,color=teal!80!black]
\tkzDefPoint(0,0){O} \tkzDefPoint(2.25,0){A}
\tkzDrawCircle(O,A)
\foreach \i in {0,...,5}{
  \tkzDefPointBy[rotation= center O angle 30+60*\i](A)\tkzGetPoint{a\i}
  \tkzDefPointBy[rotation= center {a\i} angle 120](O)\tkzGetPoint{b\i}
  \tkzDefPointBy[rotation= center {a\i} angle 180](O)\tkzGetPoint{c\i}
  \tkzDefPointBy[rotation= center {c\i} angle 120](a\i)\tkzGetPoint{d\i}
  \tkzDefPointBy[rotation= center {c\i} angle 60](d\i)\tkzGetPoint{f\i}
  \tkzDefPointBy[rotation= center {d\i} angle 60](f\i)\tkzGetPoint{e\i}
  \tkzDefPointBy[rotation= center {d\i} angle 180](e\i)\tkzGetPoint{h\i}
  \tkzDefPointBy[rotation= center {e\i} angle 180](h\i)\tkzGetPoint{k\i}
  \tkzDrawCircle(a\i,O)
  \tkzDrawCircle(b\i,a\i)
  \tkzDrawCircle(c\i,a\i)
  \tkzDrawArc[rotate](f\i,d\i)(-120)
  \tkzDrawArc[rotate](e\i,d\i)(180)
  \tkzDrawArc[rotate](d\i,f\i)(180)
  \tkzDrawArc[rotate](g\i,f\i)(60)
  \tkzDrawArc[rotate](h\i,d\i)(60)
  \tkzDrawArc[rotate](k\i,e\i)(60)
}
\tkzClipCircle(O,f0)
\end{tikzpicture}
45.15. Pentagon in a circle

To inscribe an equilateral and equiangular pentagon in a given circle.

\begin{tikzpicture}
\tkzDefPoint(0,0){O} \tkzDefPoint(5,0){A}
\tkzDefPoint(0,5){B} \tkzDefPoint(-5,0){C}
\tkzDefMidPoint(A,O) \tkzGetPoint{I}
\tkzInterLC(I,B)(I,A) \tkzGetPoints{F}{E}
\tkzInterCC(O,C)(B,E) \tkzGetPoints{D3}{D2}
\tkzInterCC(O,C)(B,F) \tkzGetPoints{D4}{D1}
\tkzDrawArc[angles](B,E)(180,360)
\tkzDrawArc[angles](B,F)(220,340)
\tkzDrawLine[add=.5 and .5](B,I)
\tkzDrawCircle(O,A)
\tkzDrawCircle[diameter](O,A)
\tkzDrawSegments(B,D C,A)
\tkzDrawPoints(A,...,D,O)
\tkzDrawPoints[shift={(0,0)},new](E,F,I,D1,D2,D3,D4)
\tkzDrawPoints[shift={(0,0)},new](E,F,I,D1,D2,D3,D4)
\tkzLabelPoints(A,...,D,O)
\tkzLabelPoints[shift={(0,0)},new](I,E,F,D1,D2,D3,D4)
\end{tikzpicture}
45. Some interesting examples

45.16. Pentagon in a square

To inscribe an equilateral and equiangular pentagon in a given square.

\begin{tikzpicture}
\tkzDefPoint(-5,-5){A} \tkzDefPoint(0,0){O}
\tkzDefPoint(+5,-5){B} \tkzDefPoint(0,-5){F}
\tkzDefPoint(+5,0){F'} \tkzDefPoint(0,+5){E} \tkzDefPoint(-5,0){K}
\tkzDefSquare(A,B) \tkzGetPoints{C}{D}
\tkzDefMidPoint(D,T) \tkzGetPoint{I}
\tkzInterLC(D,C)(E,B) \tkzGetSecondPoint{T}
\tkzInterCC[with nodes](O,D,I)(E,D,I) \tkzGetSecondPoint{H}
\tkzInterLC(O,H)(D,E) \tkzGetSecondPoint{M}
\tkzInterCC(O,E)(E,M) \tkzGetFirstPoint{Q}
\tkzInterCC[with nodes](O,O,E)(Q,E,M) \tkzGetFirstPoint{P}
\tkzInterCC[with nodes](O,O,E)(P,E,M) \tkzGetFirstPoint{N}
\tkzCompass(O,H)
\tkzCompass(E,H)
\tkzDrawArc(E,H)
\tkzDrawPolygon(A,B,C,D)
\tkzDrawCircle(O,E)
\tkzDrawSegments[T](T,I O,H E,F F',K)
\tkzDrawPoints(T,M,Q,P,N,I)
\tkzDrawPolygon(M,E,Q,P,N)
\tkzLabelPoints(A,B,O,N,P,Q,M,H)
\tkzLabelPoints[above right](C,D,E,I,T)
\end{tikzpicture}
45. Some interesting examples

45.17. Hexagon Inscribed

To inscribe a regular hexagon in a given equilateral triangle perfectly inside it (no boarders).
45.18. Power of a point with respect to a circle

\[ MA \times MB = MT^2 = MO^2 - OT^2 \]

\begin{tikzpicture}
  \pgfmathsetmacro{\r}{2}
  \pgfmathsetmacro{\xO}{6}
  \pgfmathsetmacro{\xE}{\xO-\r}
  \tkzDefPoints{0/0/M, \xO/0/O, \xE/0/E}
  \tkzDefCircle[\text{diameter}](M,O)
  \tkzGetPoint{I}
  \tkzInterCC(I,O)(O,E) \tkzGetPoints{T}{T'}
  \tkzDefShiftPoint[O](45:2){B}
  \tkzInterLC(M,B)(O,E) \tkzGetPoints{A}{B}
  \tkzDrawCircle(O,E)
  \tkzDrawSemiCircle[\text{dashed}](I,O)
  \tkzDrawLine(M,O)
  \tkzDrawLines(M,T O,T M,B)
  \tkzDrawPoints(A,B,T)
  \tkzLabelPoints[\text{above}](A,B,O,M,T)
\end{tikzpicture}
45. Some interesting examples

45.19. Radical axis of two non-concentric circles

From Wikipedia: In geometry, the radical axis of two non-concentric circles is the set of points whose power with respect to the circles are equal. For this reason the radical axis is also called the power line or power bisector of the two circles. The notation radical axis was used by the French mathematician M. Chasles as axe radical.

\begin{tikzpicture}
\tkzDefPoints{0/0/A,4/2/B,2/3/K}
\tkzInterCC[R](A,1)(K,3) \tkzGetPoints{a}{a'}
\tkzInterCC[R](B,2)(K,3) \tkzGetPoints{b}{b'}
\tkzDrawLines[color=red,add=2 and 2](a,a') \tkzDrawLines[color=red,add=1 and 1](b,b')
\tkzInterLL(a,a')(b,b') \tkzGetPoint{X}
\tkzDefPointBy[projection= onto A--B](X) \tkzGetPoint{H}
\tkzDrawCircle[R](A,1) \tkzDrawCircle[R](B,2)
\tkzDrawCircle[R,dashed,orange](K,3)
\tkzDrawPoints(A,B,H,X,a,b,a',b')
\tkzDrawLine(A,B)
\tkzDrawLine[add= 1 and 2](X,H)
\tkzLabelPoints(A,B,H,X,a,b,a',b')
\end{tikzpicture}
45.20. External homothetic center

From Wikipedia: Given two nonconcentric circles, draw radii parallel and in the same direction. Then the line joining the extremities of the radii passes through a fixed point on the line of centers which divides that line externally in the ratio of radii. This point is called the external homothetic center, or external center of similitude (Johnson 1929, pp. 19-20 and 41).
45.21. Tangent lines to two circles

For two circles, there are generally four distinct lines that are tangent to both if the two circles are outside each other. For two of these, the external tangent lines, the circles fall on the same side of the line; the external tangent lines intersect in the external homothetic center.

\begin{tikzpicture}
\pgfmathsetmacro{\r}{1/2}
\pgfmathsetmacro{\R}{2/3}
\pgfmathsetmacro{\rt}{\R-\r}
\tkzDefPoints{0/0/A,4/2/B,2/3/K}
\tkzDefMidPoint(A,B) \tkzGetPoint{I}
\tkzInterLC[R](A,B)(B,\rt) \tkzGetPoints{E}{F}
\tkzInterCC(I,B)(B,F) \tkzGetPoints{a}{a'}
\tkzInterLC[R](B,a)(B,\R) \tkzGetPoints{X'}{T'}
\tkzDefTangent[at=T'](B) \tkzGetPoint{h}
\tkzInterLL(T',h)(A,B) \tkzGetPoint{O}
\tkzInterLC[R](0,T')(A,\r) \tkzGetPoints{T}{T'}
\tkzDrawCircle[R](A,\r) \tkzDrawCircle[R](B,\R)
\tkzDrawCircle[R,orange](B,\rt) \tkzDrawCircle[orange,dashed](I,B)
\tkzDrawPoints(O,A,B,a,a',E,F,T',T)
\tkzDrawLines(O,B,A,a,B,T'A,T)
\tkzDrawLines[add= 1 and 8](T',h)
\tkzLabelPoints(O,A,B,a,a',E,F,T,T')
\end{tikzpicture}
45.22. Tangent lines to two circles with radical axis

As soon as two circles are not concentric, we can construct their radical axis, the set of points of equal power with respect to the two circles. We know that the radical axis is a line orthogonal to the line of the centers. Note that if we specify \( P \) and \( Q \) as the points of contact of one of the common exterior tangents with the two circles and \( D \) and \( E \) as the points of the circles outside \([AB]\), then \((DP)\) and \((EQ)\) intersect on the radical axis of the two circles. We will show that this property is always true and that it allows us to construct common tangents, even when the circles have the same radius.

\[
\begin{tikzpicture}
\tkzDefPoints{0/0/A,4/2/B,2/3/K}
\tkzDrawCircles[R](A,1 B,3)
\tkzInterCC[R](A,1)(K,3) \tkzGetPoints{a}{a'}
\tkzInterCC[R](B,3)(K,3) \tkzGetPoints{b}{b'}
\tkzInterLL(a,a')(b,b') \tkzGetPoint{X}
\tkzDefPointBy[projection= onto A--B](X) \tkzGetPoint{H}
\tkzGetPoint{C}
\tkzInterLC[R](A,B)(B,3) \tkzGetPoints{b1}{E}
\tkzInterLC[R](A,B)(A,1) \tkzGetPoints{a2}{D}
\tkzDefMidPoint(D,E) \tkzGetPoint{I}
\tkzDrawCircle[orange](I,D)
\tkzInterLC(X,H)(I,D) \tkzGetPoints{M}{M'}
\tkzInterLC(M,D)(A,D) \tkzGetPoints{P}{P'}
\tkzInterLC(M,E)(B,E) \tkzGetPoints{Q}{Q'}
\tkzInterLL(P,Q)(A,D) \tkzGetPoint{O}
\tkzDrawSegments[orange](A,P I,M B,Q)
\tkzDrawPoints(A,B,D,E,M,I,O,P,Q,X,H)
\tkzDrawLines(O,E M,D M,E O,Q)
\tkzDrawLine[add= 3 and 4,orange](X,H)
\tkzLabelPoints(A,B,D,E,M,I,O,P,Q,X,H)
\end{tikzpicture}
\]
45.23. Middle of a segment with a compass

This example involves determining the middle of a segment, using only a compass.
45.24. Definition of a circle _Apollonius_

**Definition of a circle _Apollonius_**

From Wikipedia: *Apollonius showed that a circle can be defined as the set of points in a plane that have a specified ratio of distances to two fixed points, known as foci. This Apollonian circle is the basis of the Apollonius pursuit problem. ... The solutions to this problem are sometimes called the circles of Apollonius.*

**Explanation**

A circle is the set of points in a plane that are equidistant from a given point O. The distance r from the center is called the radius, and the point O is called the center. It is the simplest definition but it is not the only one. Apollonius of Perga gives another definition: The set of all points whose distances from two fixed points are in a constant ratio is a circle.

With tkz-euclide is easy to show you the last definition

**The code and the analyse**

```latex
\documentclass{standalone}
% Excellent class to show the result and to verify the bounding box.
\usepackage{tkz-euclide}
% no need to use \usetkzobj !
\begin{document}
\begin{tikzpicture}[/scale=1.5]
% Firstly we defined two fixed point.
% The figure depends of these points and the ratio K
\tkzDefPoint(0,0){A}
\tkzDefPoint(4,0){B}
% tkz-euclide.sty knows about the apollonius's circle
% with K=2 we search some points like I such as IA=2 x IB
\tkzDefCircle[apollonius,K=2](A,B) \tkzGetPoint{K1}
\tkzGetLength{rAp}
\tkzDefPointOnCircle[R= angle 30 center K1 radius \rAp](I)
\tkzDefPointOnCircle[R= angle 280 center K1 radius \rAp](J)
\tkzDrawSegments[new](A,I I,B A,J J,B)
\tkzDrawCircle[R,color = teal,fill=teal!20,opacity=.4](K1,\rAp pt)
\tkzDrawPoints(A,B,K1,I,J)
\tkzDrawPoints(A,B,K1,I,J)
\tkzGetPoint{J}
\tkzDrawSegments[new](A,I B A J B)
\tkzDrawCircle[R,color = teal,fill=teal!20,opacity=.4](K1,\rAp pt)
\tkzDrawPoints(A,B,K1,I,J)
\tkzDrawSegments(A,B)
\tkzLabelPoints[below,font=\scriptsize](A,B,K1,I,J)
\end{tikzpicture}
\end{document}
```

*tkz-euclide* AlterMundus
The result

45.25. Application of Inversion: Pappus chain

From Wikipedia, the Pappus chain is a ring of circles between two tangent circles investigated by Pappus of Alexandria in the 3rd century AD.
45. Some interesting examples

\begin{tikzpicture}[ultra thin]
\tkzDefPoints{0/0/A,\xB/0/B,\xC/0/C,\xD/0/D}
\tkzDrawCircle[diameter,fill=teal!20](A,C)
\tkzDrawCircle[diameter,fill=teal!30](A,B)
\foreach \i in {\nc,...,0,...,\nc}
{\tkzDefPoint(\xJ,2*\r*\i){J}
\tkzDefPoint(\xJ,2*\r*\i-\r){H}
\tkzDefCircleBy[inversion = center A through C](J,H)
\tkzDrawCircle[diameter,fill=teal](tkzFirstPointResult,tkzSecondPointResult)}
\end{tikzpicture}

45.26. Book of lemmas proposition 1 Archimedes

If two circles touch at A, and if [CD], [EF] be parallel diameters in them, A, C and E are aligned.

\begin{tikzpicture}
\tkzDefPoints{0/0/O_1,0/1/O_2,0/3/A}
\tkzDefPoint(15:3){F}
\tkzInterLC(F,O_1)(O_1,A) \tkzGetSecondPoint{E}
\tkzDefLine[parallel=through O_2](E,F)
\tkzGetPoint{x}
\tkzInterLC(x,O_2)(O_2,A) \tkzGetPoints{D}{C}
\tkzDrawCircles(O_1,A O_2,A)
\tkzDrawSegments[new](O_1,A E,F C,D)
\tkzDrawSegments[purple](A,E A,F)
\tkzDrawPoints(A,O_1,O_2,E,F,C,D)
\tkzLabelPoints(A,O_1,O_2,E,F,C,D)
\end{tikzpicture}

(CD) || (EF) (AO_1) is secant to these two lines so \( \widehat{AO_1C} = \widehat{AO_1E} \).
Since the triangles \( AO_2C \) and \( AO_1E \) are isosceles the angles at the base are equal widehatACO_2 = \( \widehat{AEO_1} = \widehat{CAO_2} = \widehat{EAO_1} \). Thus A, C and E are aligned

45.27. Book of lemmas proposition 6 Archimedes

Let \( AC \), the diameter of a semicircle, be divided at B so that \( AC/AB = \phi \) or in any ratio. Describe semicircles within the first semicircle and on AB, BC as diameters, and suppose a circle drawn touching the all three semicircles. If GH be the diameter of this circle, to find relation between GH and AC.
Let GH be the diameter of the circle which is parallel to AC, and let the circle touch the semicircles on AC, AB, BC in D, E, F respectively.

Then, by Prop. 1 A, G and D are aligned, ainsi que D, H and C.

For a like reason A, E and H are aligned, C, F and G are aligned as also are B, E and G, B, F and H.

Let (AD) meet the semicircle on [AC] at I, and let (BD) meet the semicircle on [BC] in K. Join CI, CK meeting AE, BF in L, M, and let GL, HM produced meet AB in N, P respectively.

Now, in the triangle AGB, the perpendiculars from A, C on the opposite sides meet in L. Therefore by the properties of triangles, (GN) is perpendicular to (AC). Similarly (HP) is perpendicular to (BC).

Again, since the angles at I, K, D are right, (CK) is parallel to (AD), and (CI) to (BD).

Therefore

\[
\frac{AB}{BC} = \frac{AL}{LH} = \frac{AN}{NP} \quad \text{and} \quad \frac{BC}{AB} = \frac{CM}{MG} = \frac{PC}{NP}
\]

hence

\[
\frac{AN}{NP} = \frac{NP}{PC} \quad \text{so} \quad NP^2 = AN \times PC
\]

Now suppose that B divides [AC] according to the divine proportion that is:

\[
\phi = \frac{AB}{BC} = \frac{AC}{AB} \quad \text{then} \quad AN = \phi NP \text{ and NP} = \phi PC
\]

We have

\[
AC = AN + NP + PC \quad \text{either} \quad AB + BC = AN + NP + PC \quad \text{or} \quad (\phi + 1)BC = AN + NP + PC
\]

we get

\[
(\phi + 1)BC = \phi NP + NP + PC = (\phi + 1)NP + PC = \phi(\phi + 1)PC + PC = \phi^2 + \phi + 1)PC
\]

as

\[
\phi^2 = \phi + 1 \quad \text{then} \quad (\phi + 1)BC = 2(\phi + 1)PC \quad \text{i.e.} \quad BC = 2PC
\]

That is, p is the middle of the segment BC.

Part of the proof from https://www.cut-the-knot.org

45.28. "The" Circle of APOLLONIUS

The circle which touches all three excircles of a triangle and encompasses them is often known as "the" Apollonius circle (Kimberling 1998, p. 102)
The purpose of the first examples was to show the simplicity with which we could recreate these propositions. With TikZ you need to do calculations and use trigonometry while with `tkz-euclide` you only need to build simple objects. But don’t forget that behind or far above `tkz-euclide` there is TikZ. I’m only creating an interface between TikZ and the user of my package.

The last example is very complex and it is to show you all that we can do with `tkz-euclide`.

The code and the analysis

```latex
% !TEX TS-program = lualatex
\documentclass{standalone}
\usepackage{tkz-euclide}
\tkzSetUpColors[background=white,text=black]
\tkzSetUpCompass[color=orange,line width=.4pt,delta=10]
\tkzSetUpArc[color=gray,line width=.4pt]
\tkzSetUpPoint[size=2,color=teal]
\tkzSetUpLine[line width=.4pt,color=teal]
\tkzSetUpStyle[orange]{new}
\tikzset{every picture/.style={line width=.4pt}}

\begin{document}
\begin{tikzpicture}[scale=.75]
\tkzDefPoints{0/0/A,6/0/B,0.8/4/C}
\tkzDefTriangleCenter[euler](A,B,C) \tkzGetPoint{N} \or \tkzEulerCenter(A,B,C)
\tkzDefTriangleCenter[circum](A,B,C) \tkzGetPoint{O} \or \tkzCircumCenter(A,B,C)
\tkzDefTriangleCenter[lemoine](A,B,C) \tkzGetPoint{K}
\tkzDefTriangleCenter[ortho](A,B,C) \tkzGetPoint{H}
\tkzDefSpcTriangle[excentral,name=J](A,B,C){a,b,c}
\tkzDefSpcTriangle[centroid,name=M](A,B,C){a,b,c}
\tkzDefCircle[in](Ma,Mb,Mc) \tkzGetPoint{Sp}
% \tkzDefTriangleCenter[spieker](A,B,C) \tkzGetPoint{Sp}
% each center has three projections on the sides of the triangle ABC
% We can do this with one macro
\tkzDefProjExcenter[projection=onto A--C](Ja) \tkzGetPoint{Za} \tkzGetPoint{Ja}
\tkzDefLine[parallel=through Za](A,B) \tkzGetPoint{Xc}
\tkzDefLine[parallel=through Zc](B,C) \tkzGetPoint{Ya}
\tkzDefLine[parallel=through Ya](C,B) \tkzGetPoint{Yc}
\tkzDefPointBy[reflection=over Ja--Jc](C') \tkzGetPoint{A'}
\tkzDefPointBy[reflection=over Jc--Ja](A') \tkzGetPoint{B'}
\tkzDefPointBy[reflection=over Ja--Ja](C) \tkzGetPoint{B}
\tkzDefPointBy[reflection=over Ja--Ja](A) \tkzGetPoint{C}
% But we need to find the radius or a point on the circle
\tkzInterLL(K,O)(N,Sp) \tkzGetPoint{Q}
\tkzInterLC(A,B)(Q,Cb) \tkzGetFirstPoint{Ba}
\end{tikzpicture}
\end{document}
```
\tkzInterLC(A,C)(Q,Cb) \tkzGetPoints{Ac}{Ca}
\tkzInterLC(B,C')(Q,Cb) \tkzGetFirstPoint{Bc}
\tkzInterLC(Ja,Q)(Q,Cb) \tkzGetSecondPoint{F'a}
\tkzInterLC(Jc,Q)(Q,Cb) \tkzGetFirstPoint{F'c}
\tkzInterLC(Jb,Q)(Q,Cb) \tkzGetSecondPoint{F'b}
\tkzInterLC[common=F'a](Sp,F'a)(Ja,F'a) \tkzGetFirstPoint{Fa}
\tkzInterLC[common=F'b](Sp,F'b)(Jb,F'b) \tkzGetFirstPoint{Fb}
\tkzInterLC[common=F'c](Sp,F'c)(Jc,F'c) \tkzGetFirstPoint{Fc}
\tkzInterLC(Mc,Sp)(Q,Cb) \tkzGetFirstPoint{A''}
\tkzDefLine[parallel=through A''](N,Mc) \tkzGetPoint{q}
% Calculations are done, now you can draw, mark and label
\tkzDrawPolygon(A,B,C)
\tkzDrawCircle(Q,Bc)
\tkzDrawCircle[euler,lightgray](A,B,C)
\tkzDrawCircles(ex)(A,B,C,B,C,A,C,A,B)
\tkzDrawSegments[dashed](A,A' C,C' A',Zc Za,C' B,Cb B,Ab A,Ca C,Ac
Ja,Xa Jb,Yb Jc,Zc)
\begin{scope}
  \tkzClipCircle(Q,Cb) % We limit the drawing of the lines
  \tkzDrawLine[add=5 and 12,orange](K,O)
  \tkzDrawLine[add=12 and 28,red!50!black](N,Sp)
\end{scope}
\tkzDrawPoints(A,B,C,Xa,Xb,Yb,Yc,Za,Zc)
\tkzDrawPoints(A,B,C,Xa,Xb,Yb,Yc,Za,Zc)
\tkzLabelPoints(Ja,Jb,Jc,Q,Xa,Xb,Yb,Yc,Za,Zc)
\tkzLabelPoints[above](O,K,F'a,Fa,A'')
\tkzLabelPoints[below](B,F'c,Yc,N,Sp,Fc,Mc)
\tkzLabelPoints[above](O,K,F'a,Fa,A'')
\tkzLabelPoints[right](C)
\tkzLabelPoints[right](C)
\tkzDrawSegments[color=green!50!black](Mc,Mc,A'',A'',Q)
\tkzDrawSegments[color=red,dashed](Ac,Ab,Cb,Ba,Bc Ja,Jc A',Cb C',Ab)
\tkzDrawSegments[color=red](Cb,Ab,Ac Ba,Ca A',C')
\tkzMarkSegments[color=red,mark=|](Cb,Ab,Ac Ba,Ca)
\tkzMarkRightAngles(Jc,Zc,A Ja,Xa,B Jb,Yb,C)
\tkzDrawSegments[green,dashed](A,F'a B,F'b C,F'c)
\end{tikzpicture}
The result
Part X.

FAQ
46. FAQ

46.1. Most common errors

For the moment, I’m basing myself on my own, because having changed syntax several times, I’ve made a number of mistakes. This section is going to be expanded. With version 4.05 new problems may appear.

- The mistake I make most often is to forget to put an "s" in the macro used to draw more than one object: like \tkzDrawSegment(s) or \tkzDrawCircle(s) ok like in this example \tkzDrawPoint(A,B) when you need \tkzDrawPoints(A,B);

- Don’t forget that since version 4 the unit is obligatorily the “cm” it is thus necessary to withdraw the unit like here \tkzDrawCircle[R](O,3cm) which becomes \tkzDrawCircle[R](O,3). The traditional options of TikZ keep their units example below right = 12pt on the other hand one will write size=1.2 to position an arc in \tkzMarkAngle;

- The following error still happens to me from time to time. A point that is created has its name in brackets while a point that is used either as an option or as a parameter has its name in braces. Example \tkzGetPoint(A) When defining an object, use braces and not brackets, so write: \tkzGetPoint{A};

- The changes in obtaining the points of intersection between lines and circles sometimes exchange the solutions, this leads either to a bad figure or to an error.

\tkzGetPoint{A} in place of \tkzGetFirstPoint{A}. When a macro gives two points as results, either we retrieve these points using \tkzGetPoints{A}{B}, or we retrieve only one of the two points, using \tkzGetFirstPoint{A} or \tkzGetSecondPoint{A}. These two points can be used with the reference tkzFirstPointResult or tkzSecondPointResult. It is possible that a third point is given as tkzPointResult;

- Mixing options and arguments; all macros that use a circle need to know the radius of the circle. If the radius is given by a measure then the option includes a \texttt{R}.

- The angles are given in degrees, more rarely in radians.

- If an error occurs in a calculation when passing parameters, then it is better to make these calculations before calling the macro.

- Do not mix the syntax of \texttt{pgfmath} and \texttt{xfp}. I’ve often chosen \texttt{xfp} but if you prefer \texttt{pgfmath} then do your calculations before passing parameters.

- Error ”dimension too large” : In some cases, this error occurs. One way to avoid it is to use the ”\texttt{xfp}” option. When this option is used in an environment, the ”veclen” function is replaced by a function dependent on ”\texttt{xfp}”. For example, an error occurs if you use the macro \texttt{\tkzDrawArc} with too small an angle. The error is produced by the \texttt{decoration} library when you want to place a mark on an arc. Even if the mark is absent, the error is still present.
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